

# KD TREE DEMO



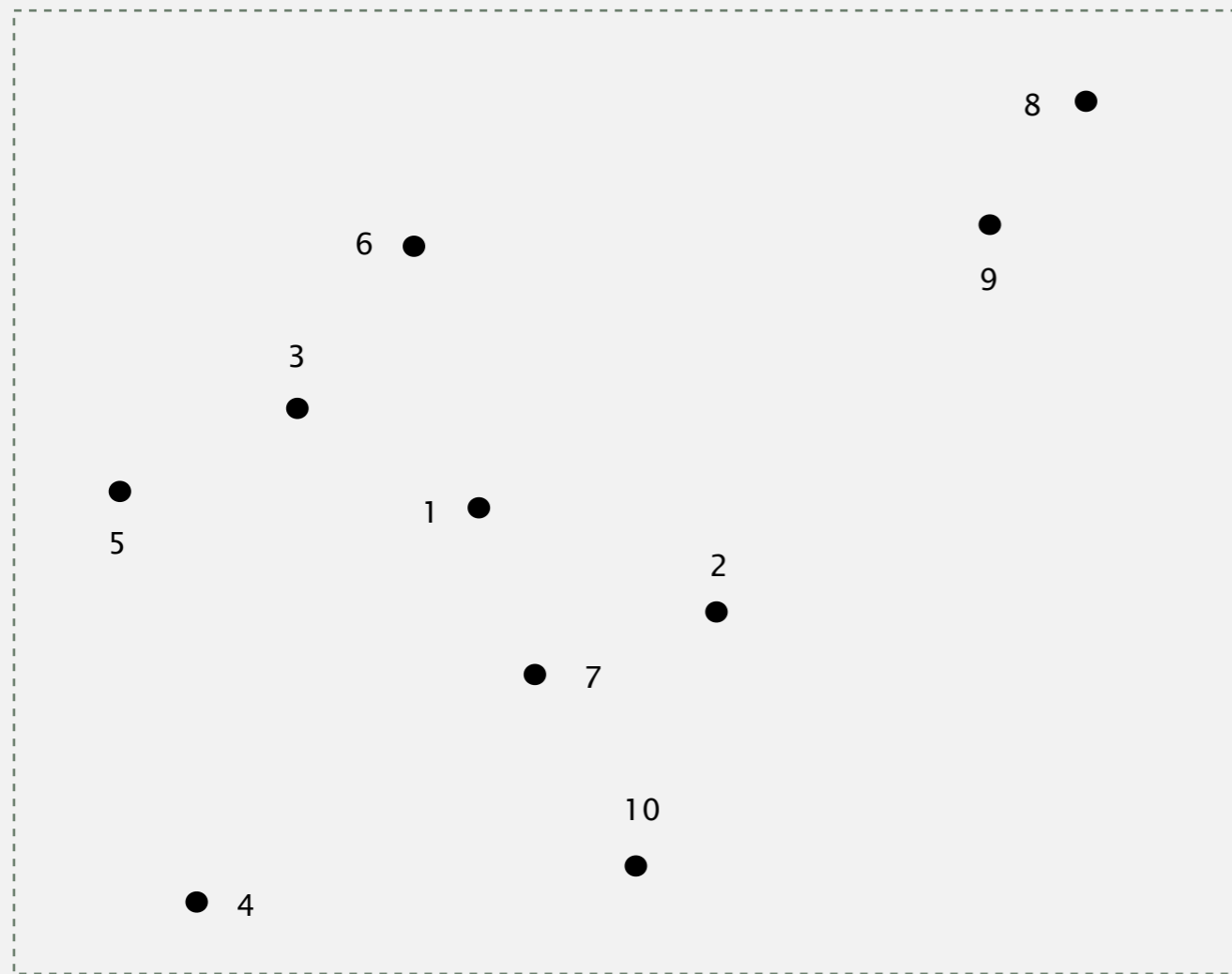
- ▶ insertion
- ▶ range search
- ▶ nearest neighbor search

**click to begin demo**

- ▶ **insertion**
- ▶ range search
- ▶ nearest neighbor search

## Insertion in a 2d tree

Recursively partition plane into two halfplanes.



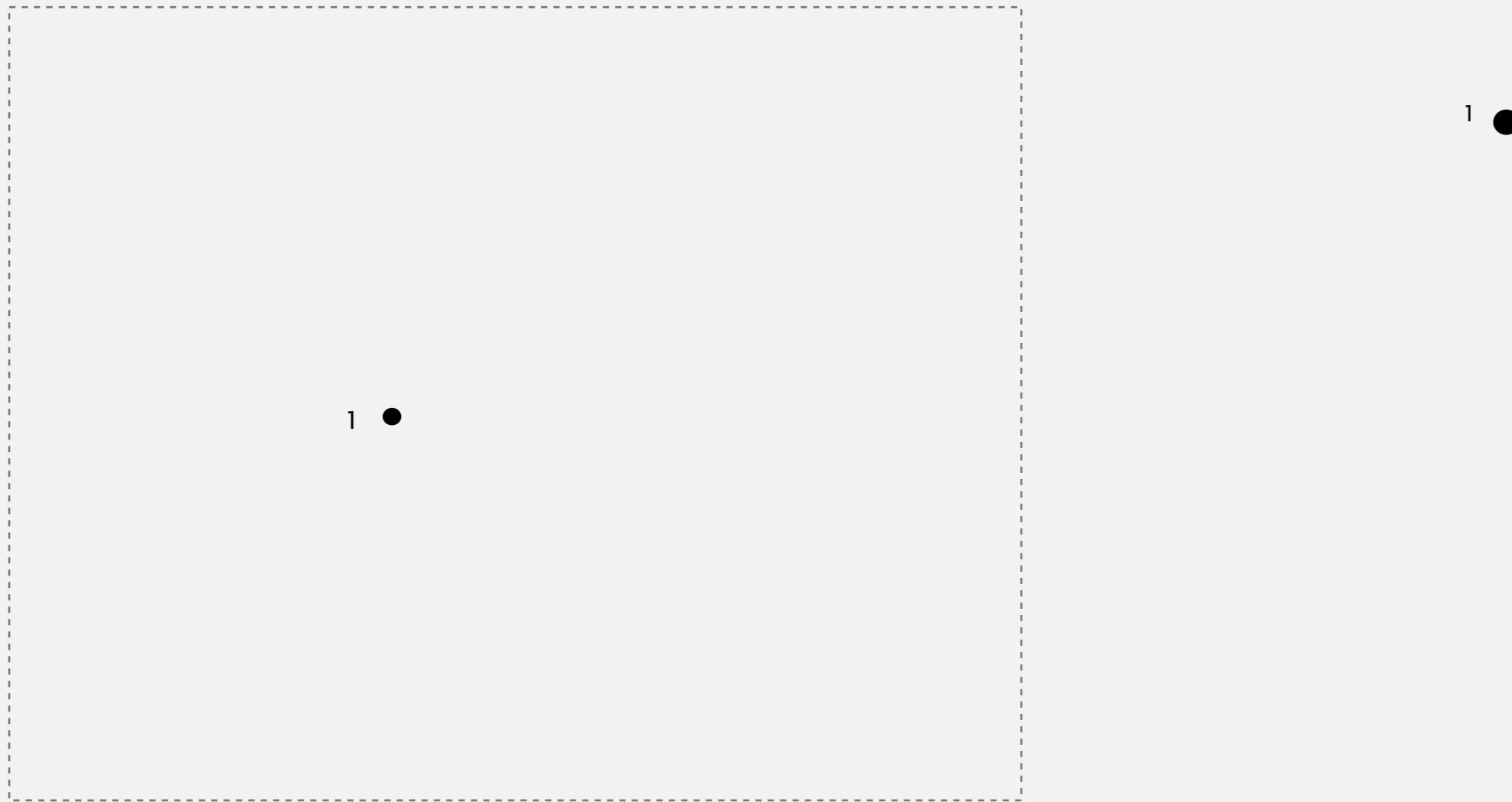
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Recursively partition plane into two halfplanes.



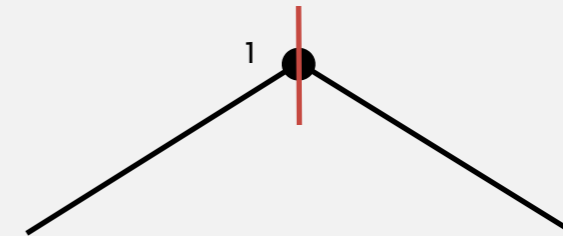
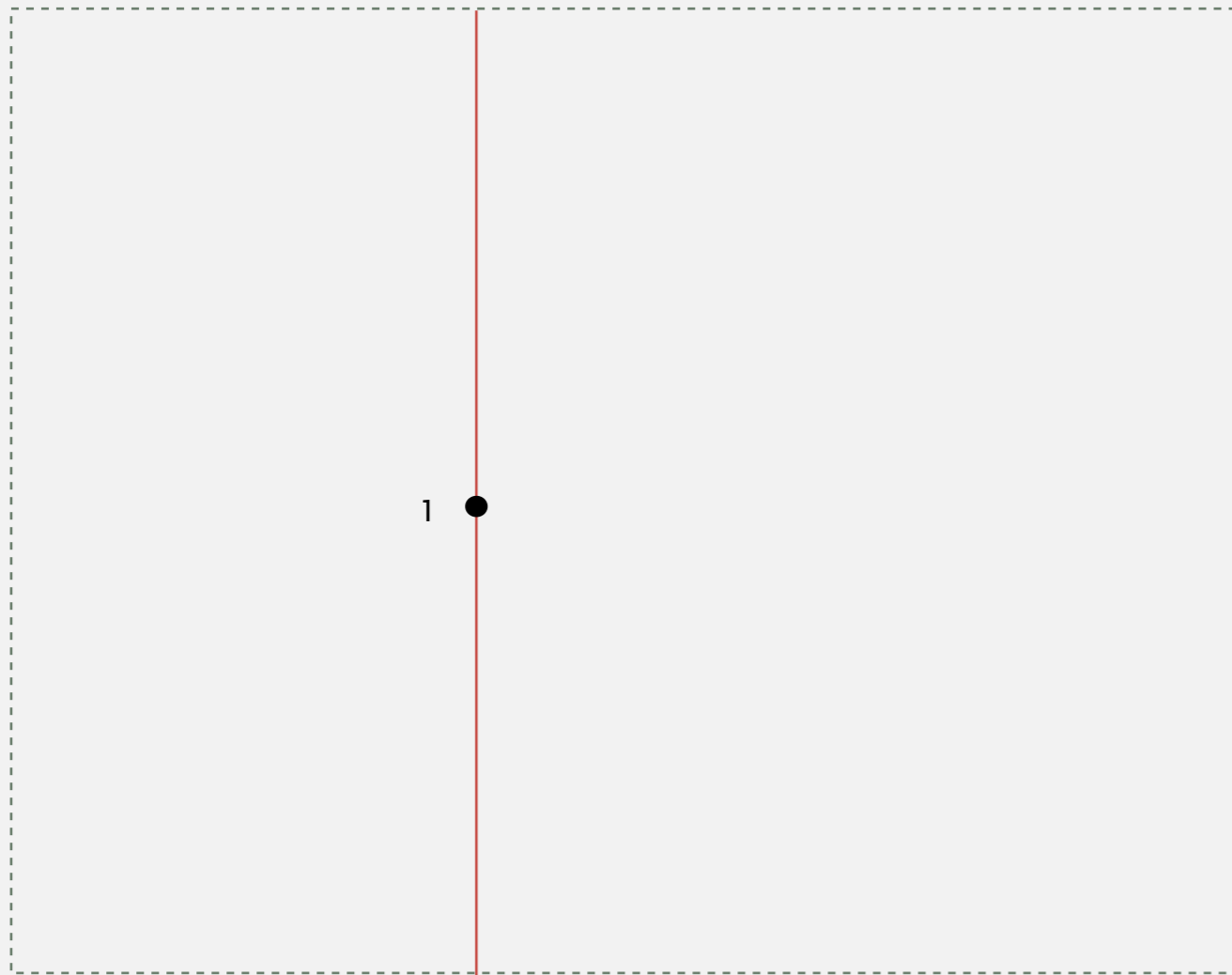
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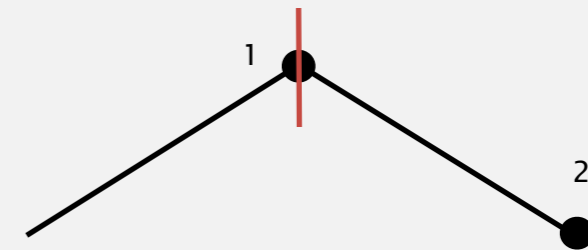
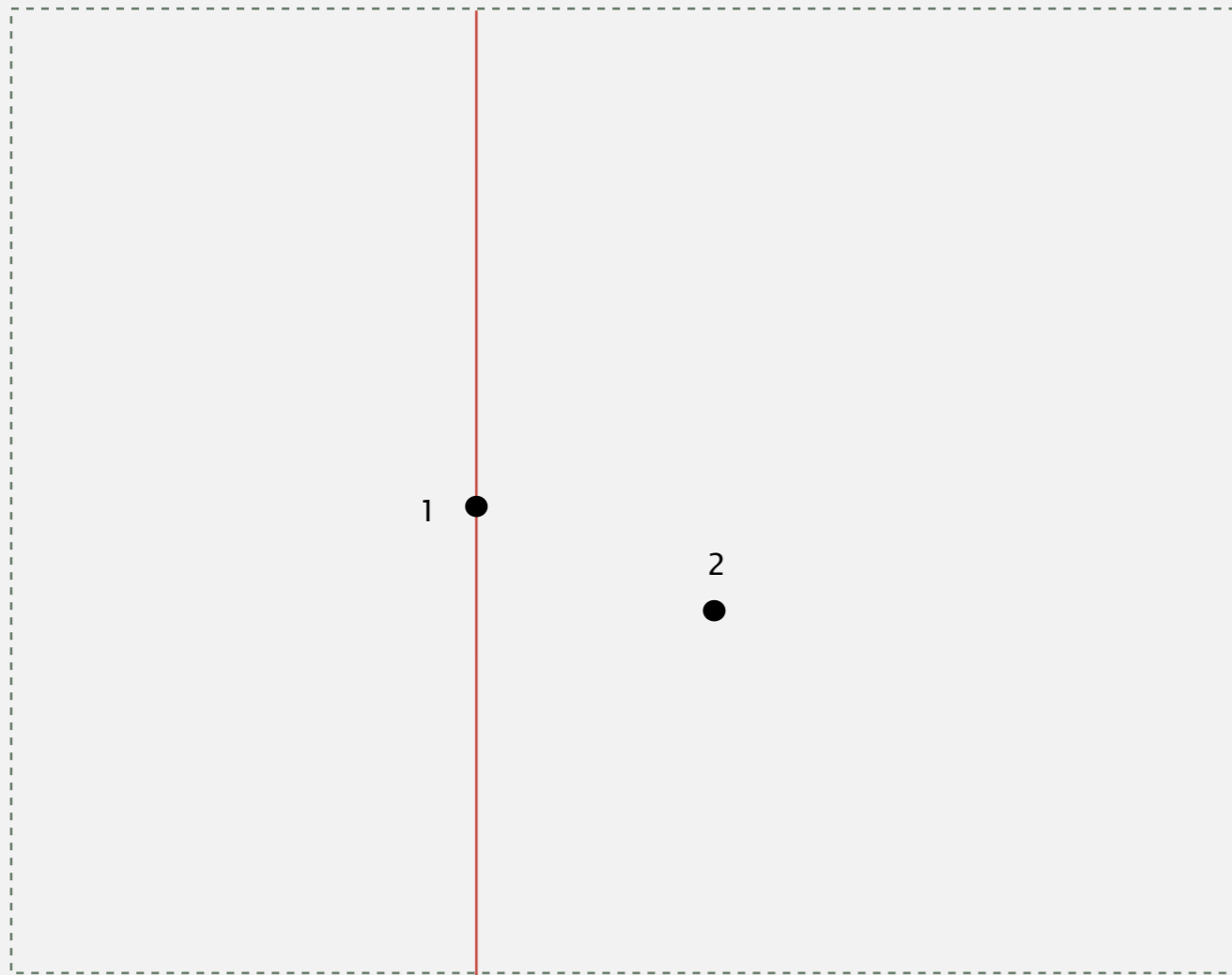
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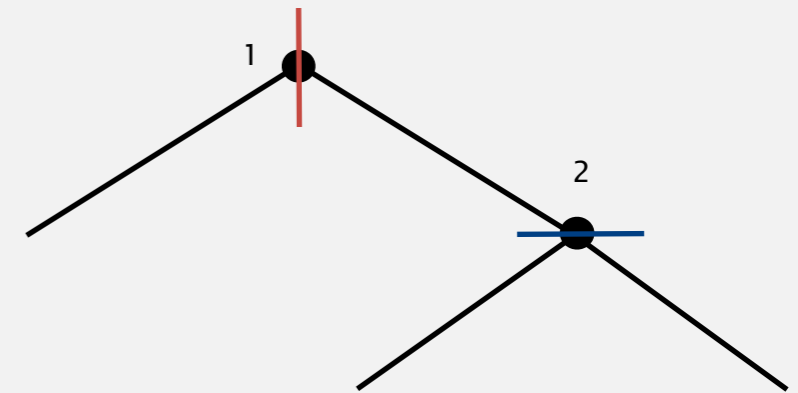
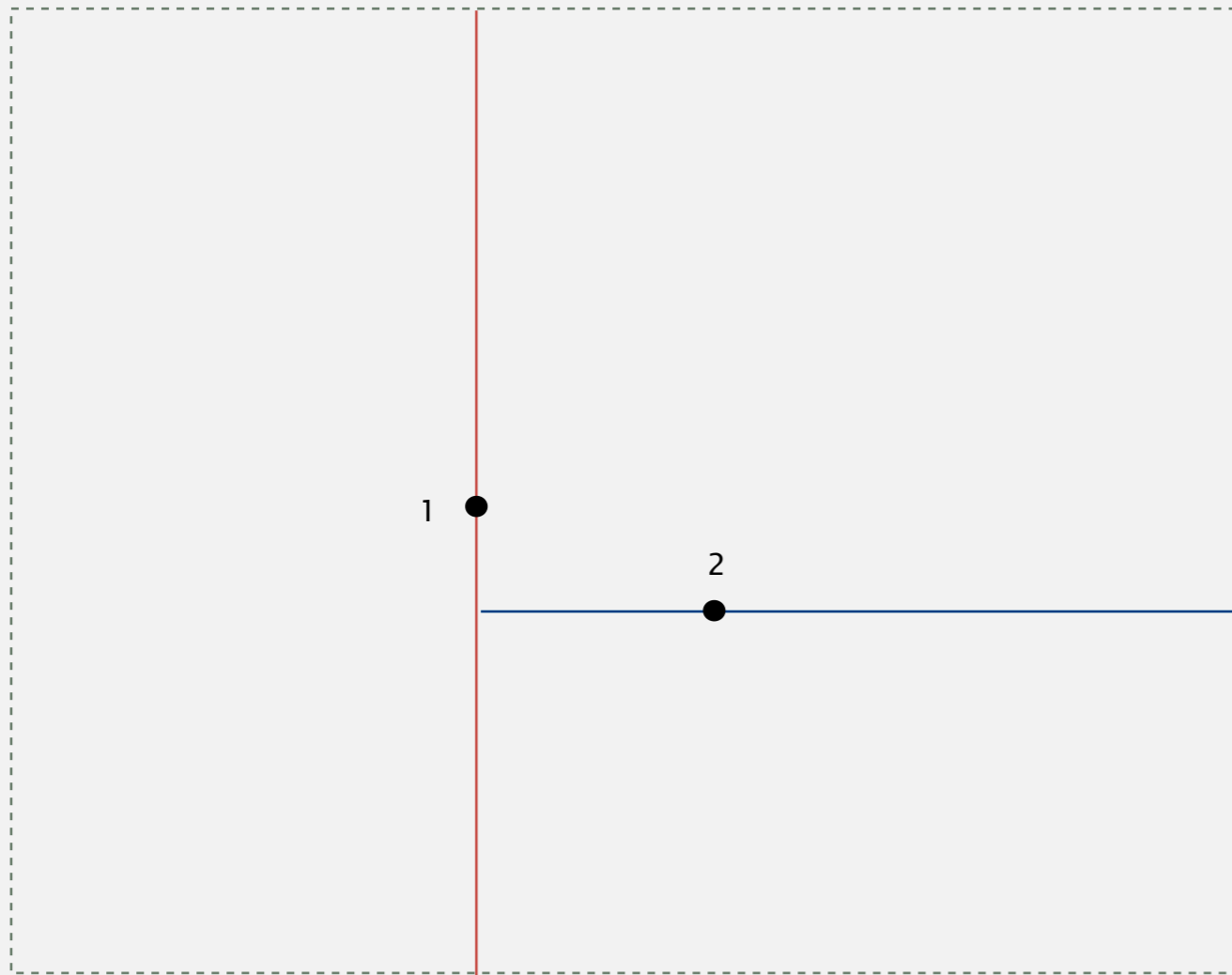
# Insertion in a 2d tree

Recursively partition plane into two halfplanes.



# Insertion in a 2d tree

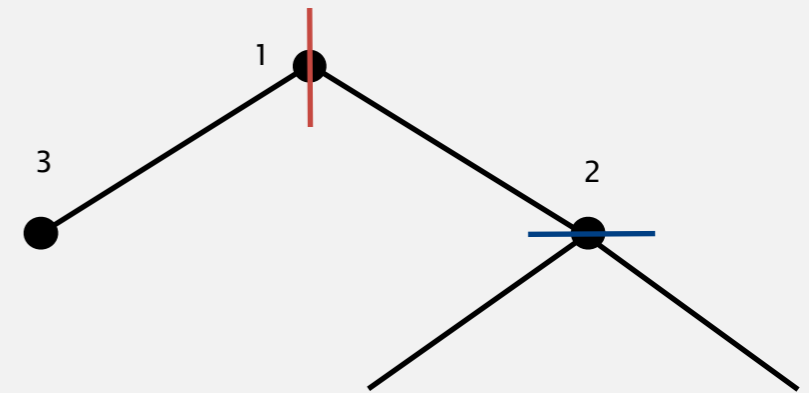
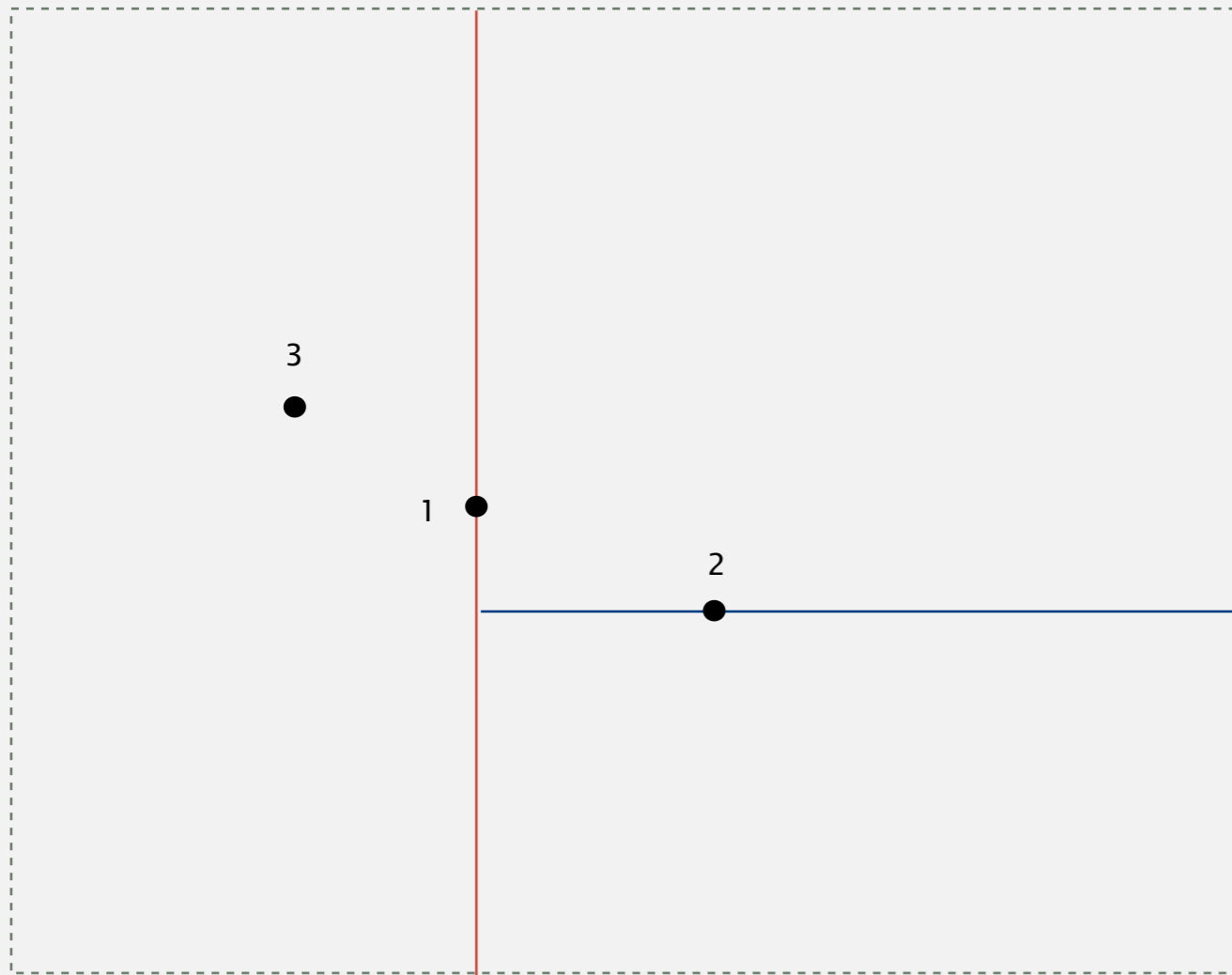
Recursively partition plane into two halfplanes.





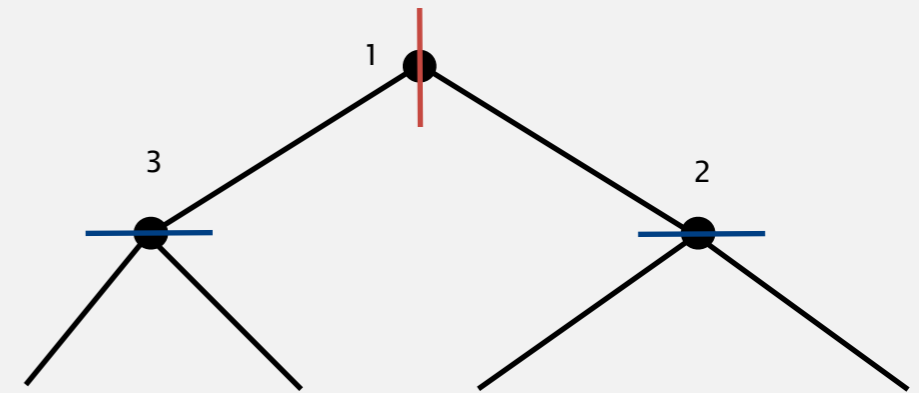
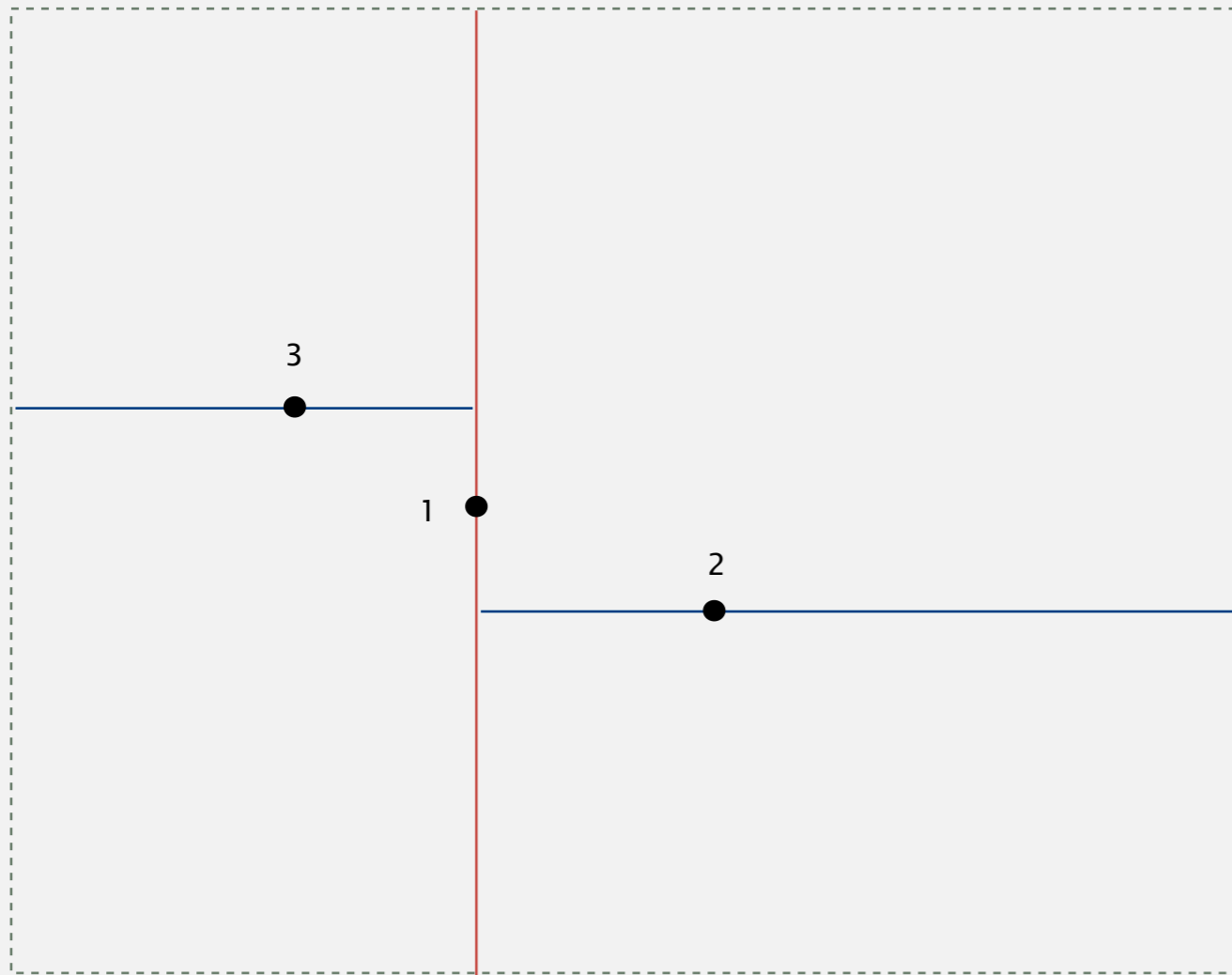
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Recursively partition plane into two halfplanes.



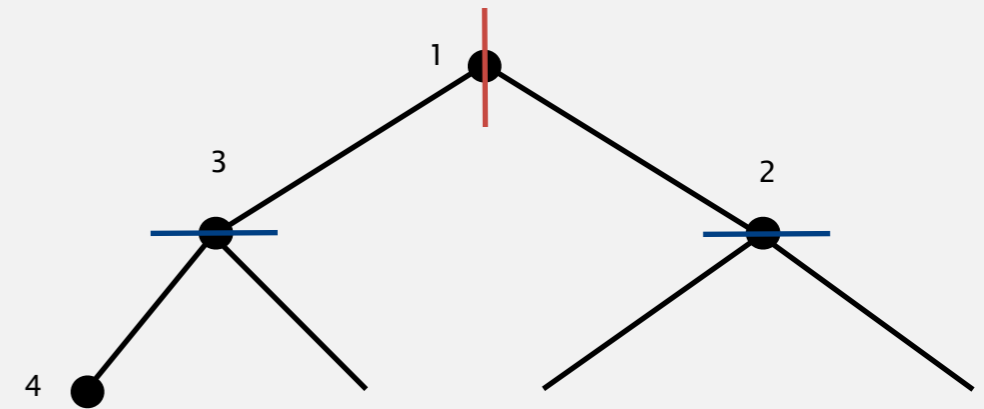
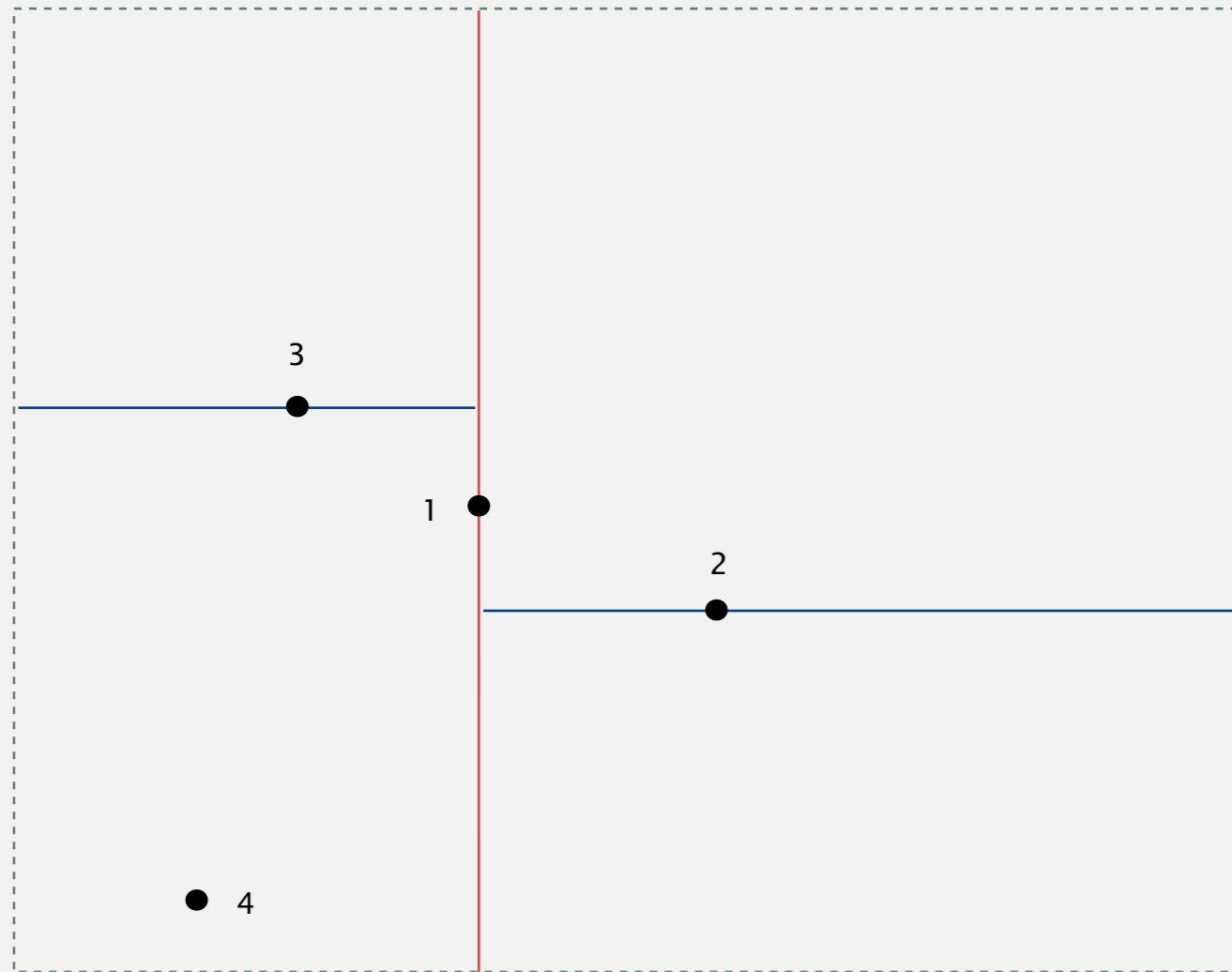
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Recursively partition plane into two halfplanes.



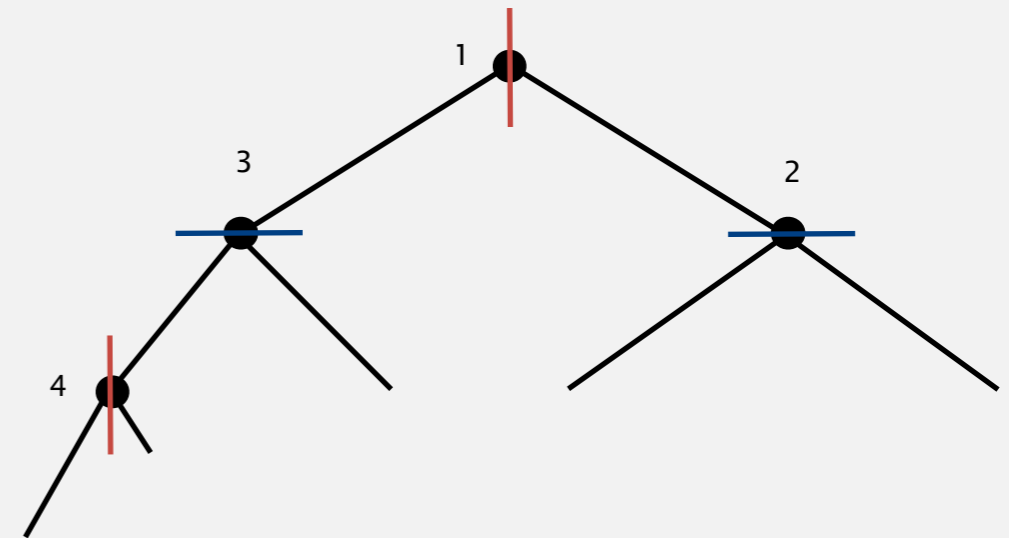
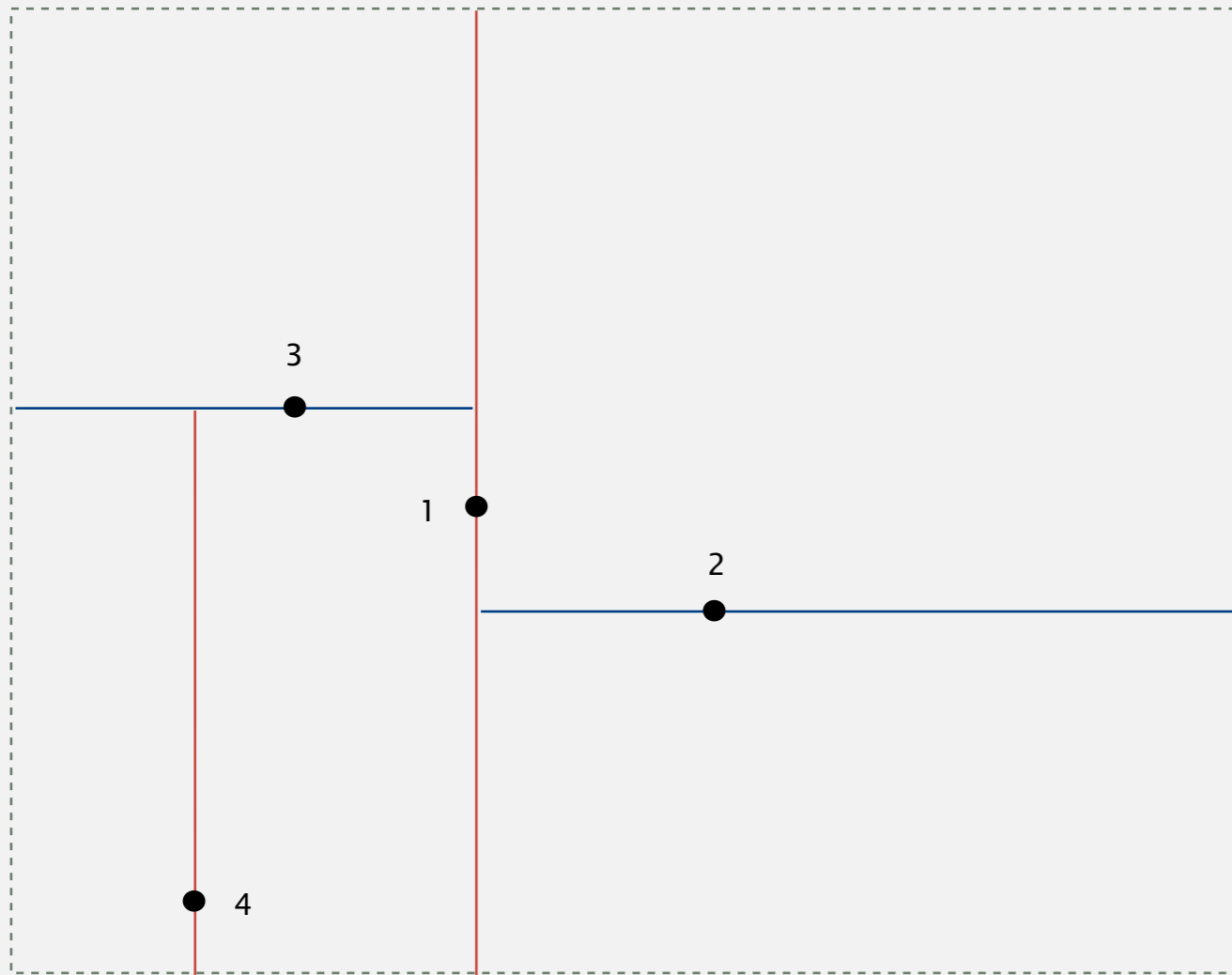
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Recursively partition plane into two halfplanes.



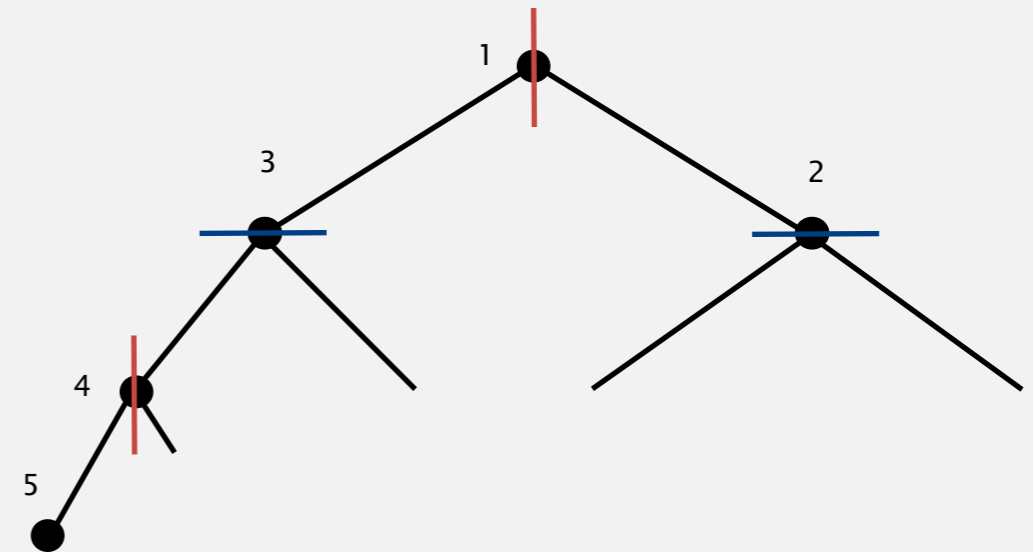
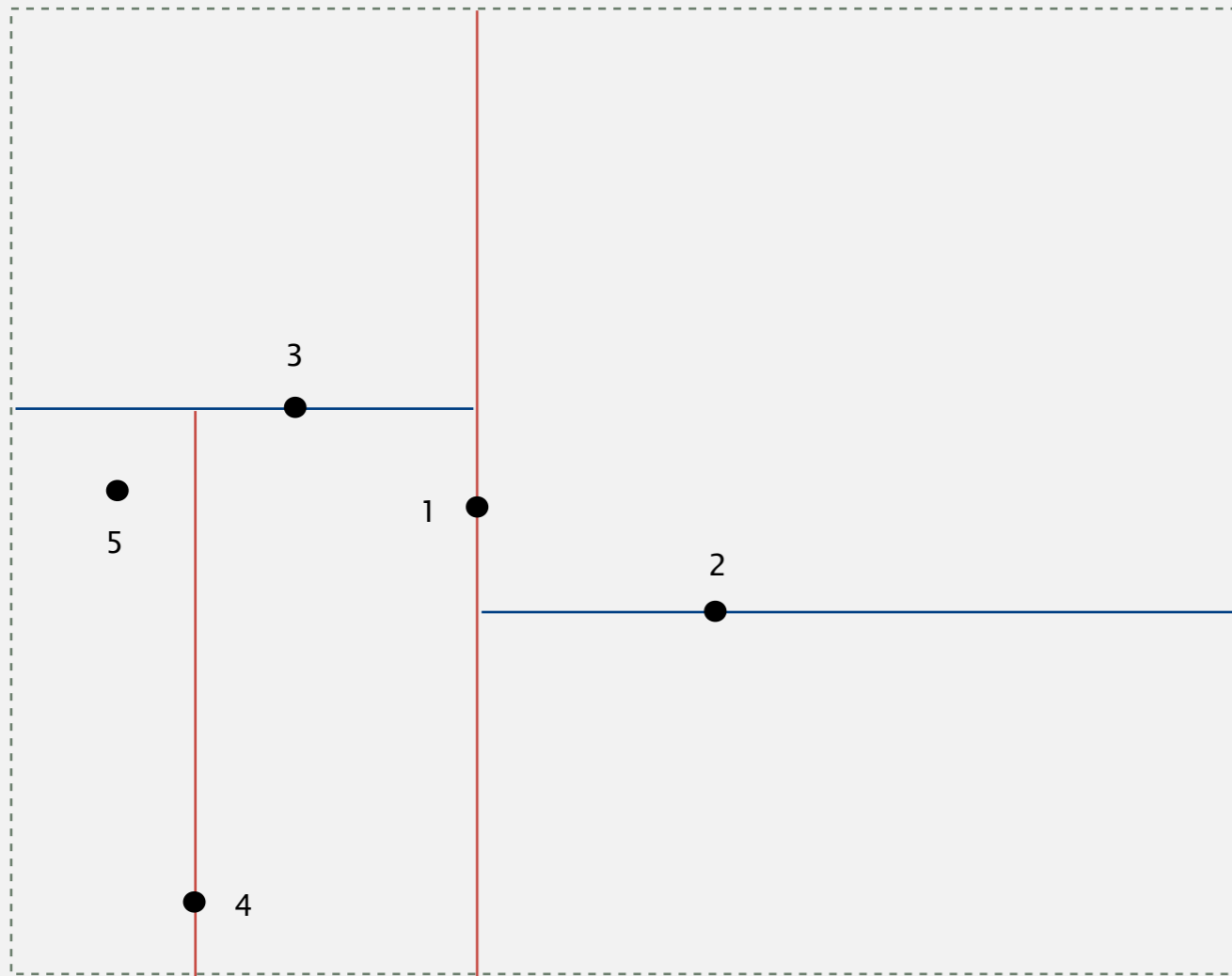
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Recursively partition plane into two halfplanes.



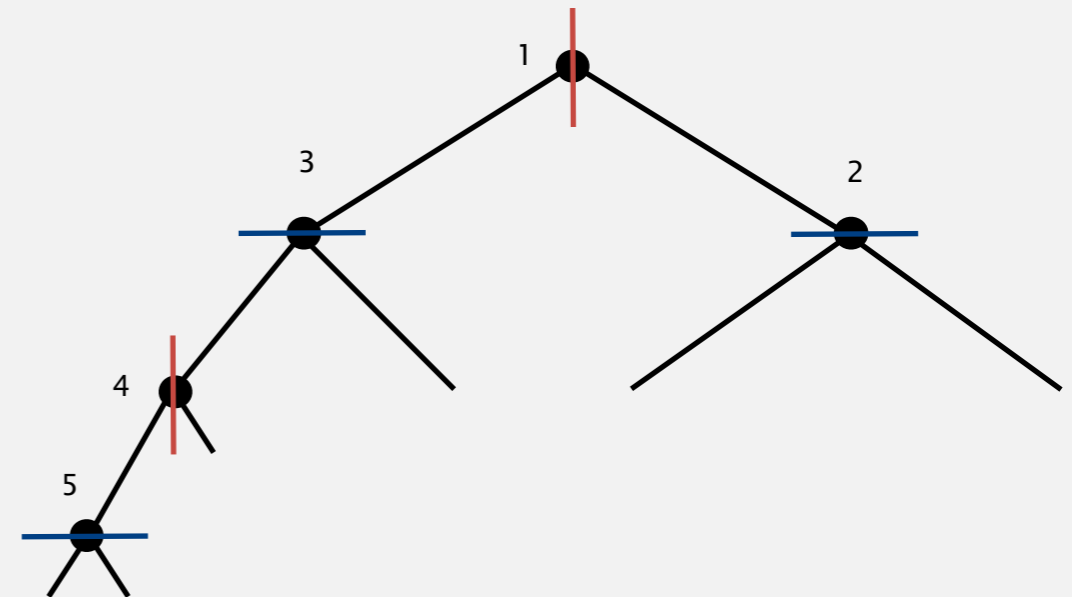
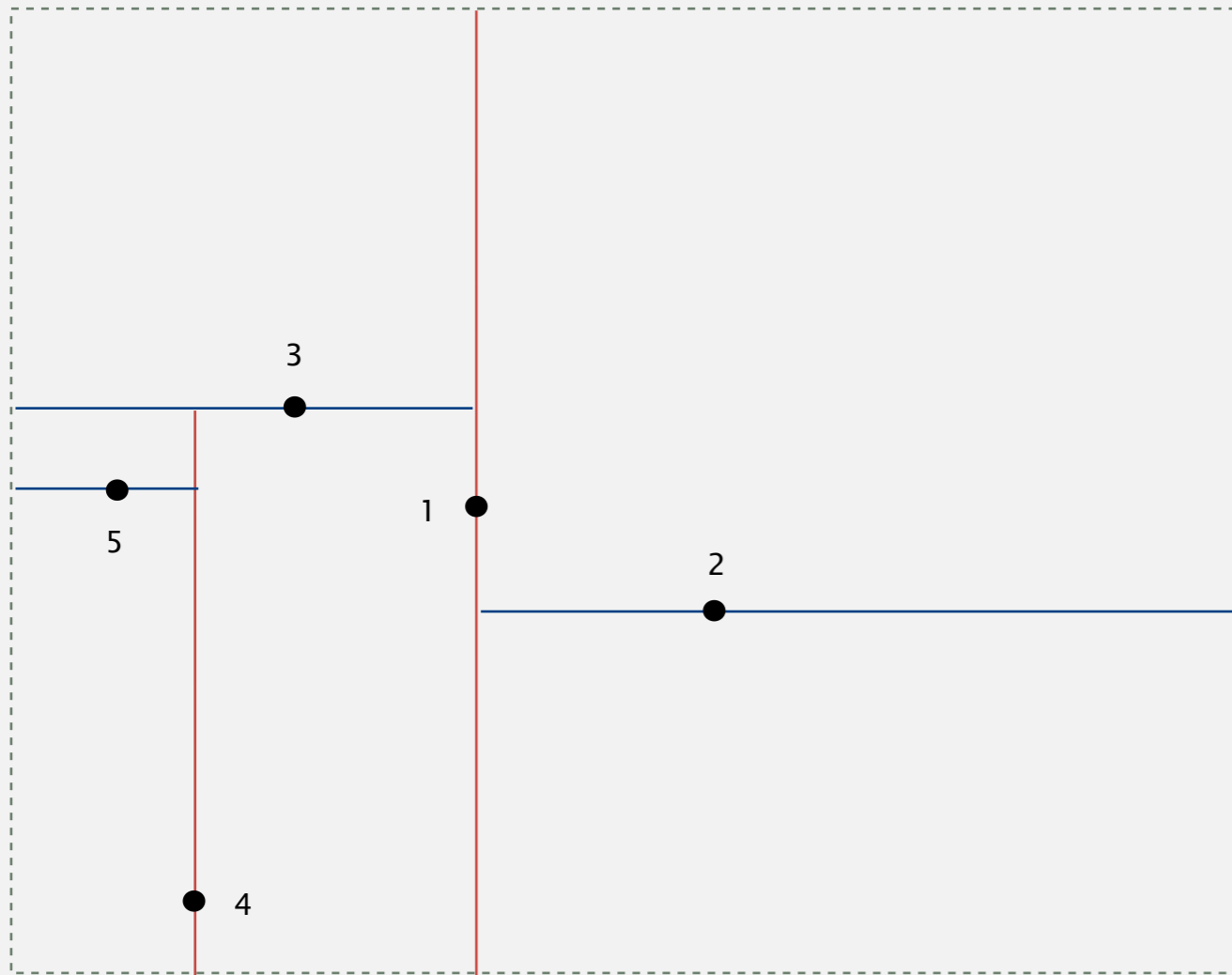
# Insertion in a 2d tree

Recursively partition plane into two halfplanes.



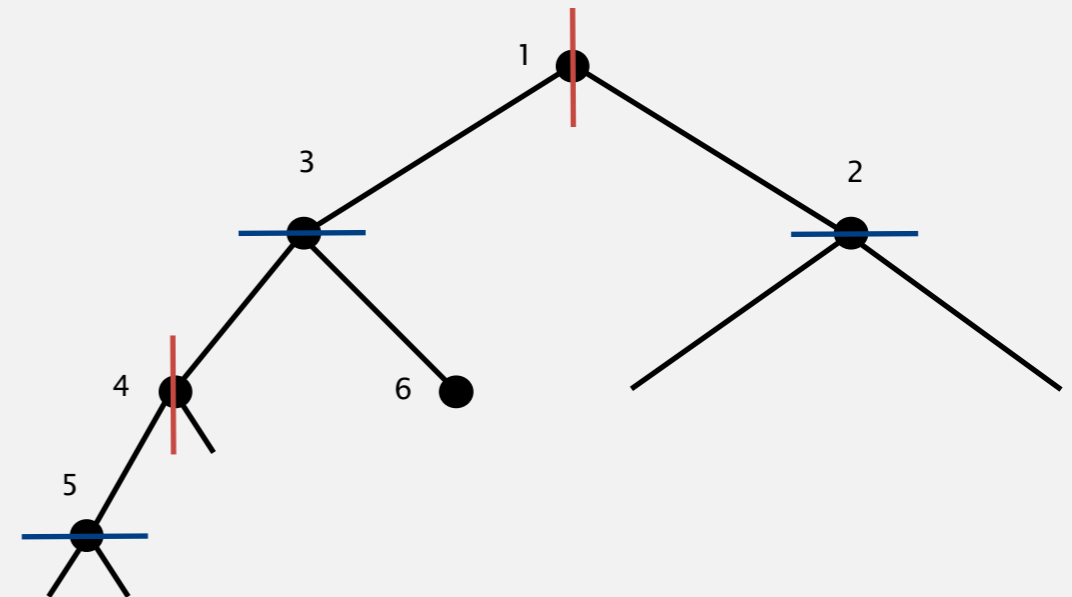
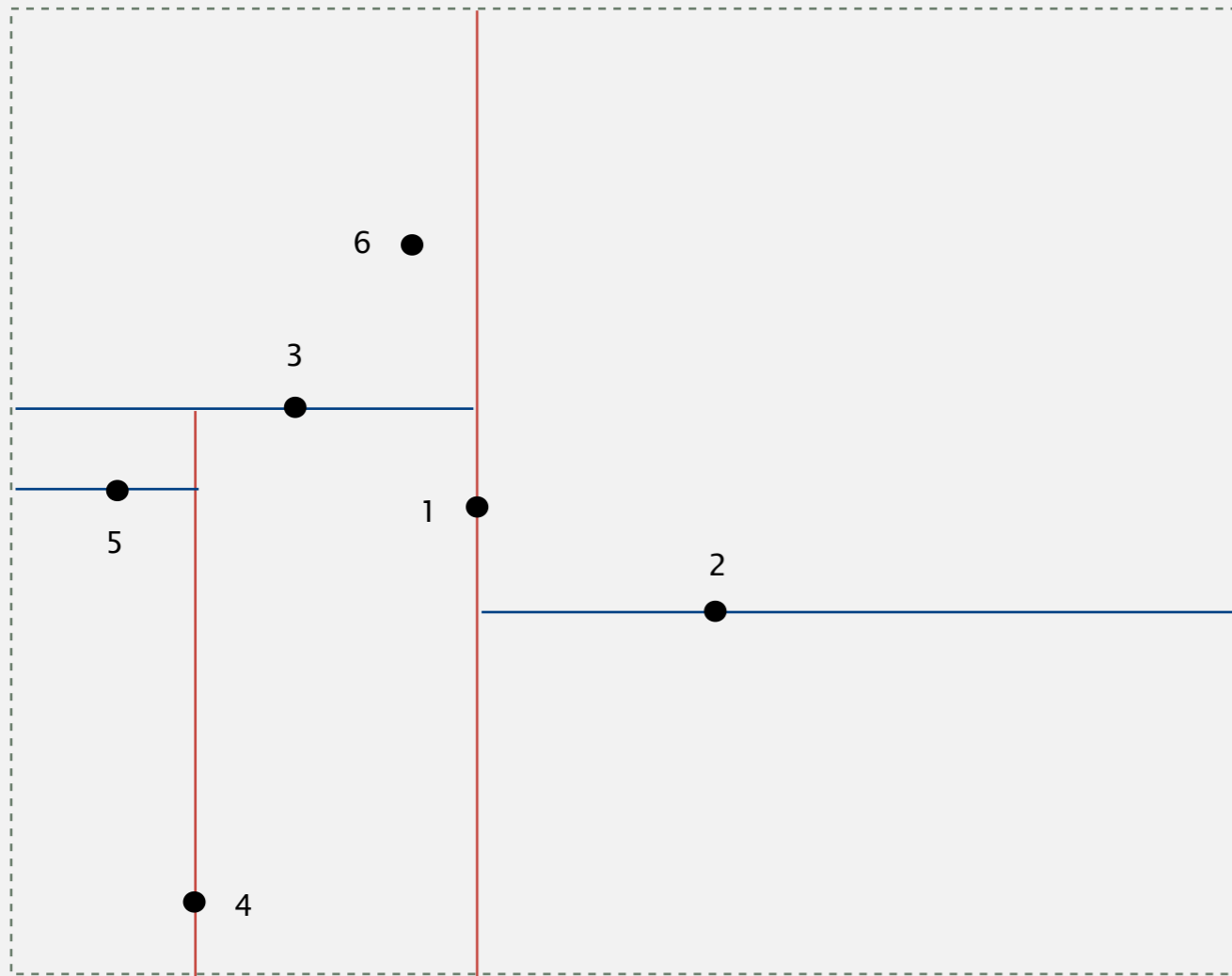
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Recursively partition plane into two halfplanes.



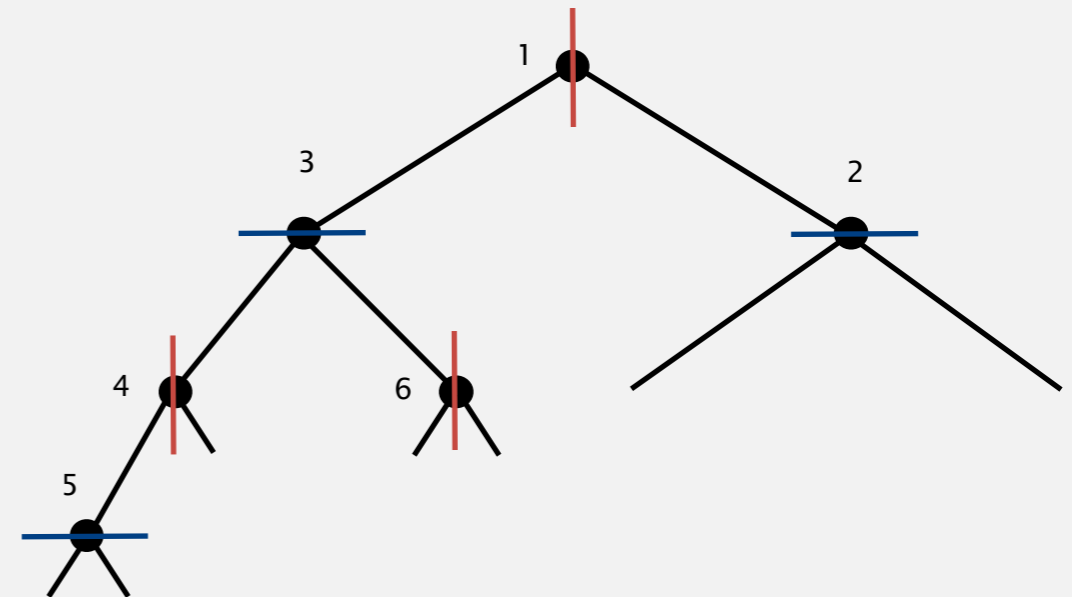
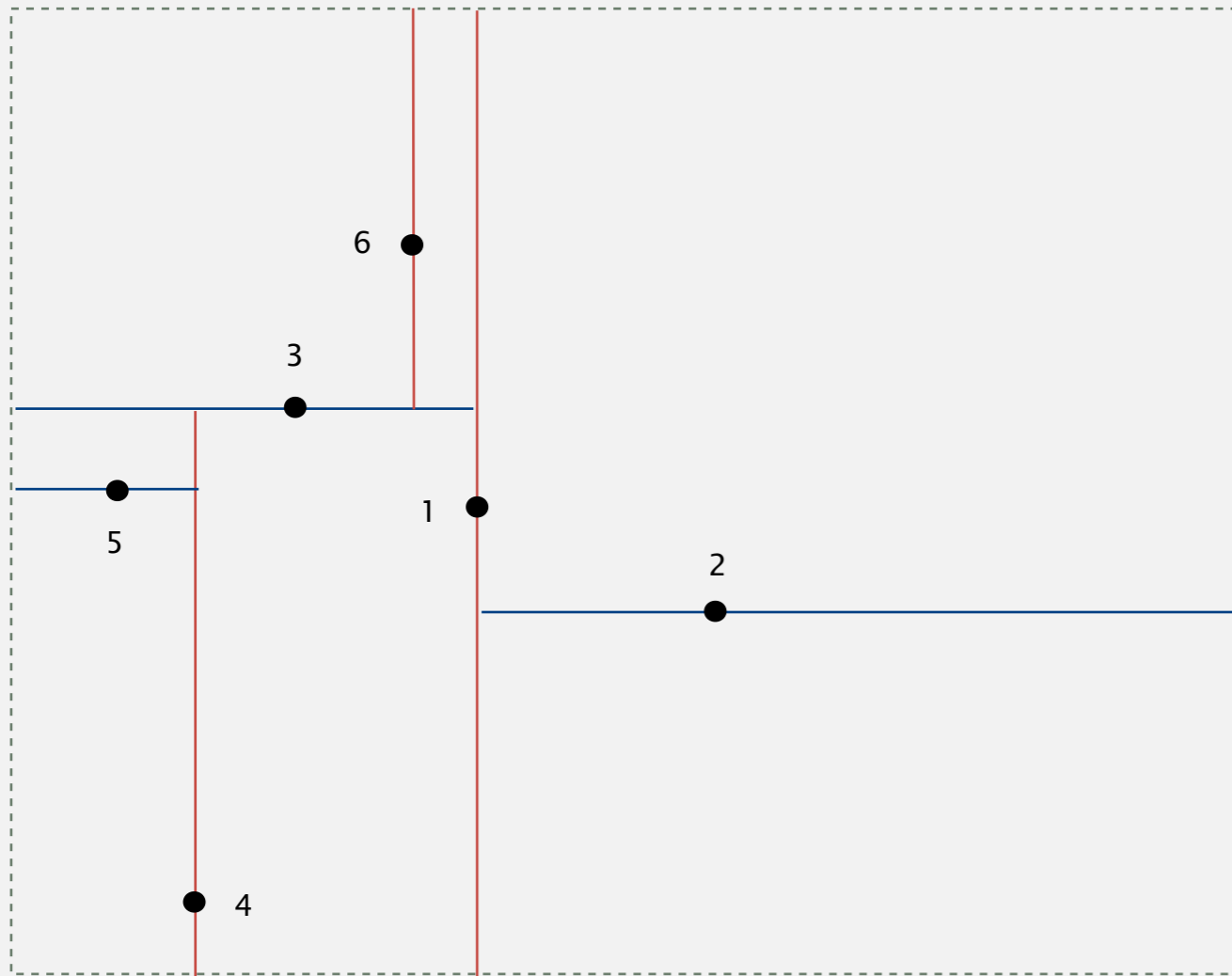
# Insertion in a 2d tree

Recursively partition plane into two halfplanes.



# Insertion in a 2d tree

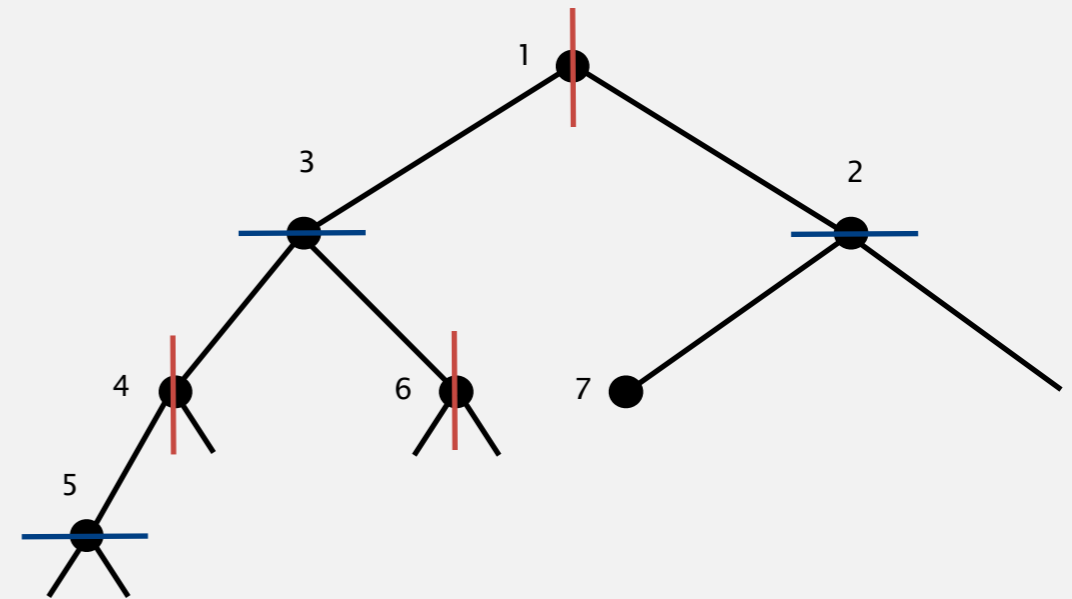
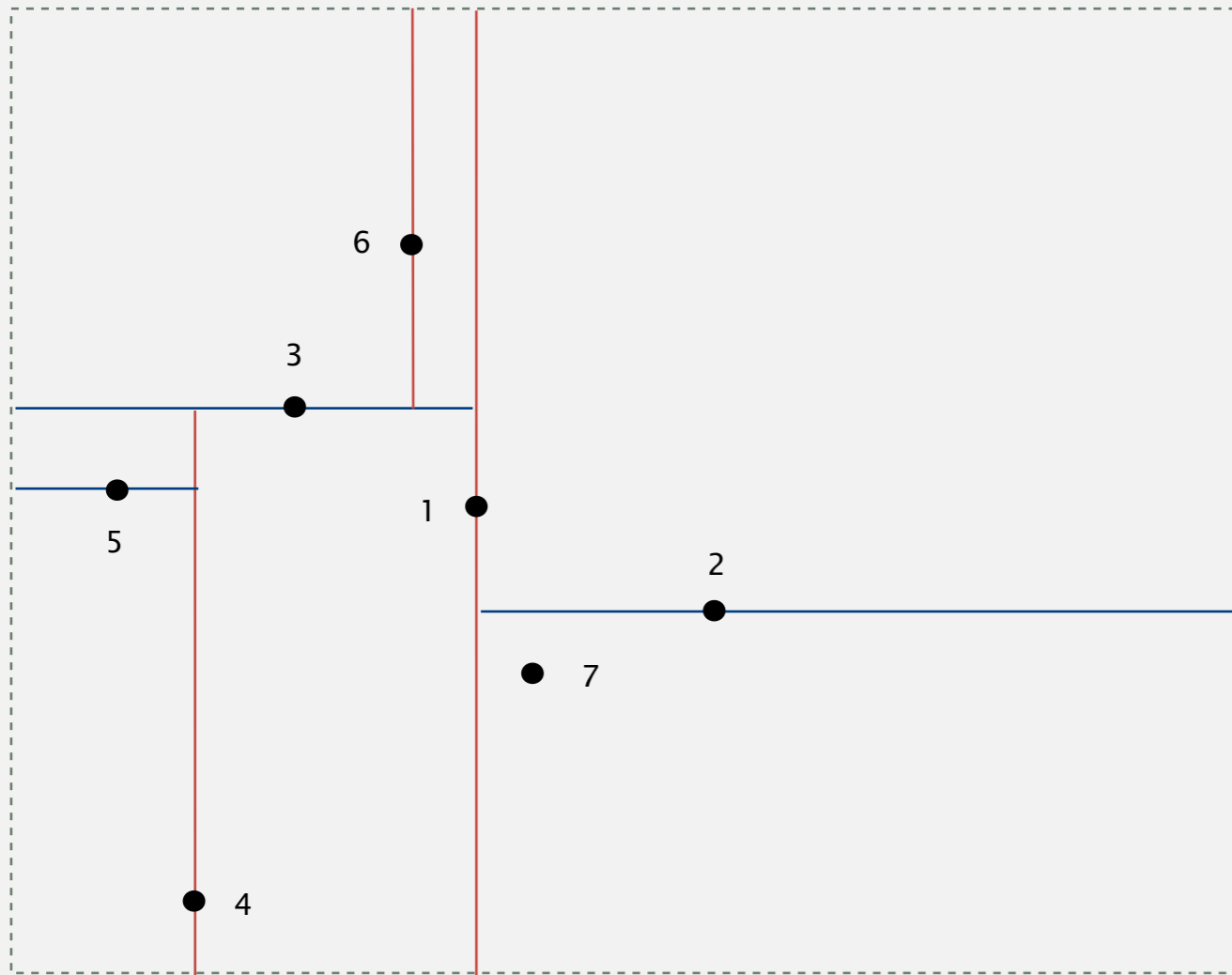
Recursively partition plane into two halfplanes.





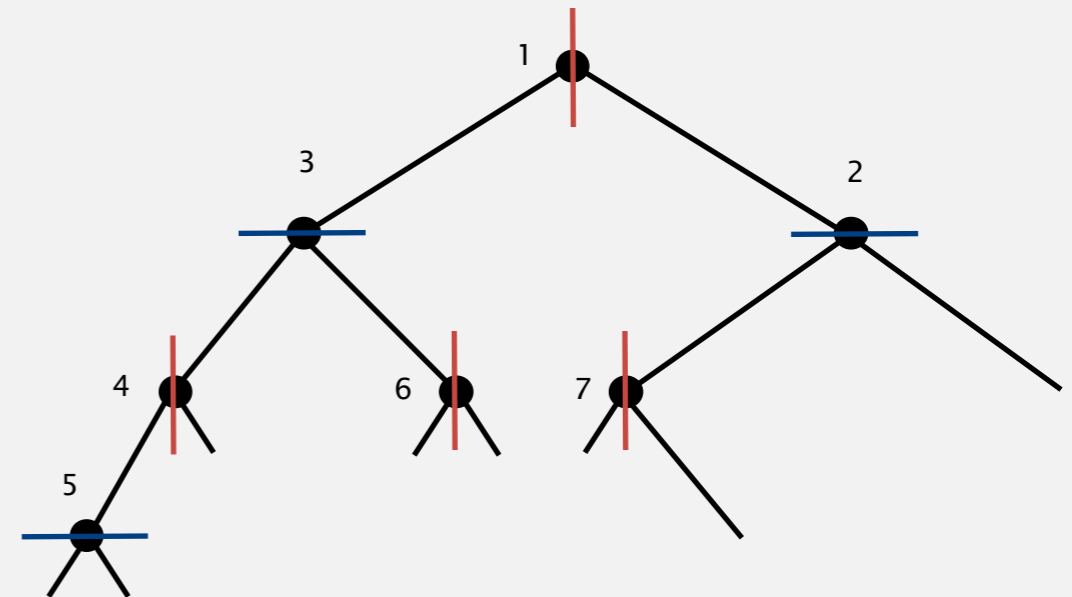
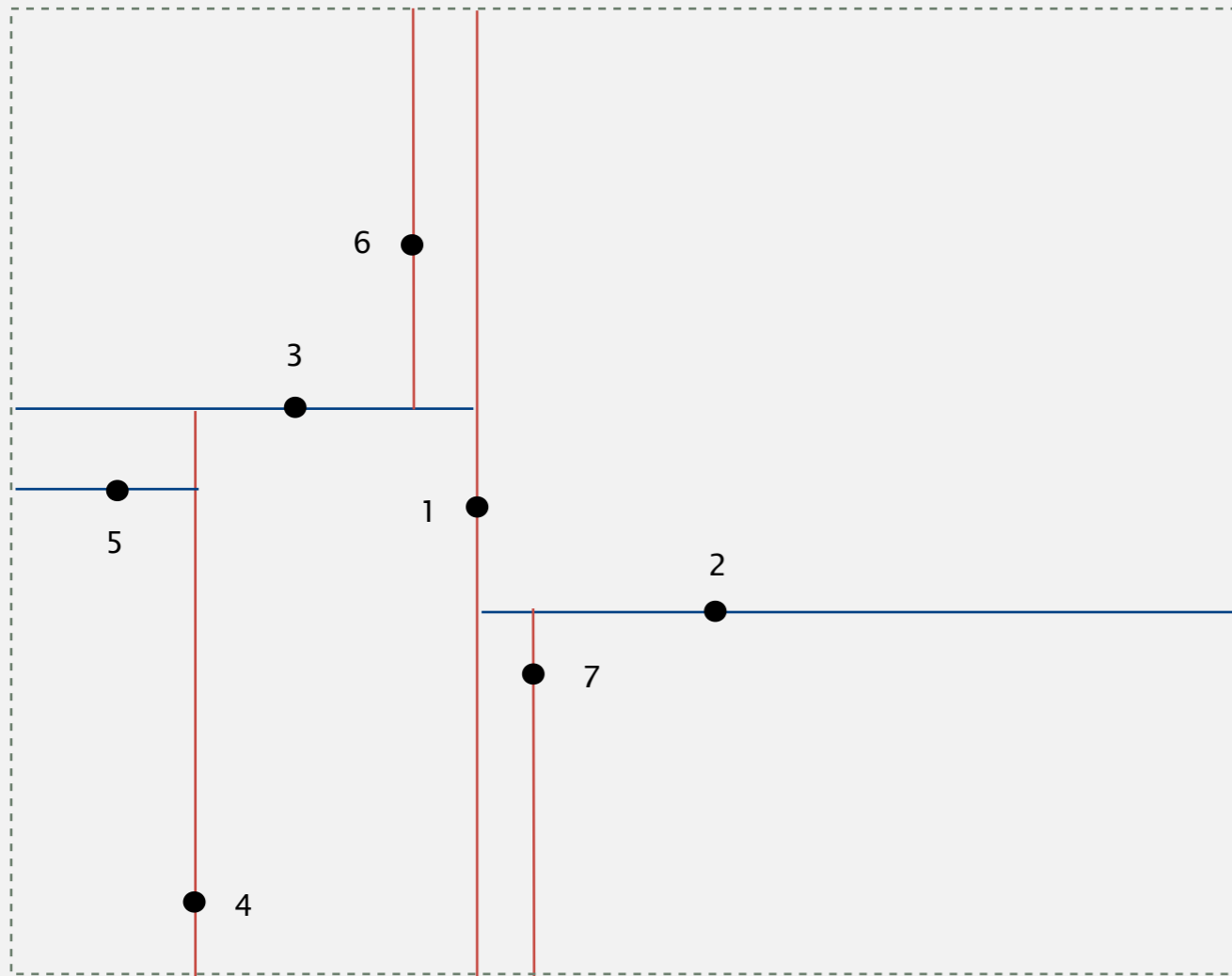
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Recursively partition plane into two halfplanes.



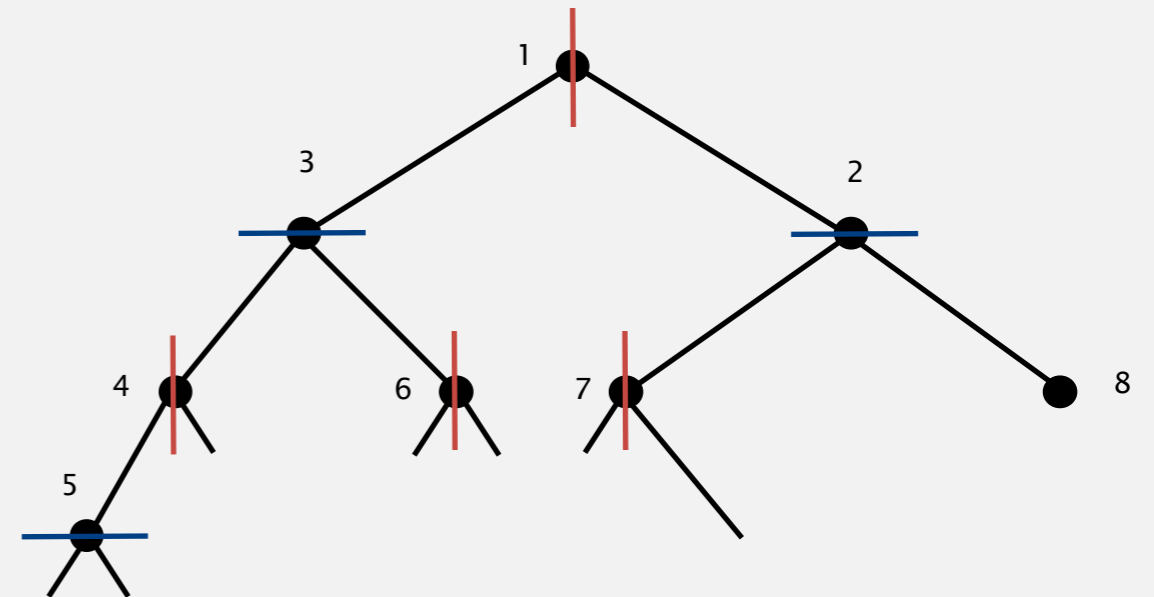
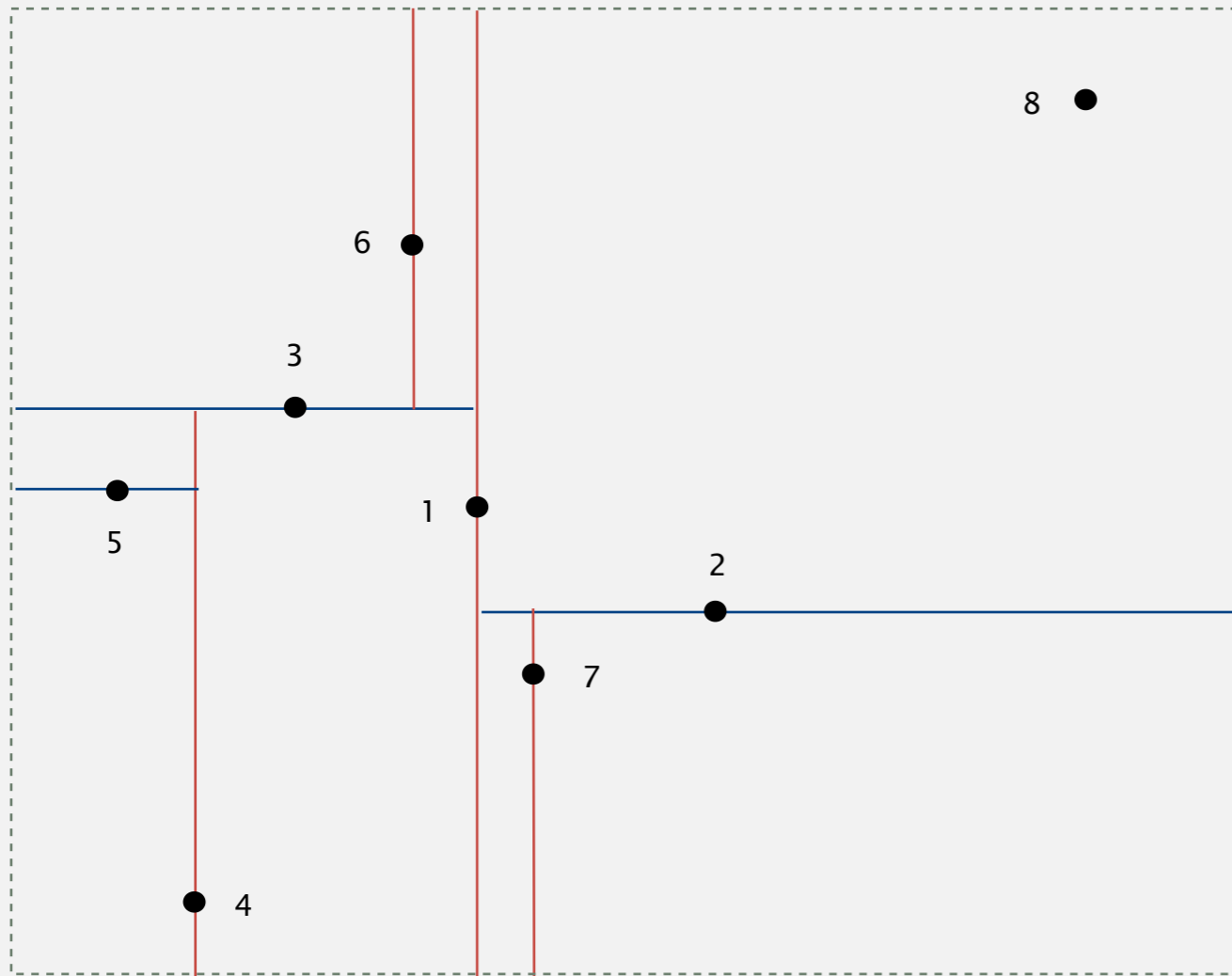
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Recursively partition plane into two halfplanes.



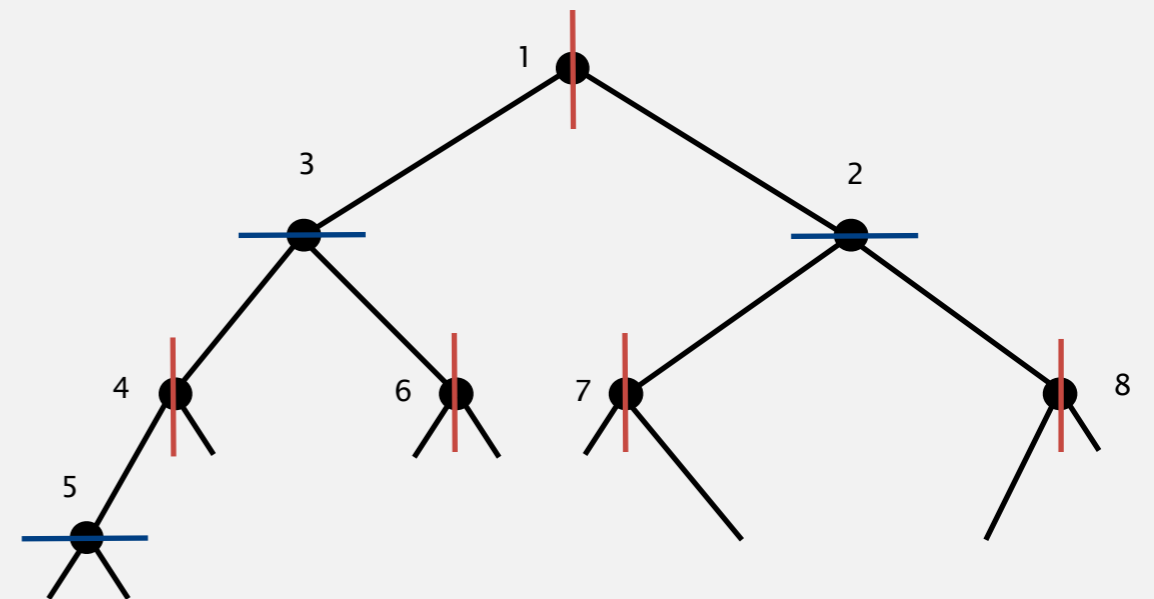
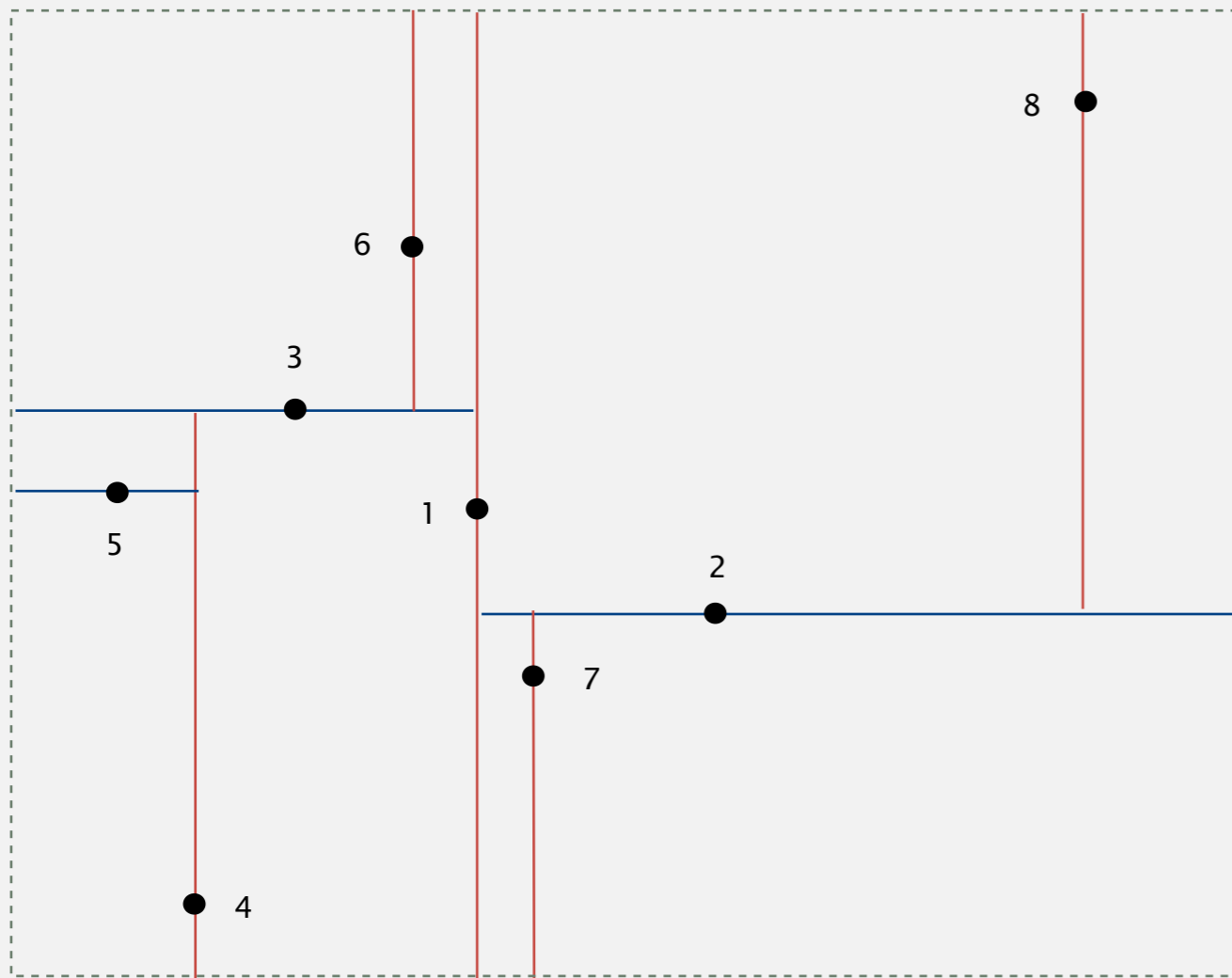
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Recursively partition plane into two halfplanes.



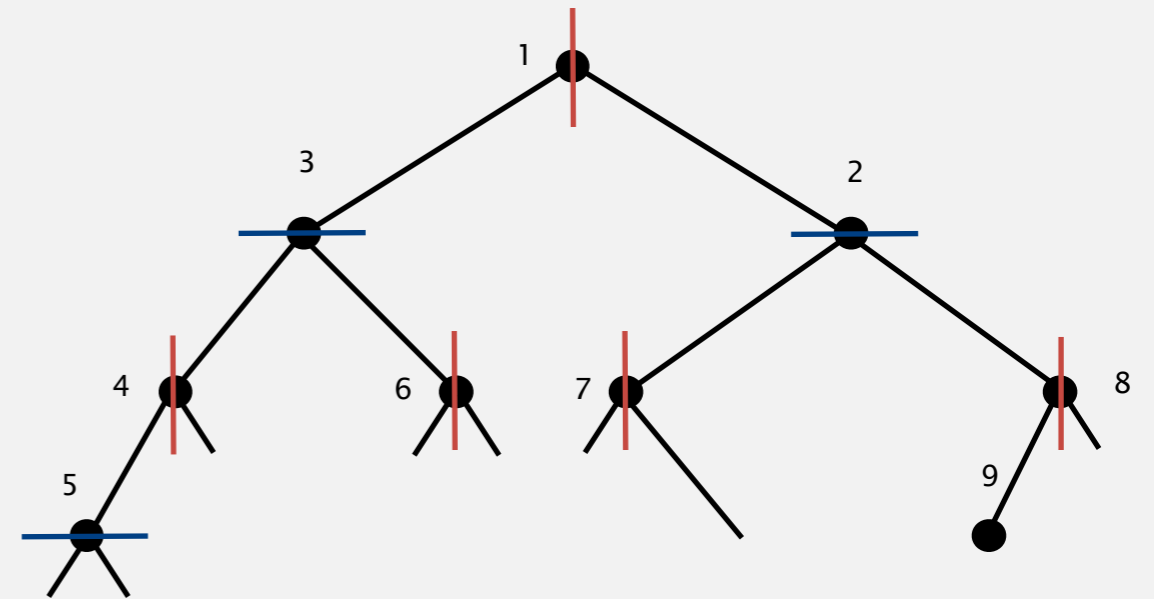
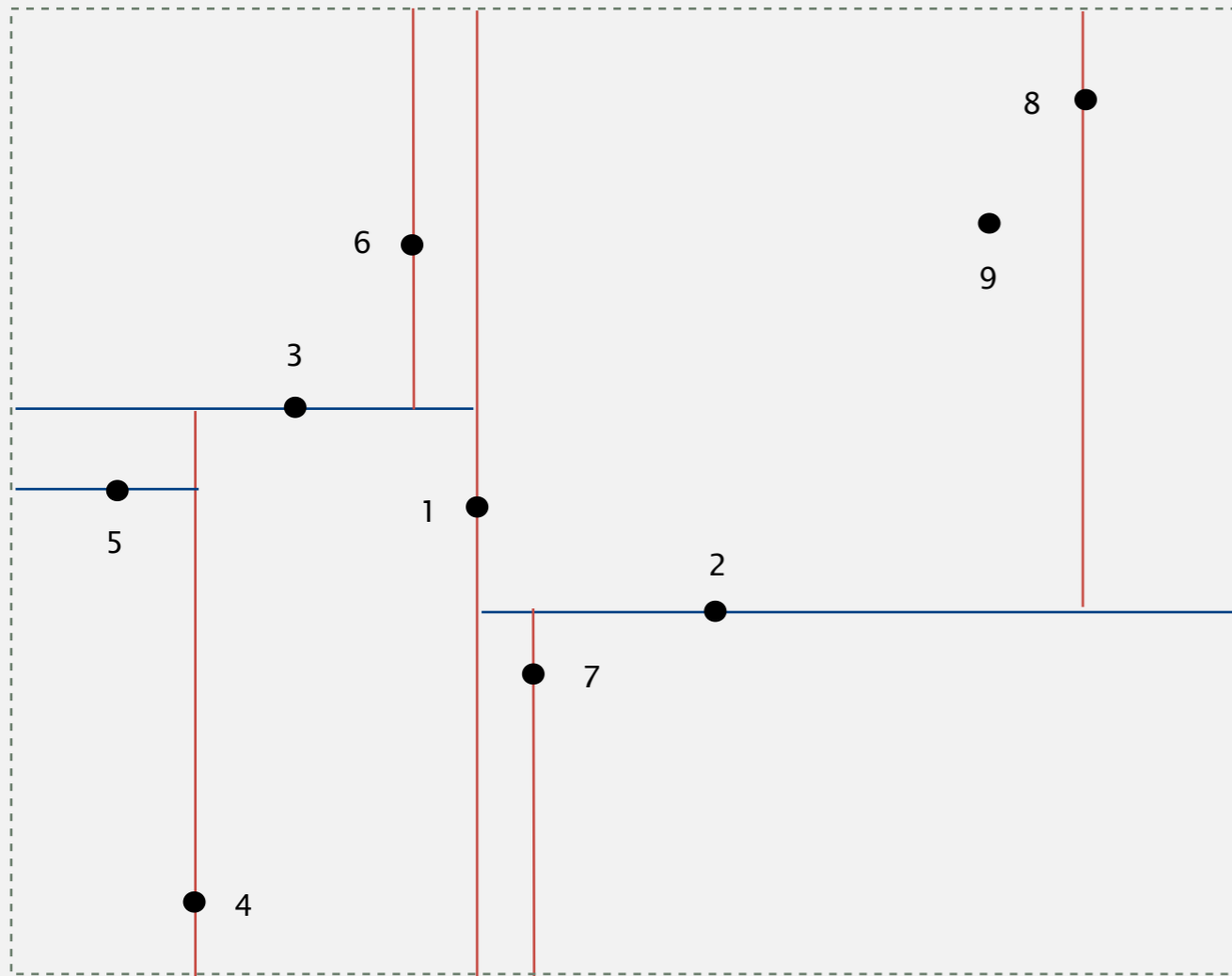
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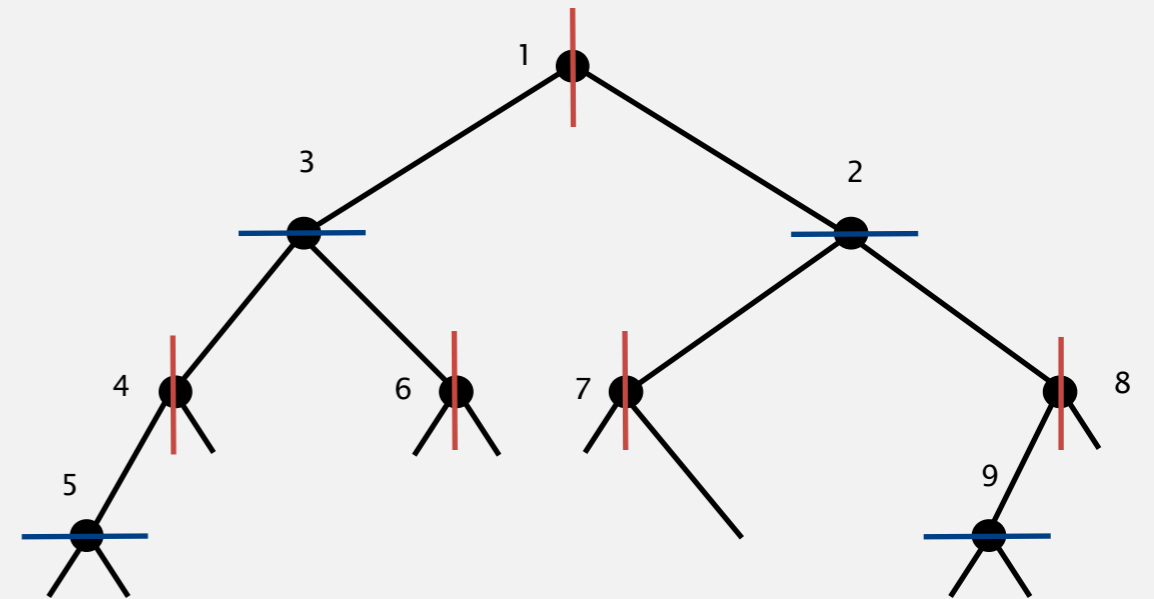
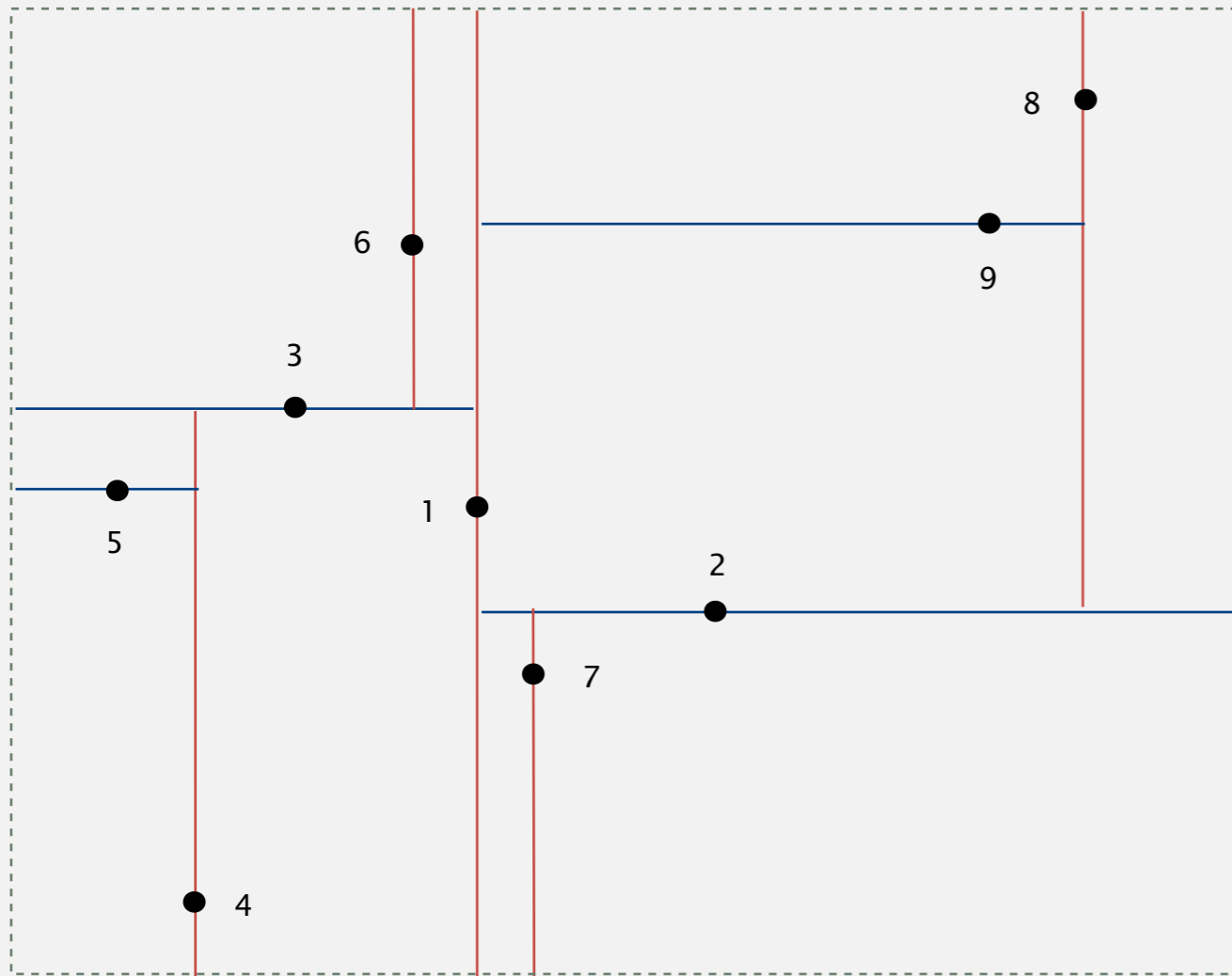
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Recursively partition plane into two halfplanes.



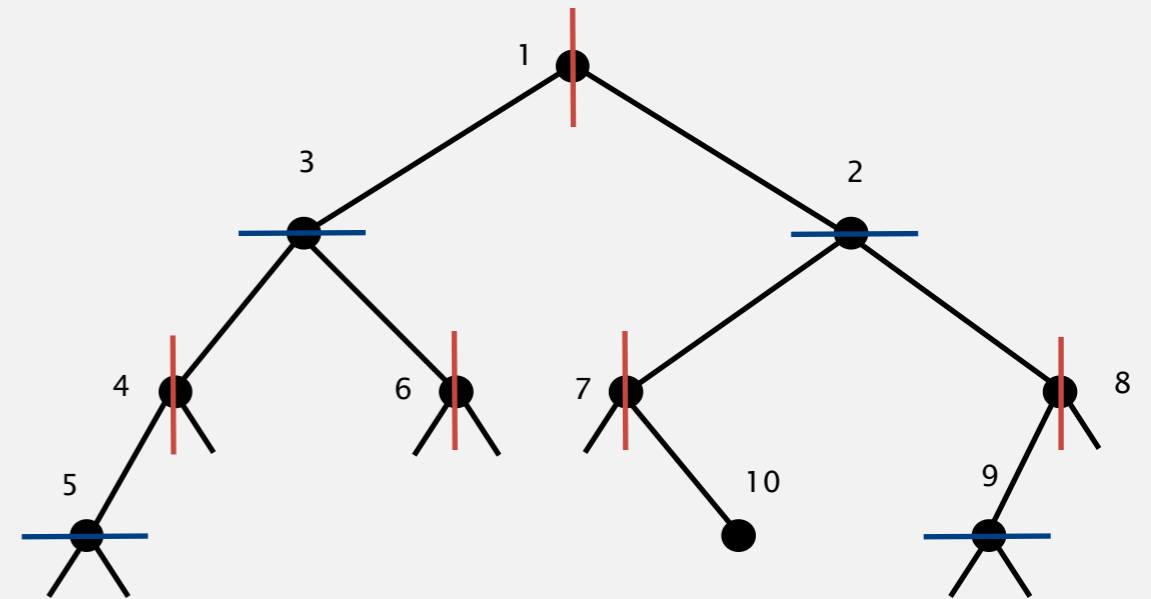
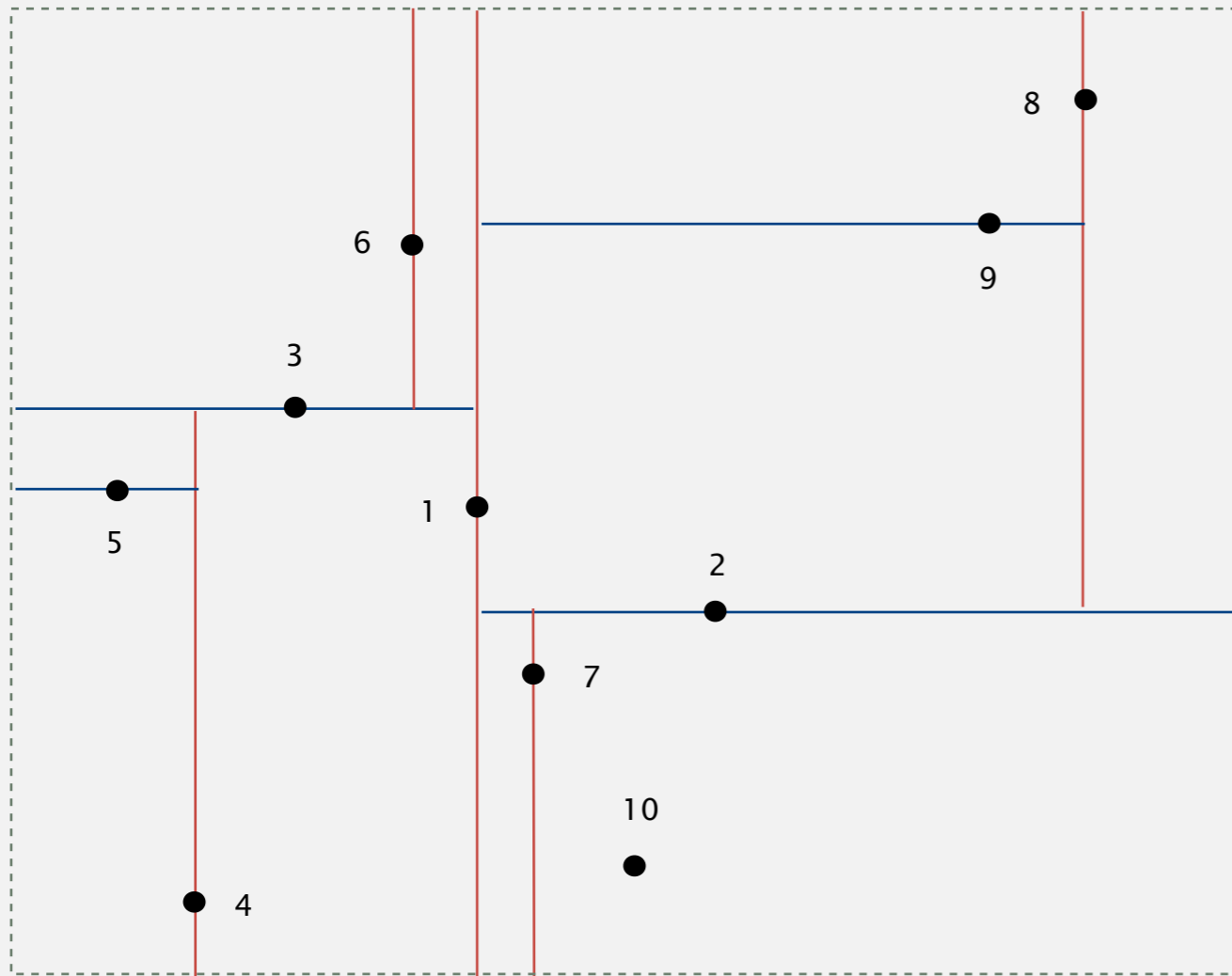
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Recursively partition plane into two halfplanes.



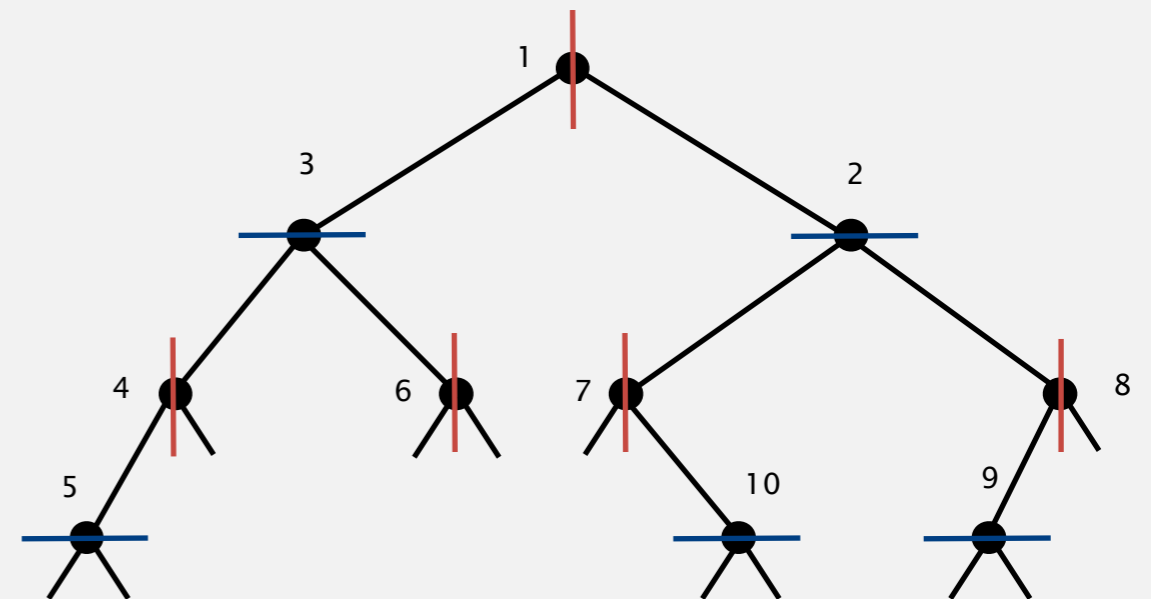
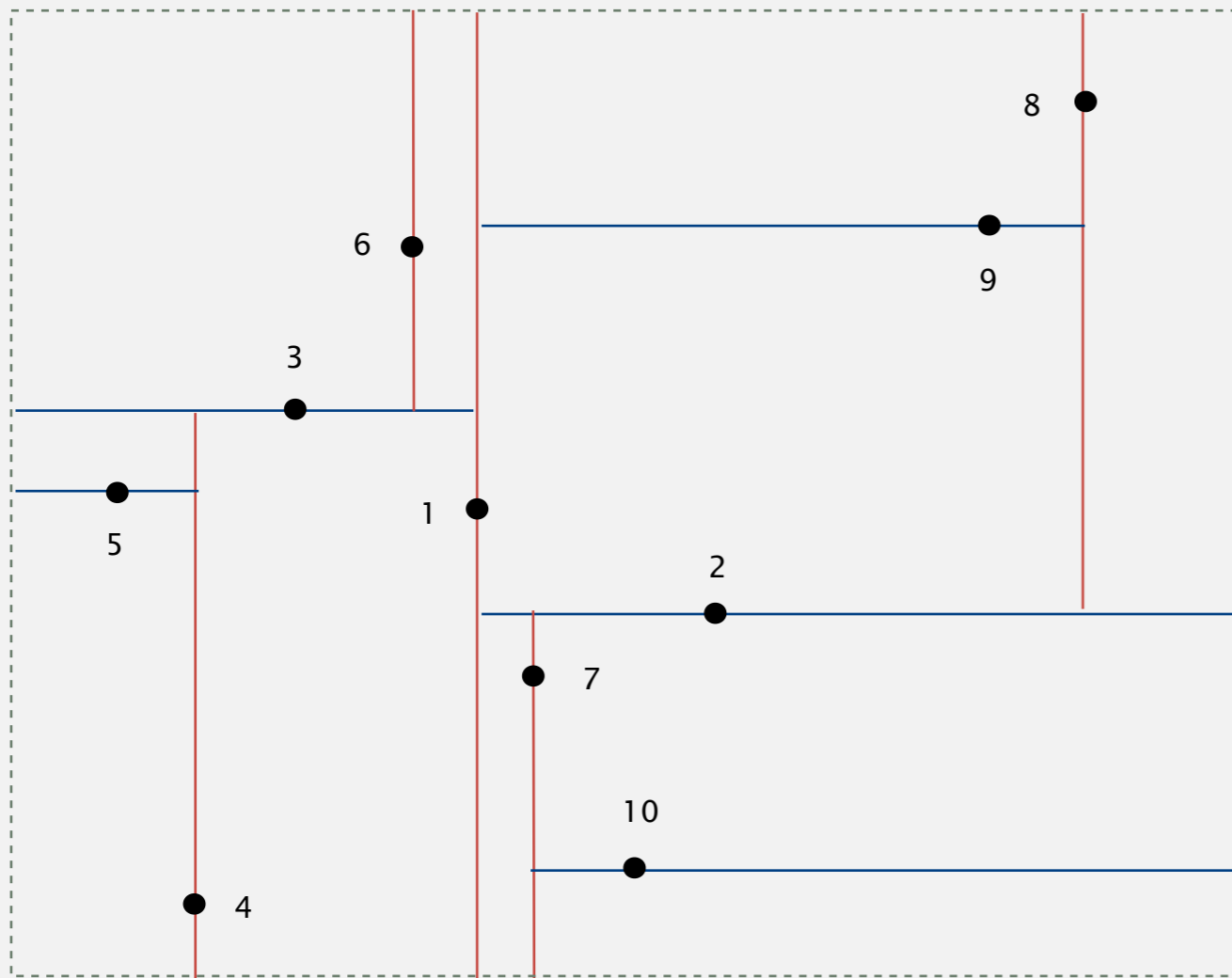
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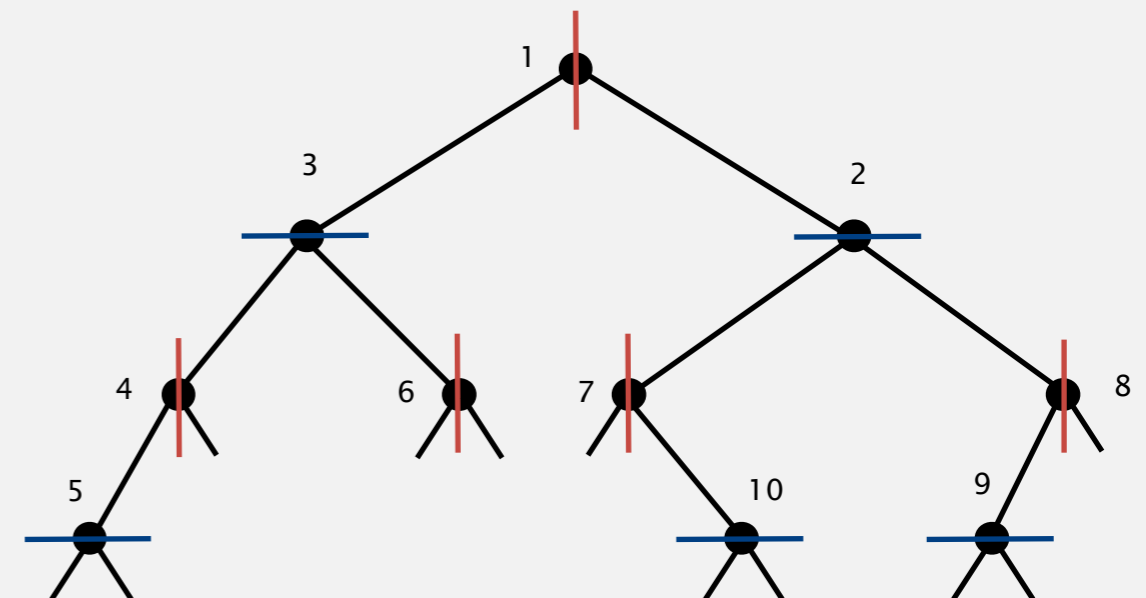
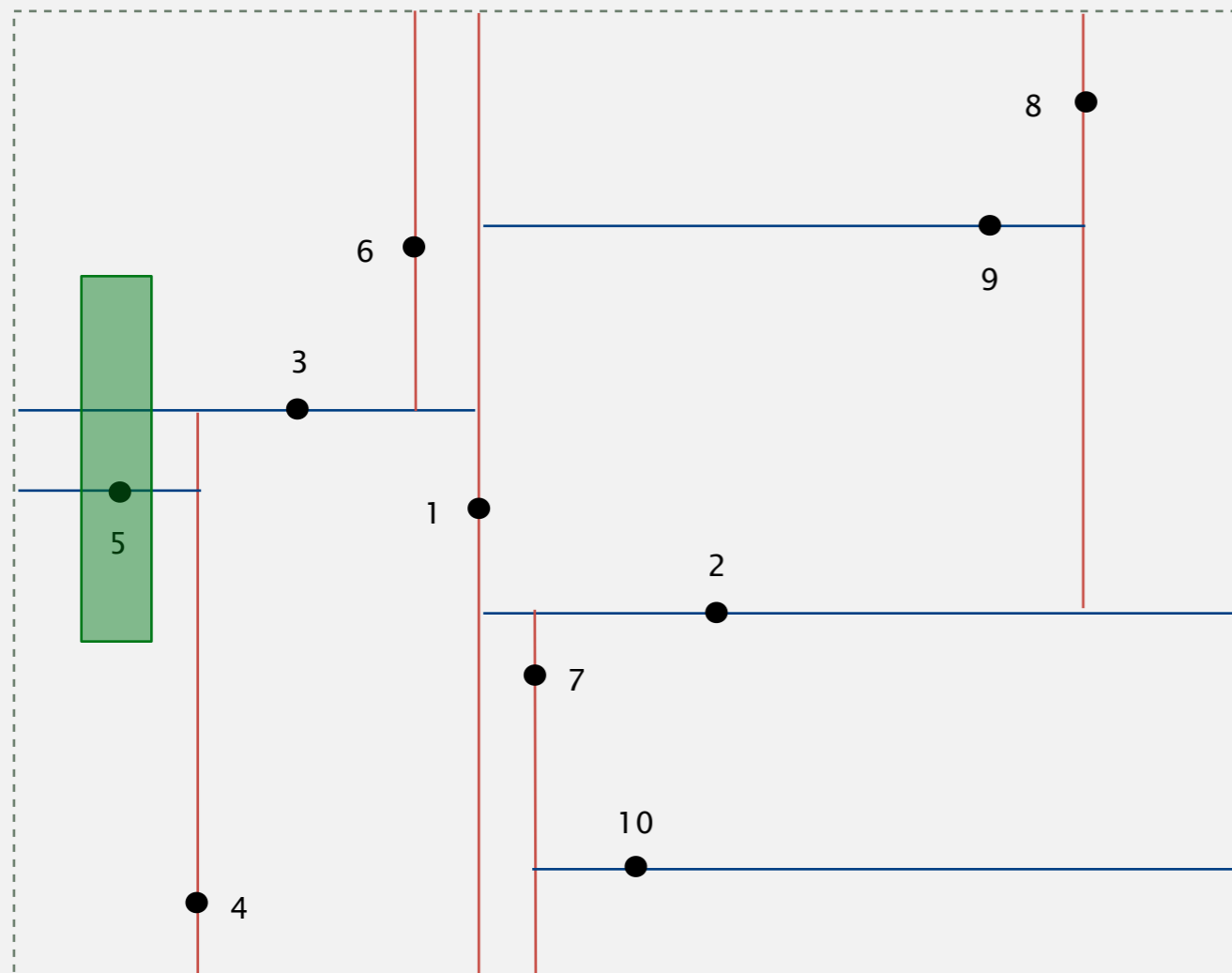




- ▶ insertion
- ▶ **range search**
- ▶ nearest neighbor search

## Range search in a 2d tree

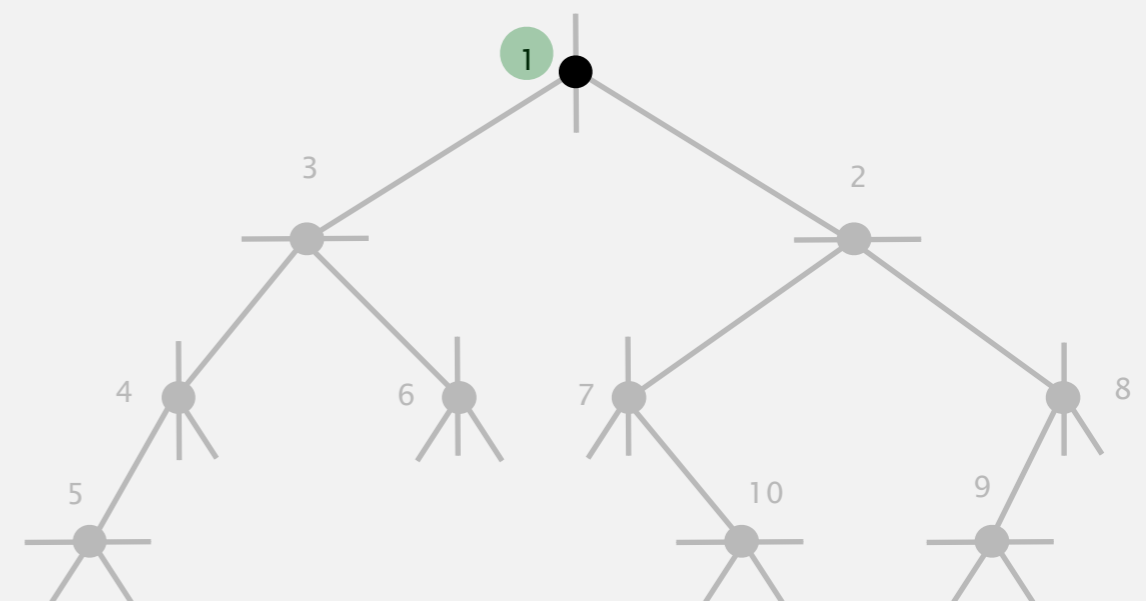
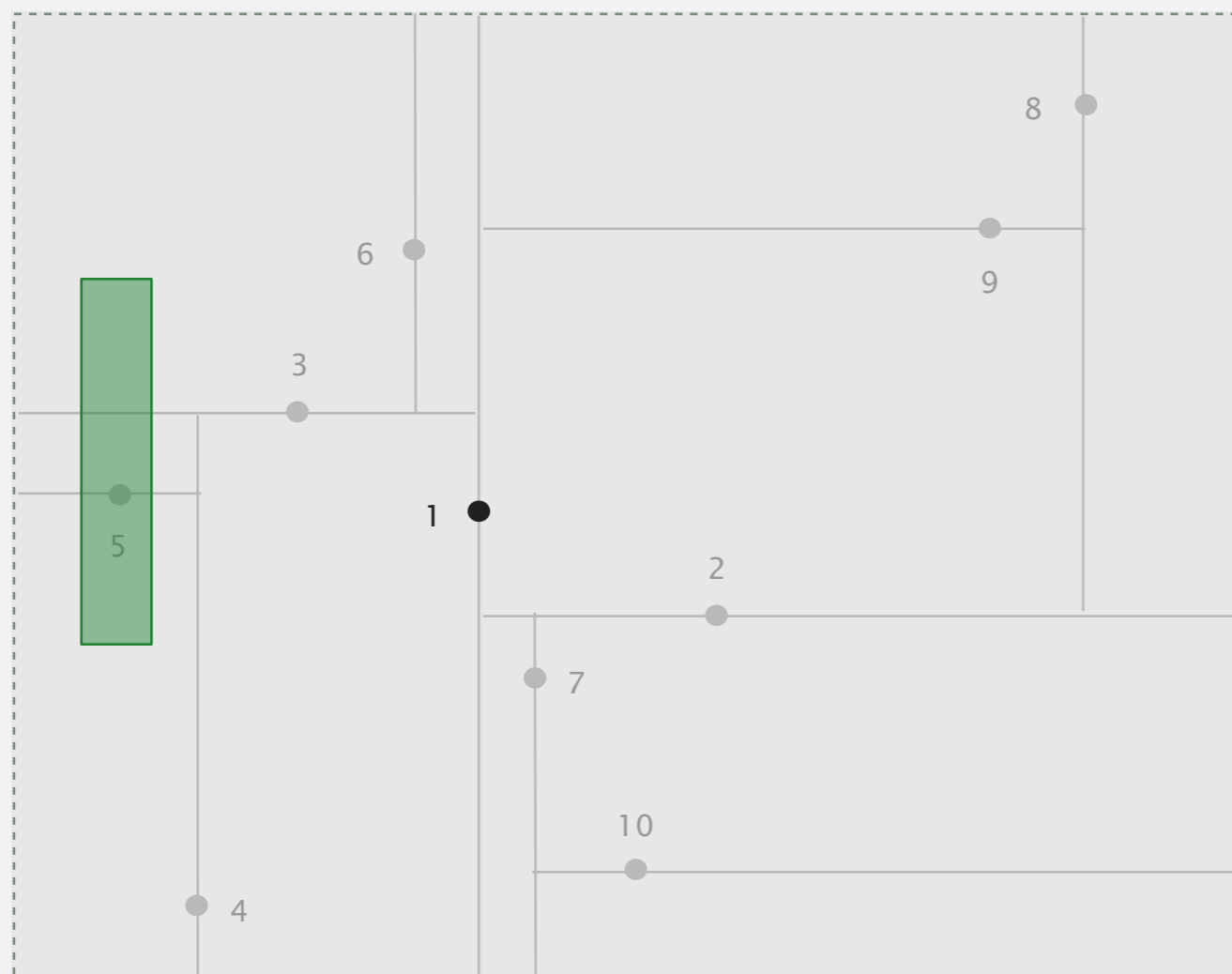
- Check if point in node lies in given rectangle.
- Recursively search left/bottom subdivision (if any could fall in rectangle).
- Recursively search right/top subdivision (if any could fall in rectangle).



find all points in 2d tree that are contained in green query rectangle

## Range search in a 2d tree

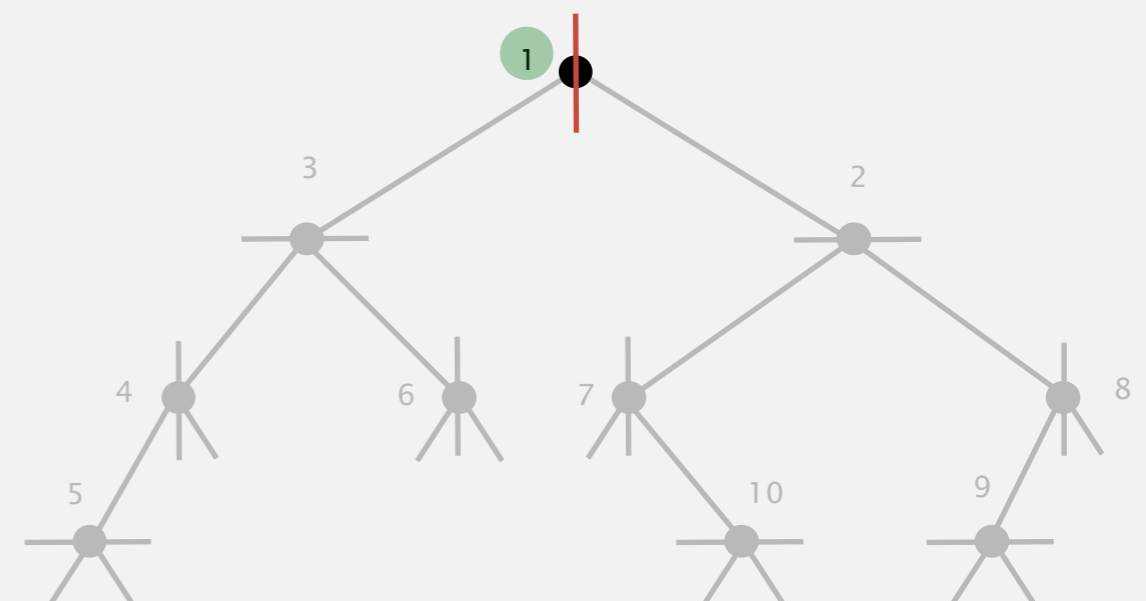
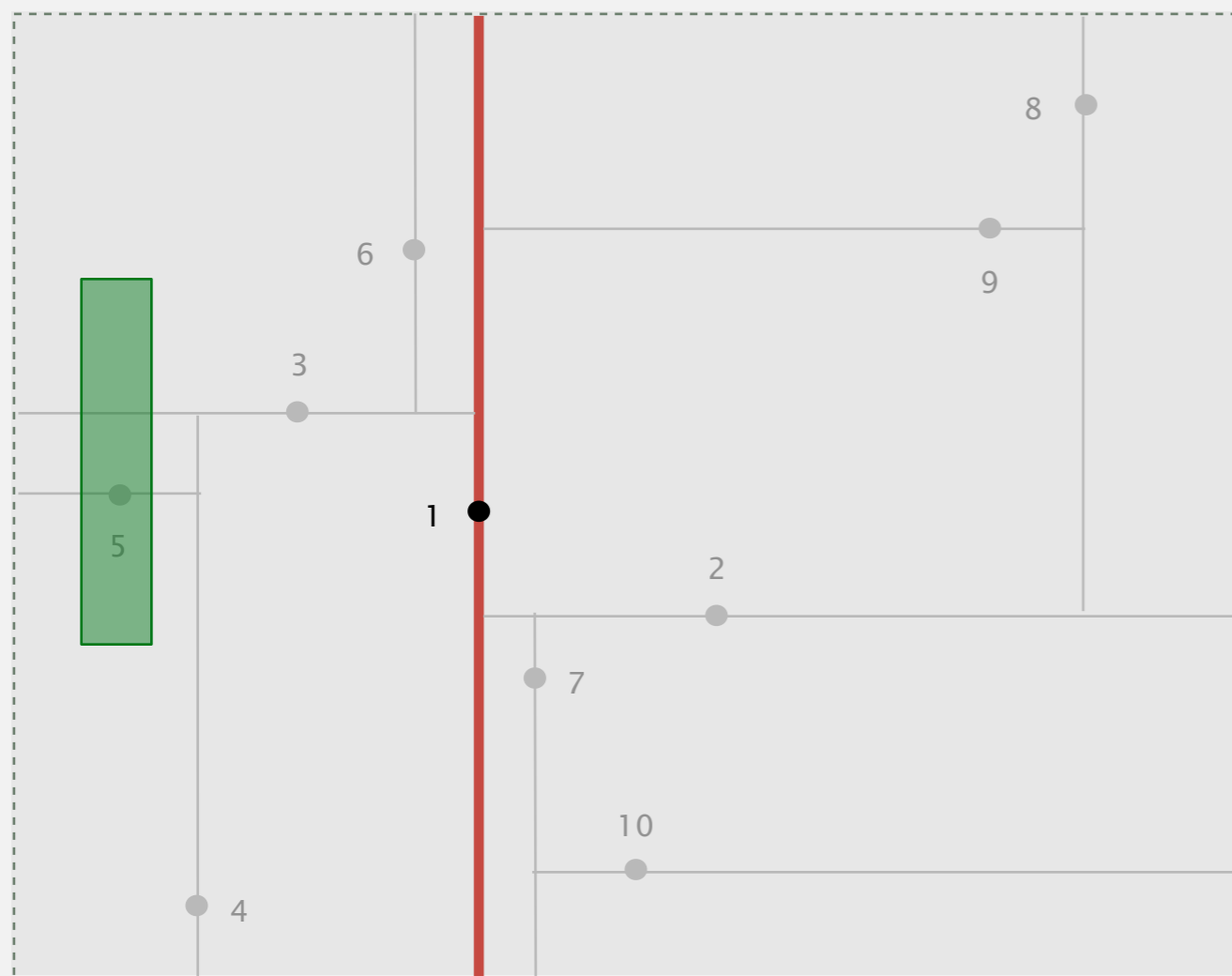
- Check if point in node lies in given rectangle.
- Recursively search left/bottom subdivision (if any could fall in rectangle).
- Recursively search right/top subdivision (if any could fall in rectangle).



**search root node**  
**check if query rectangle contains point 1**

## Range search in a 2d tree

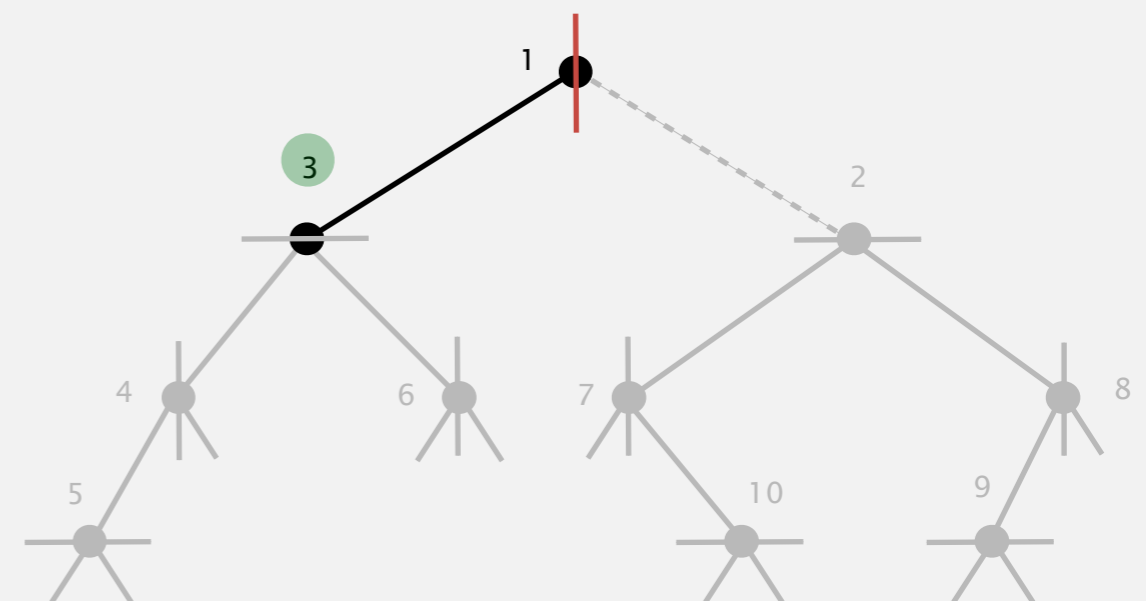
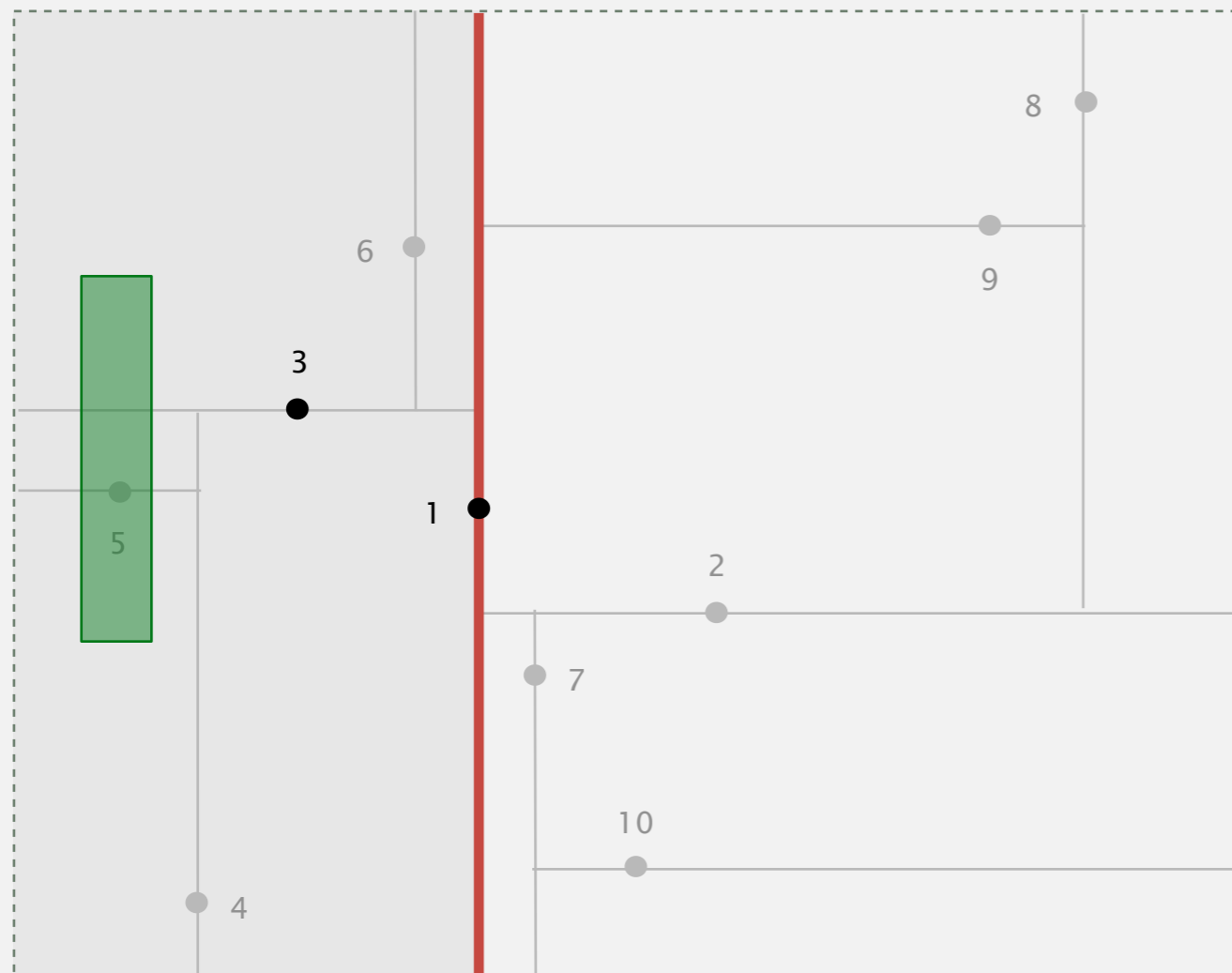
- Check if point in node lies in given rectangle.
- Recursively search left/bottom subdivision (if any could fall in rectangle).
- Recursively search right/top subdivision (if any could fall in rectangle).



**query rectangle to left of splitting line  
search only in left subtree**

## Range search in a 2d tree

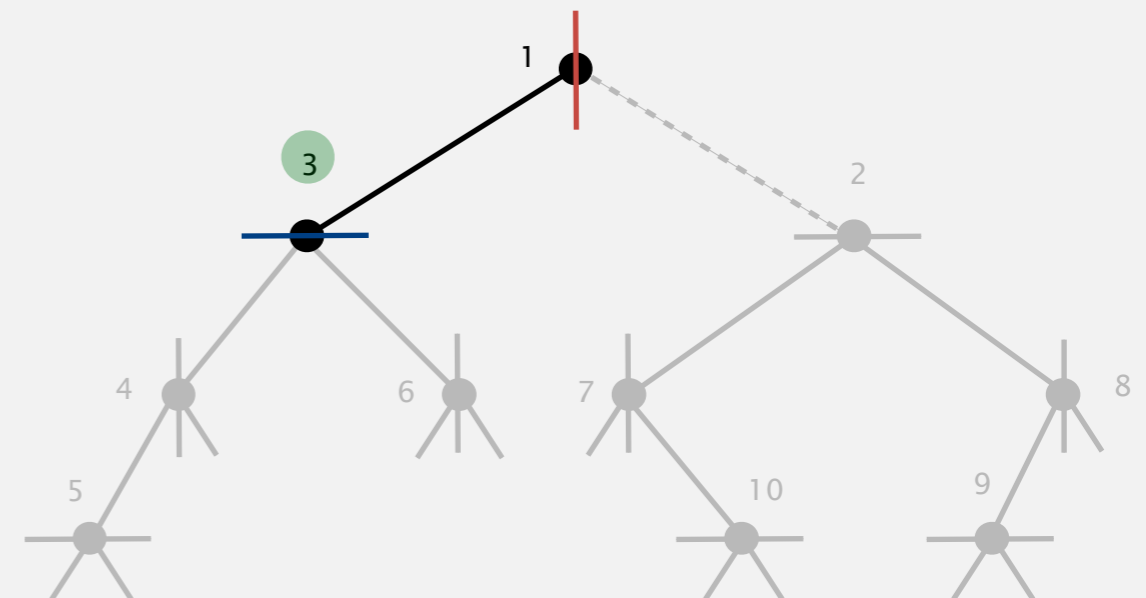
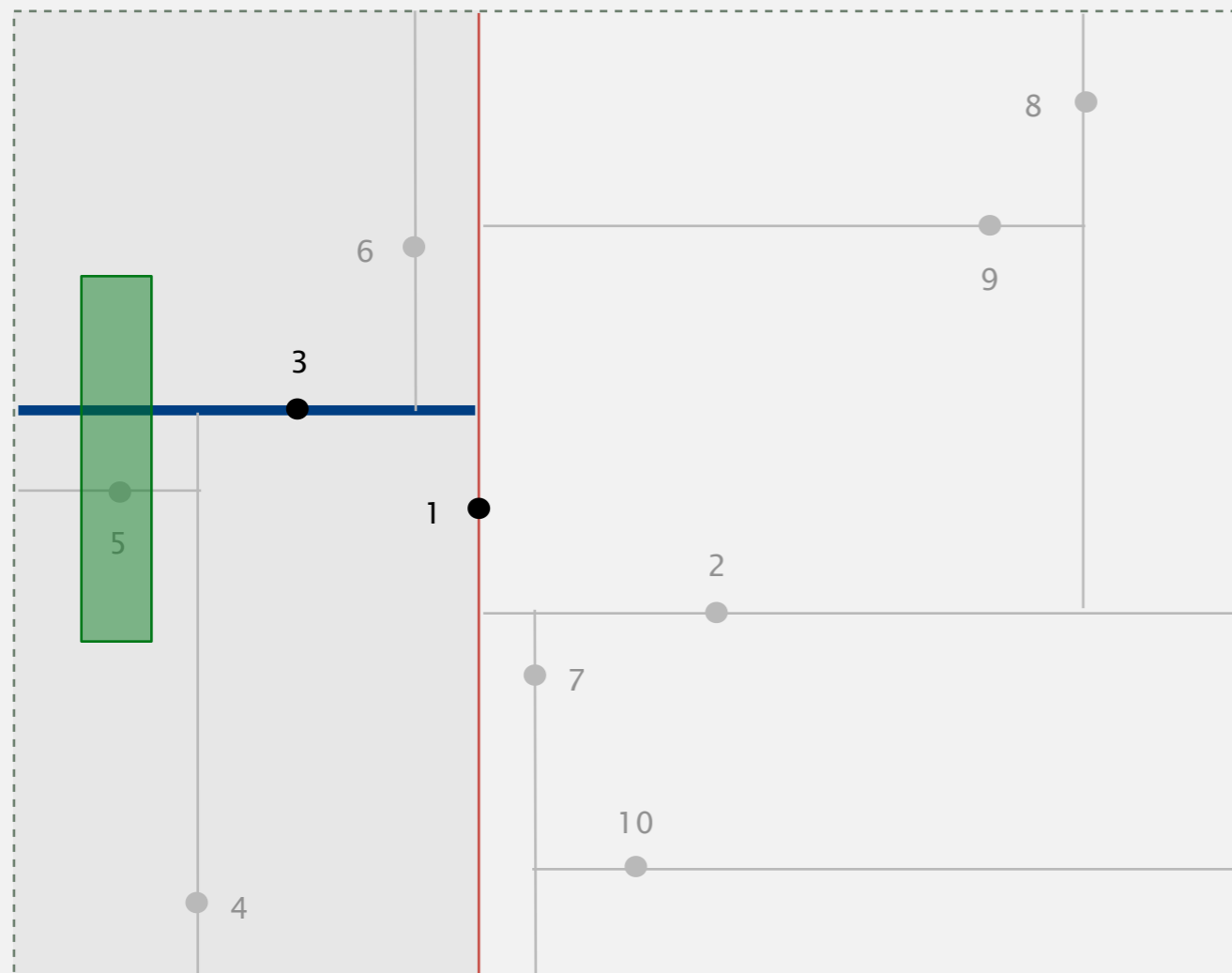
- Check if point in node lies in given rectangle.
- Recursively search left/bottom subdivision (if any could fall in rectangle).
- Recursively search right/top subdivision (if any could fall in rectangle).



**search left subtree**  
**check if query rectangle contains point 3**

## Range search in a 2d tree

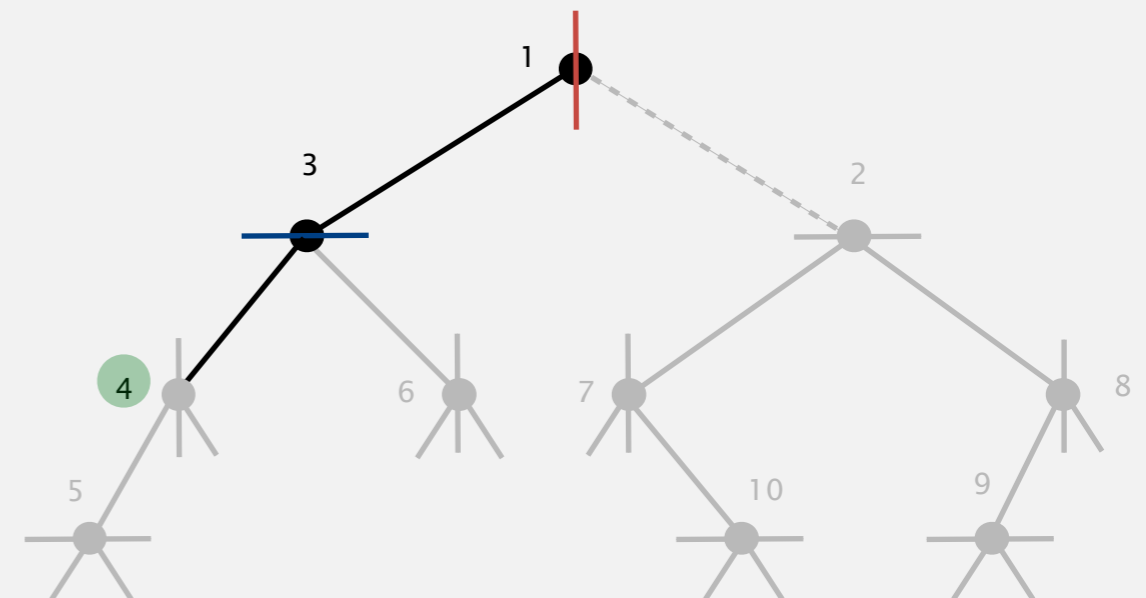
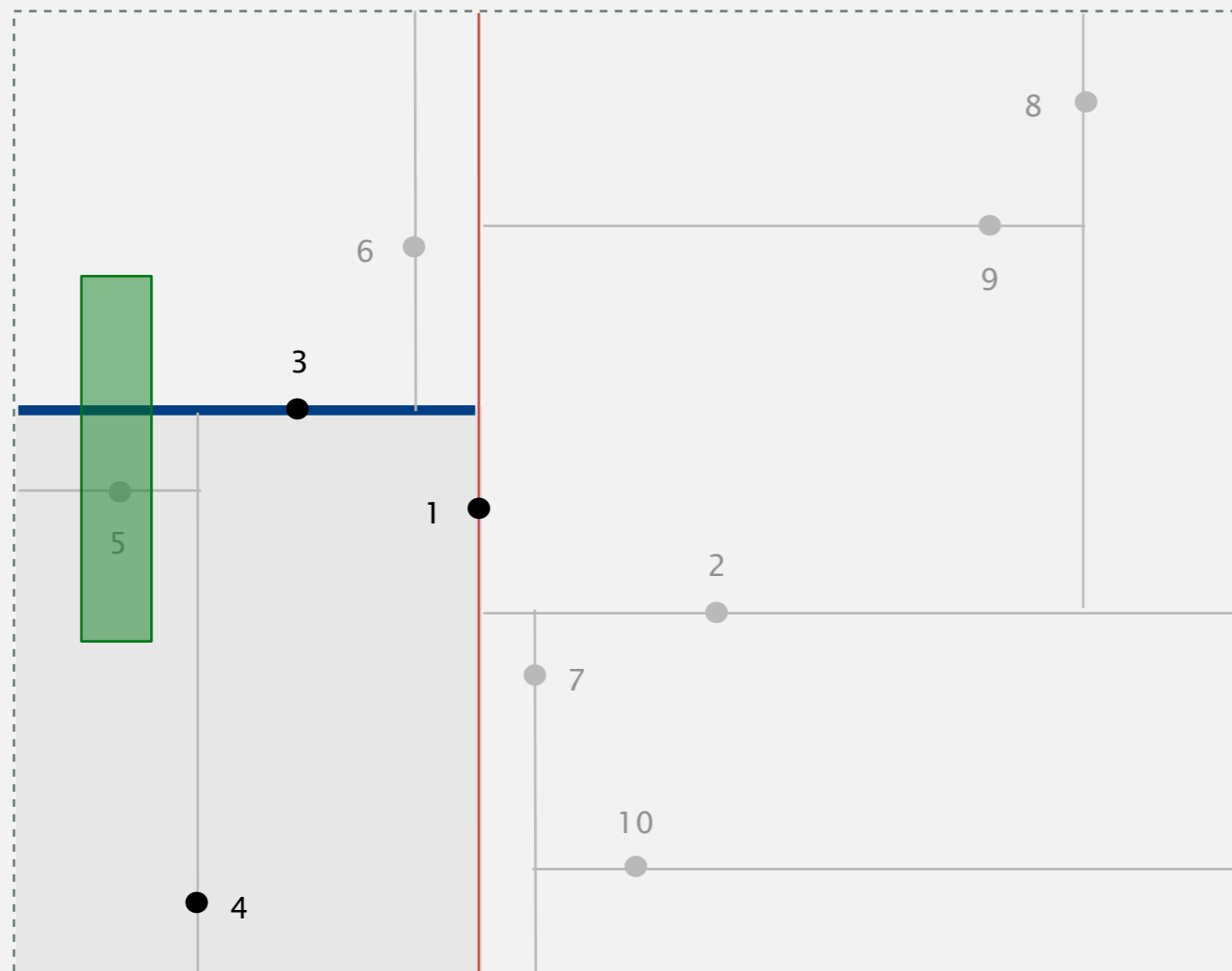
- Check if point in node lies in given rectangle.
- Recursively search left/bottom subdivision (if any could fall in rectangle).
- Recursively search right/top subdivision (if any could fall in rectangle).



**query rectangle intersects splitting line  
search bottom and top subtrees**

## Range search in a 2d tree

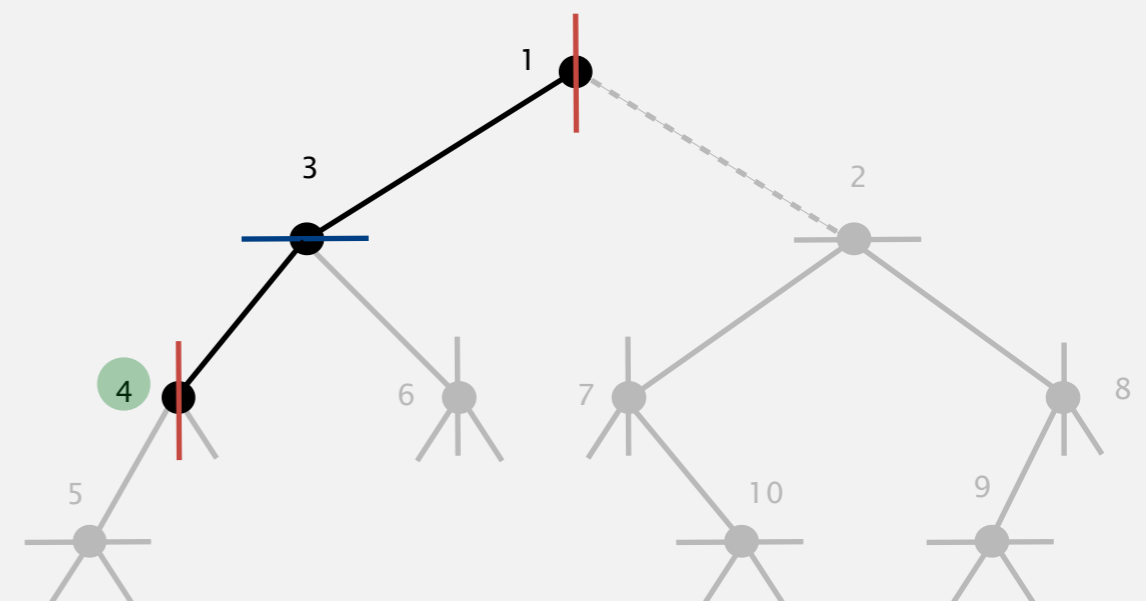
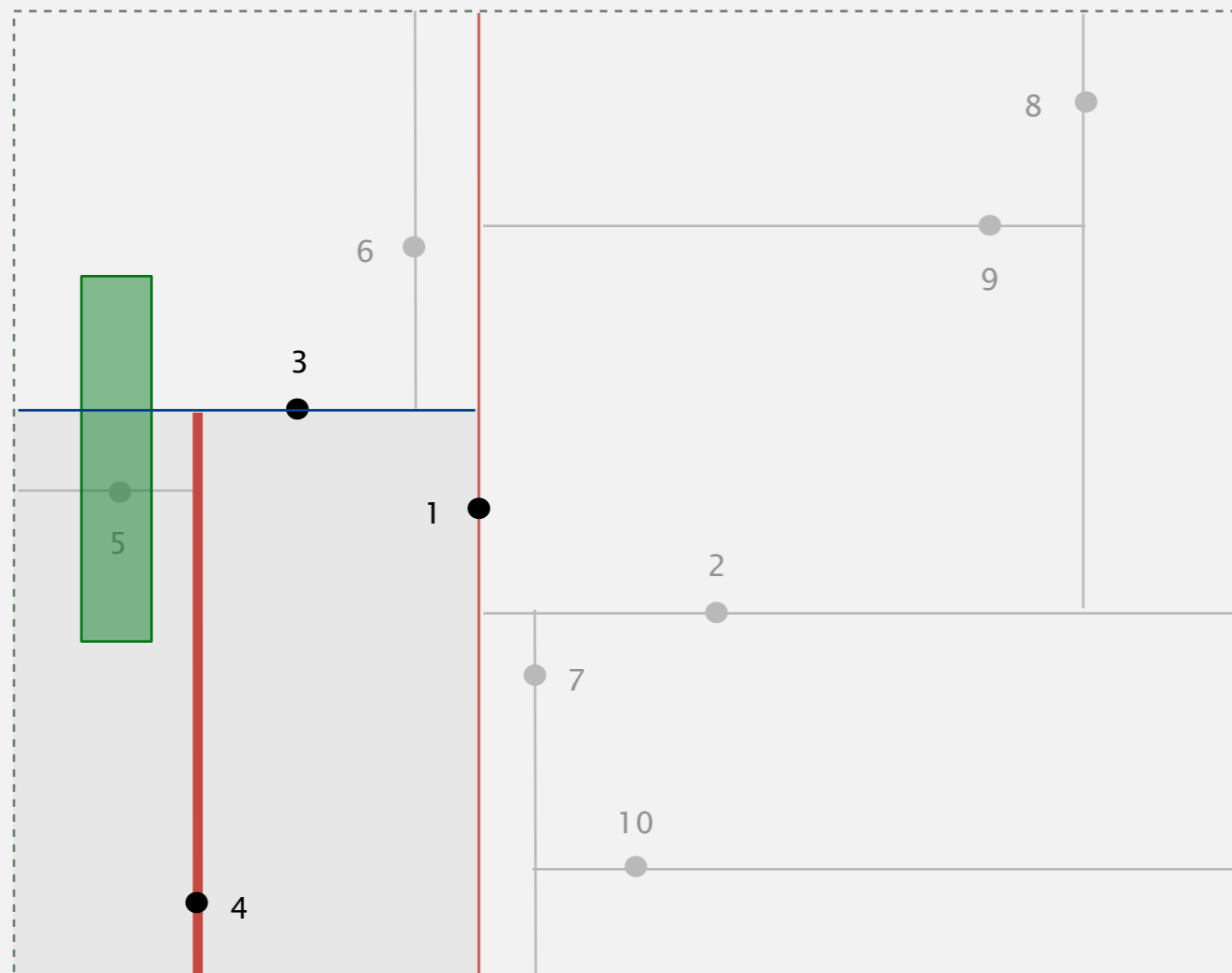
- Check if point in node lies in given rectangle.
- Recursively search left/bottom subdivision (if any could fall in rectangle).
- Recursively search right/top subdivision (if any could fall in rectangle).



**search left subtree**  
**check if query rectangle contains point 4**

## Range search in a 2d tree

- Check if point in node lies in given rectangle.
- Recursively search left/bottom subdivision (if any could fall in rectangle).
- Recursively search right/top subdivision (if any could fall in rectangle).

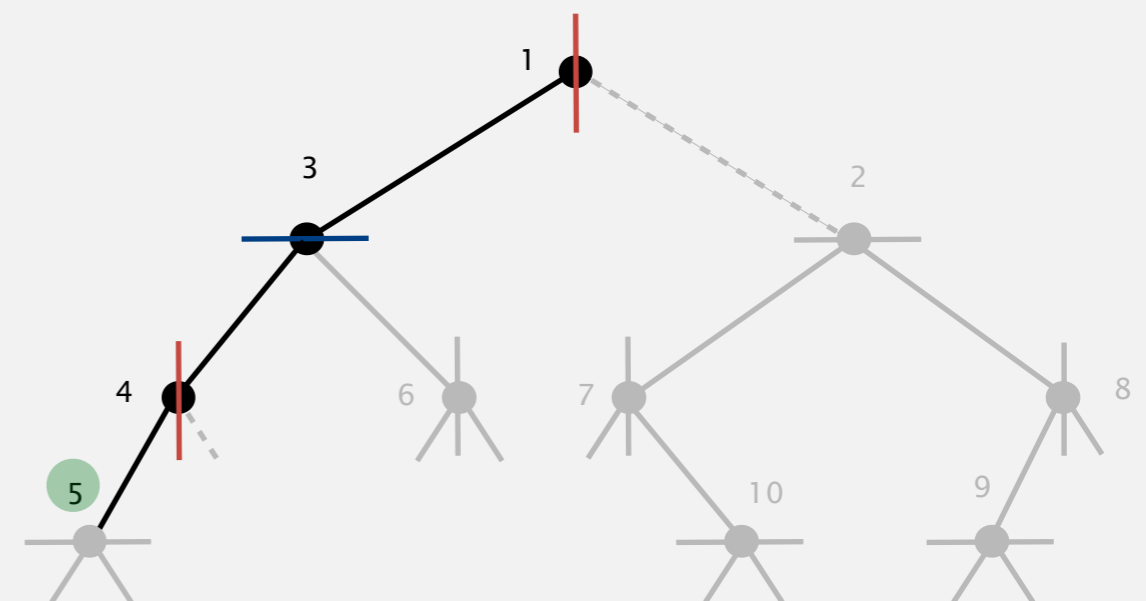
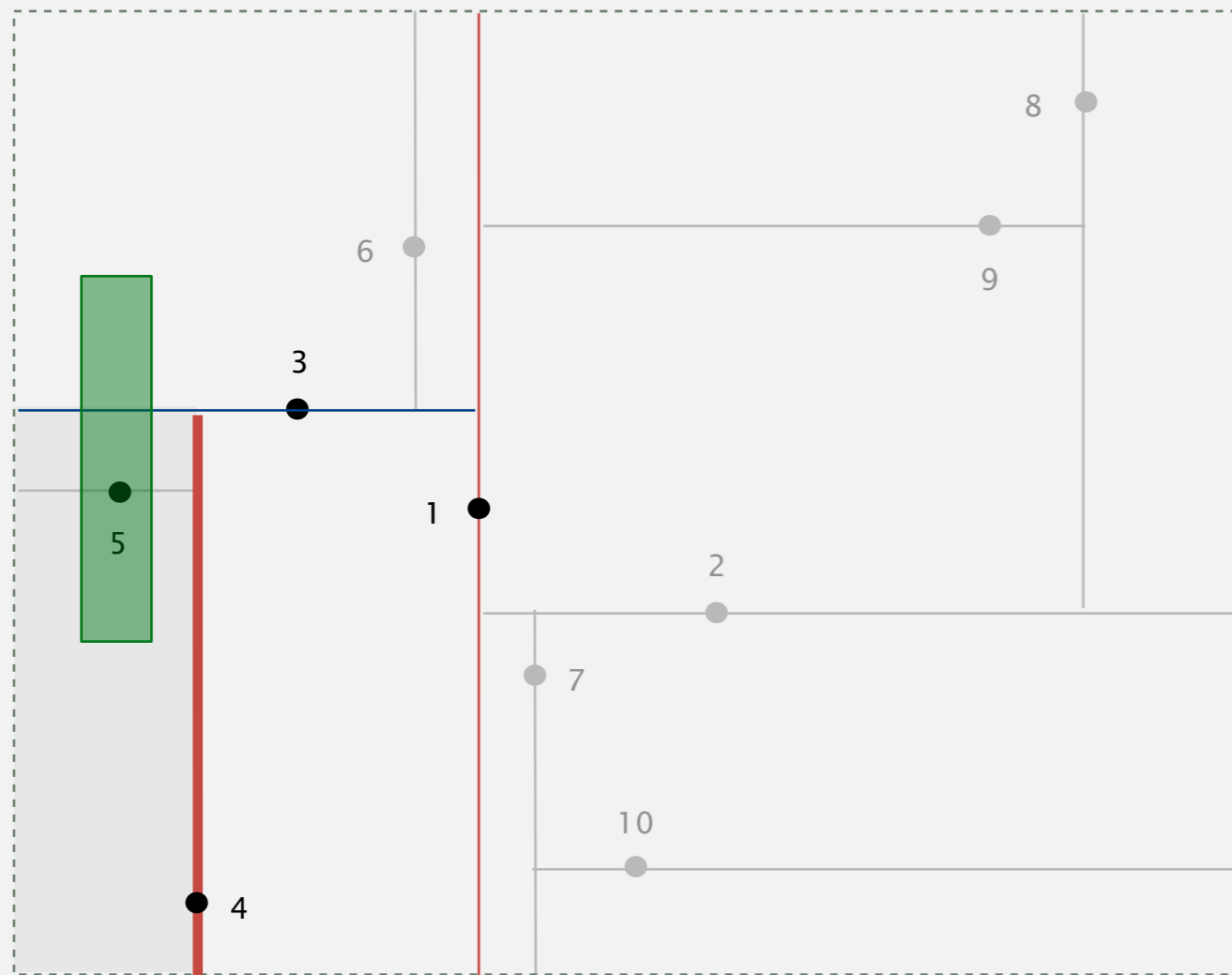


**query rectangle to left of splitting line  
search only in left subtree**



## Range search in a 2d tree

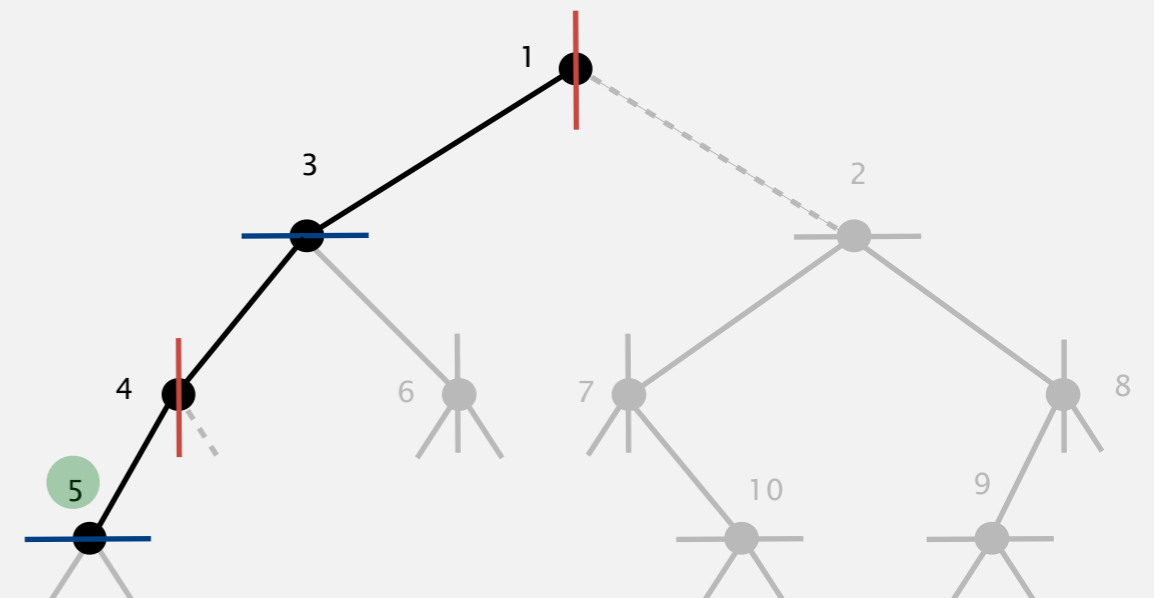
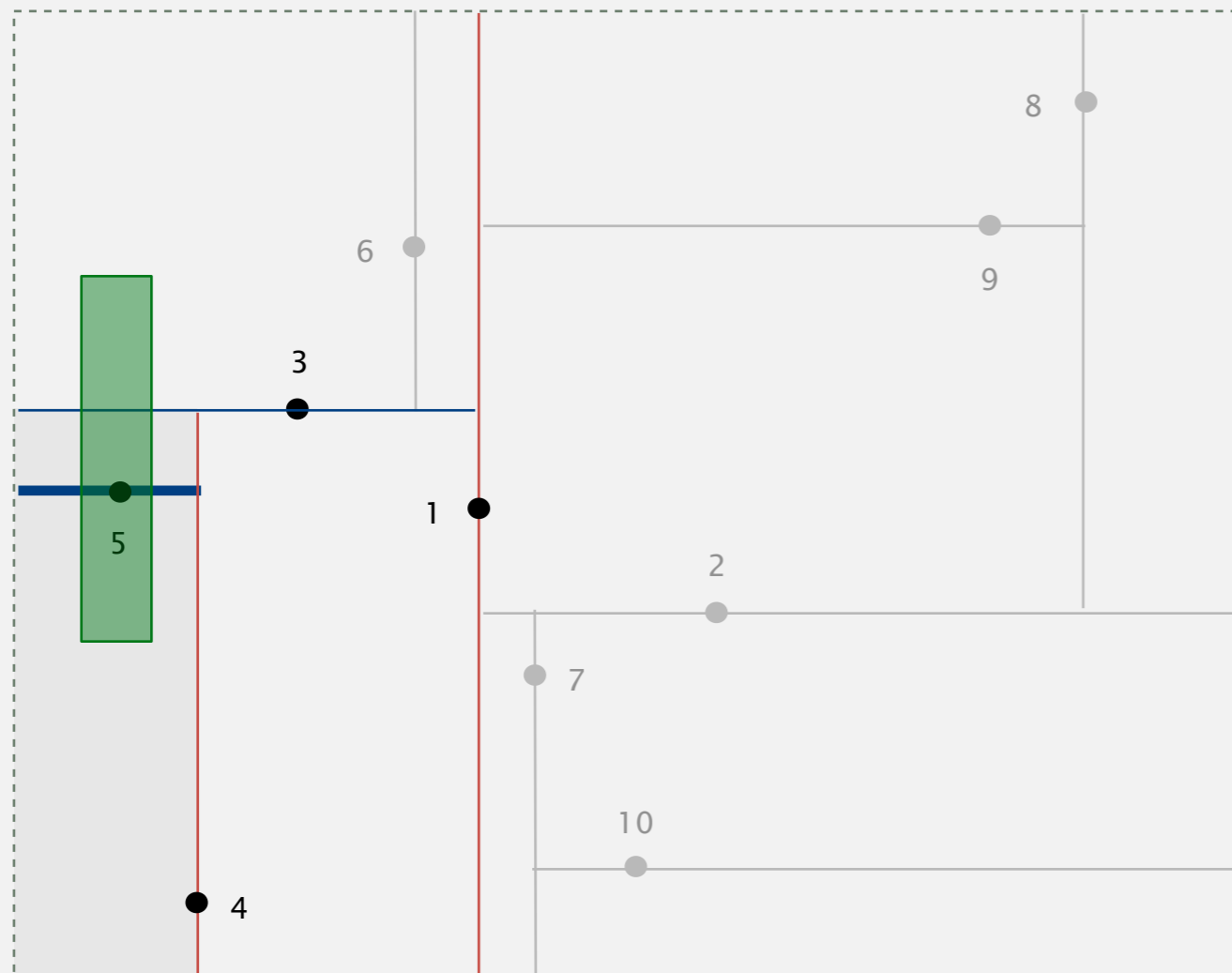
- Check if point in node lies in given rectangle.
- Recursively search left/bottom subdivision (if any could fall in rectangle).
- Recursively search right/top subdivision (if any could fall in rectangle).



**search left subtree**  
**check if query rectangle contains point 5**  
**(search hit)**

## Range search in a 2d tree

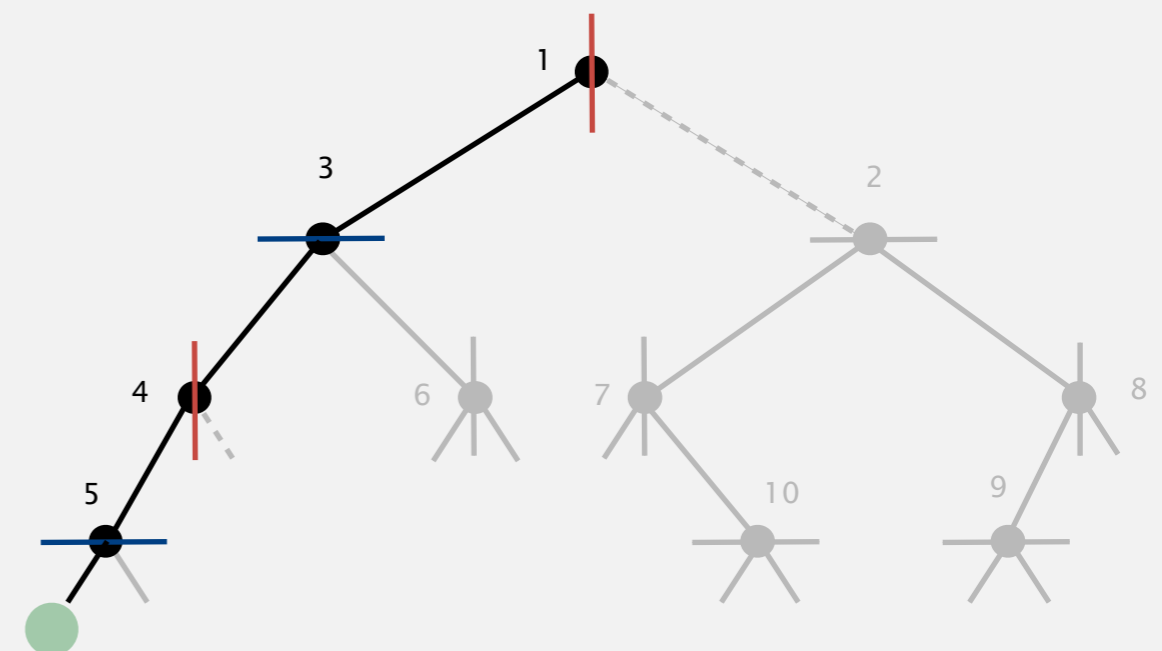
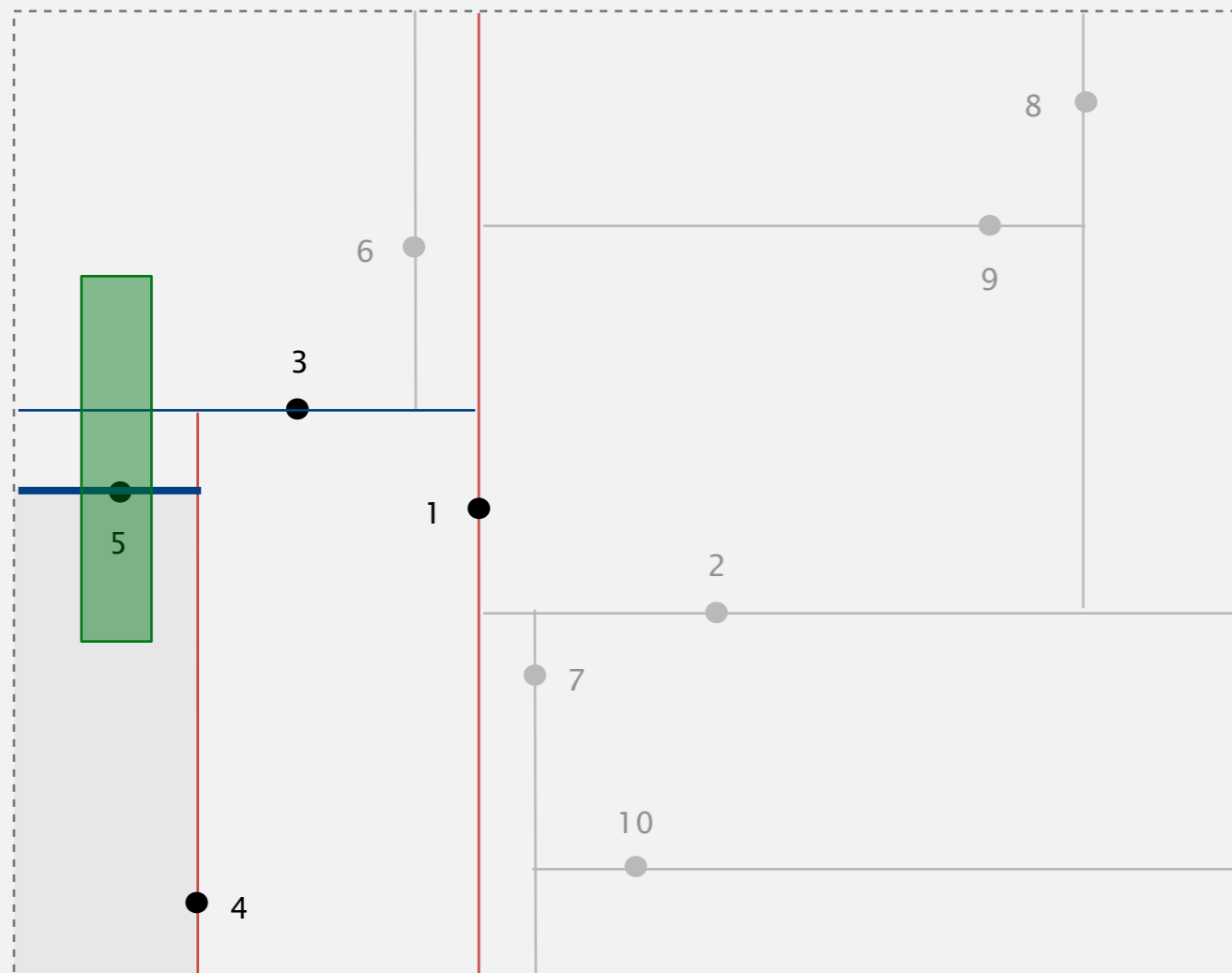
- Check if point in node lies in given rectangle.
- Recursively search left/bottom subdivision (if any could fall in rectangle).
- Recursively search right/top subdivision (if any could fall in rectangle).



**query rectangle intersects splitting line  
search bottom and top subtrees**

## Range search in a 2d tree

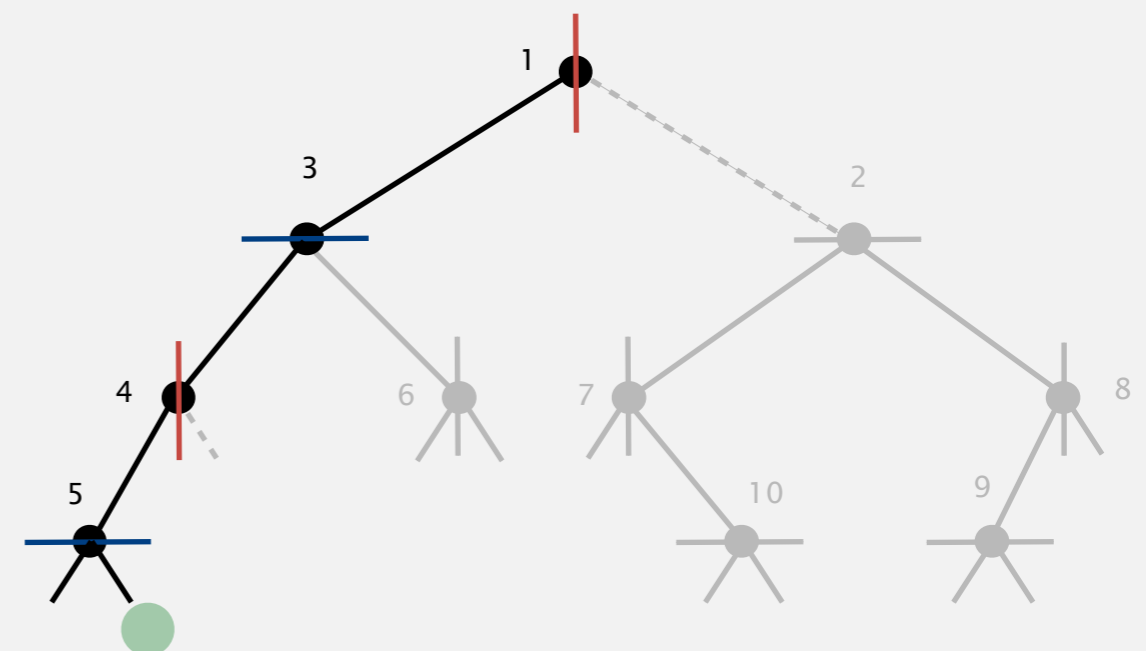
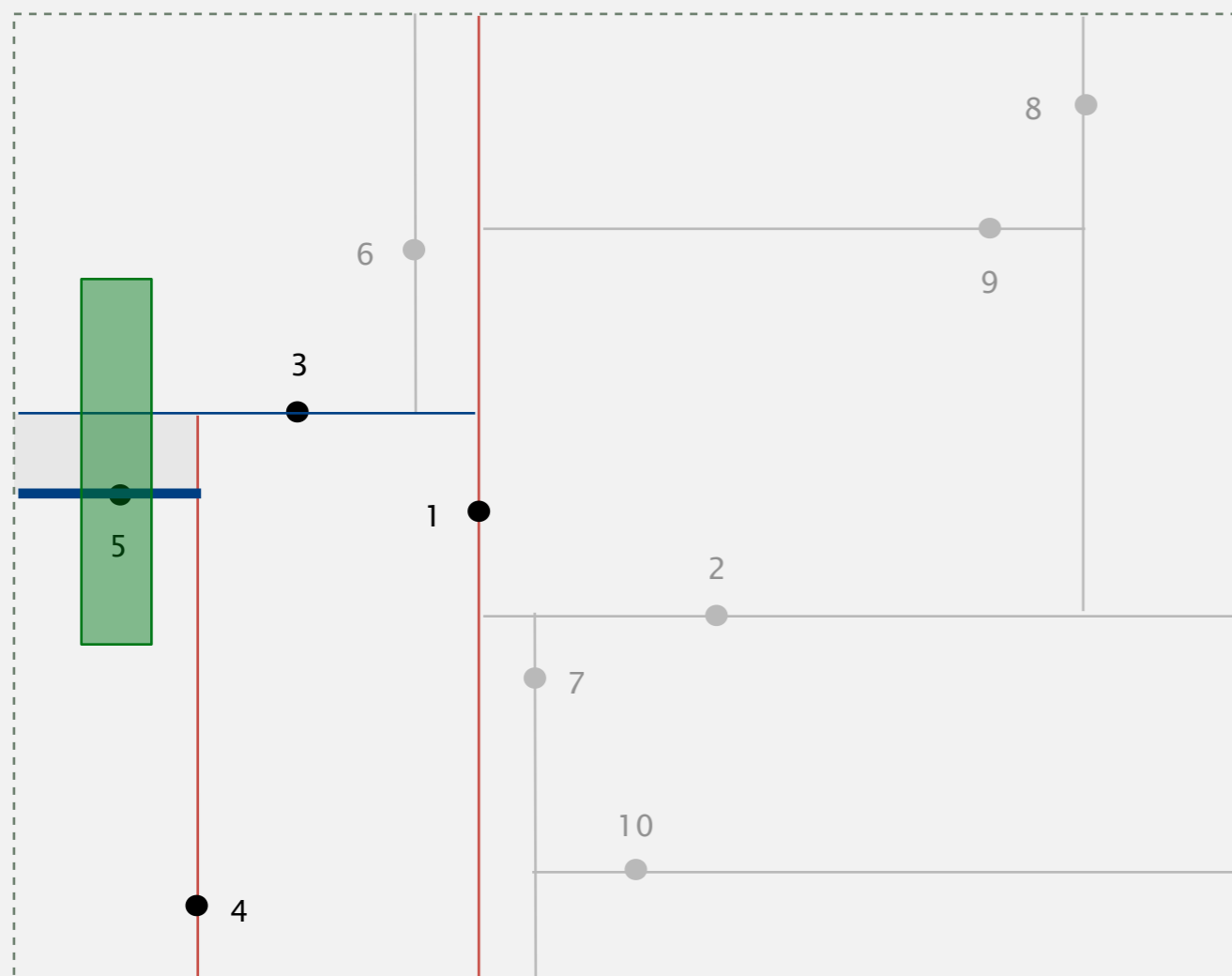
- Check if point in node lies in given rectangle.
- Recursively search left/bottom subdivision (if any could fall in rectangle).
- Recursively search right/top subdivision (if any could fall in rectangle).



**search bottom subtree  
stop since empty**

## Range search in a 2d tree

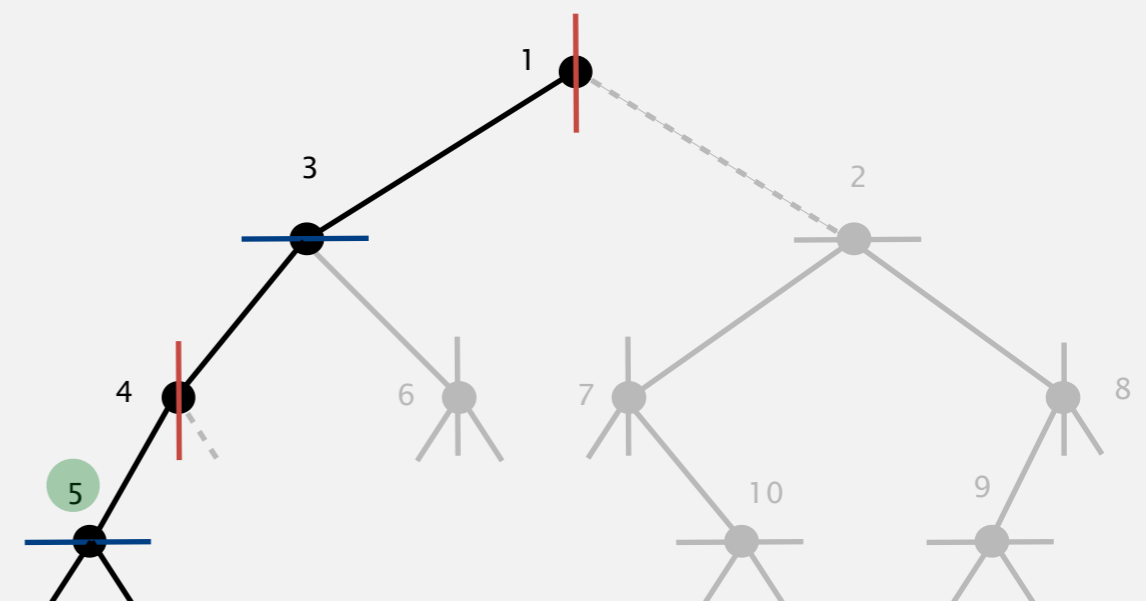
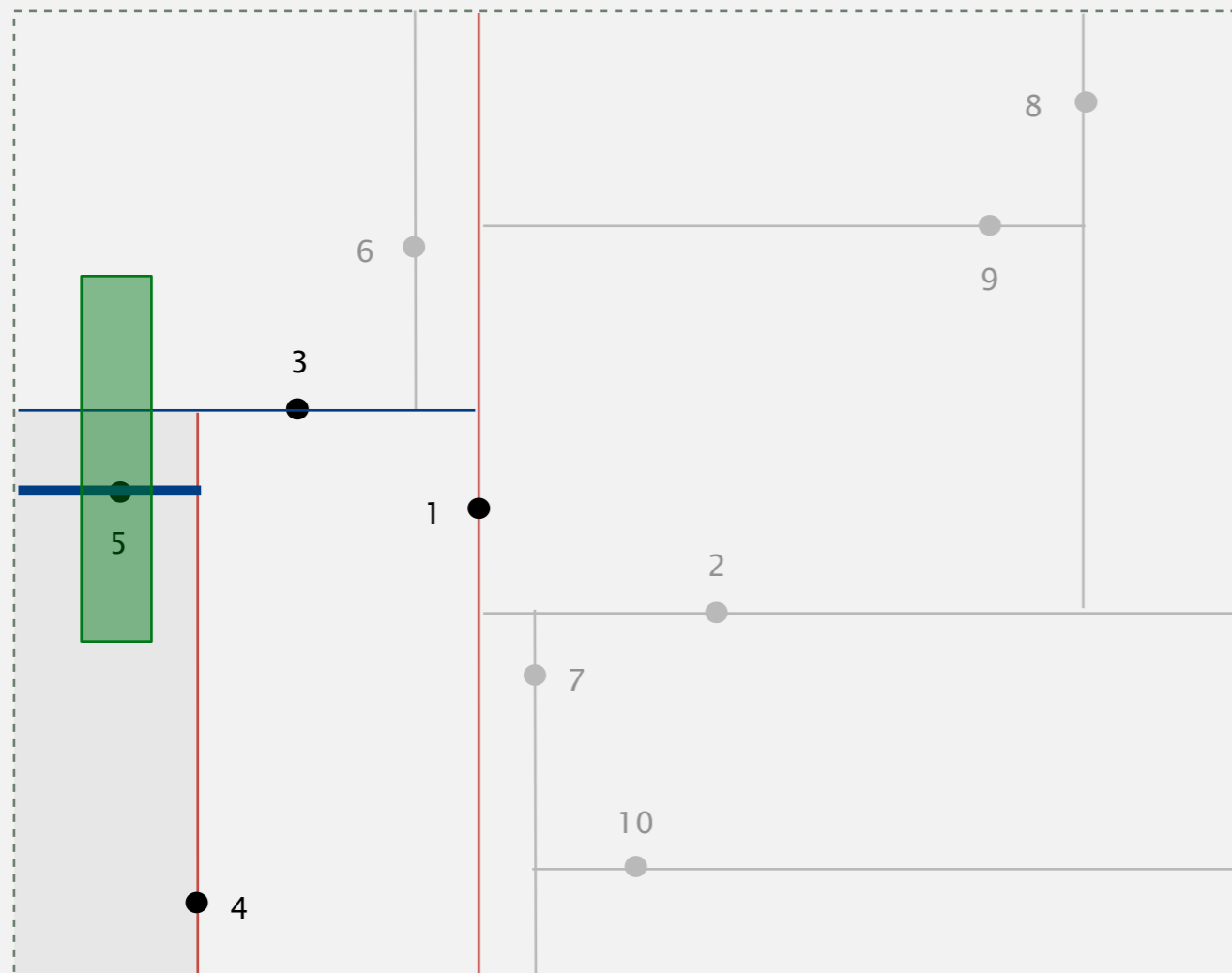
- Check if point in node lies in given rectangle.
- Recursively search left/bottom subdivision (if any could fall in rectangle).
- Recursively search right/top subdivision (if any could fall in rectangle).



**search top subtree  
stop since empty**

## Range search in a 2d tree

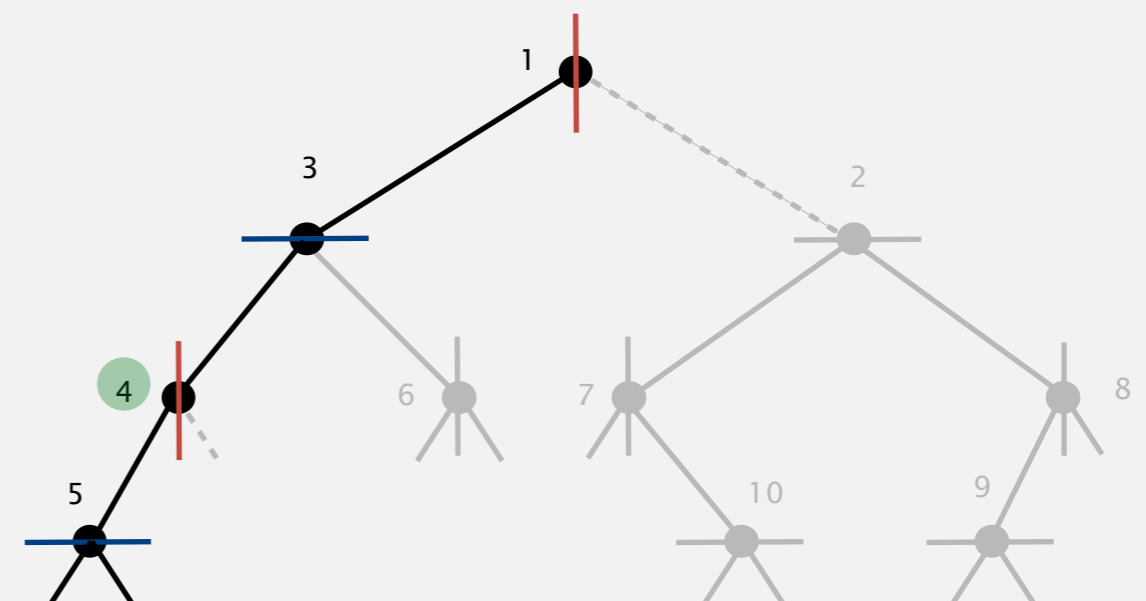
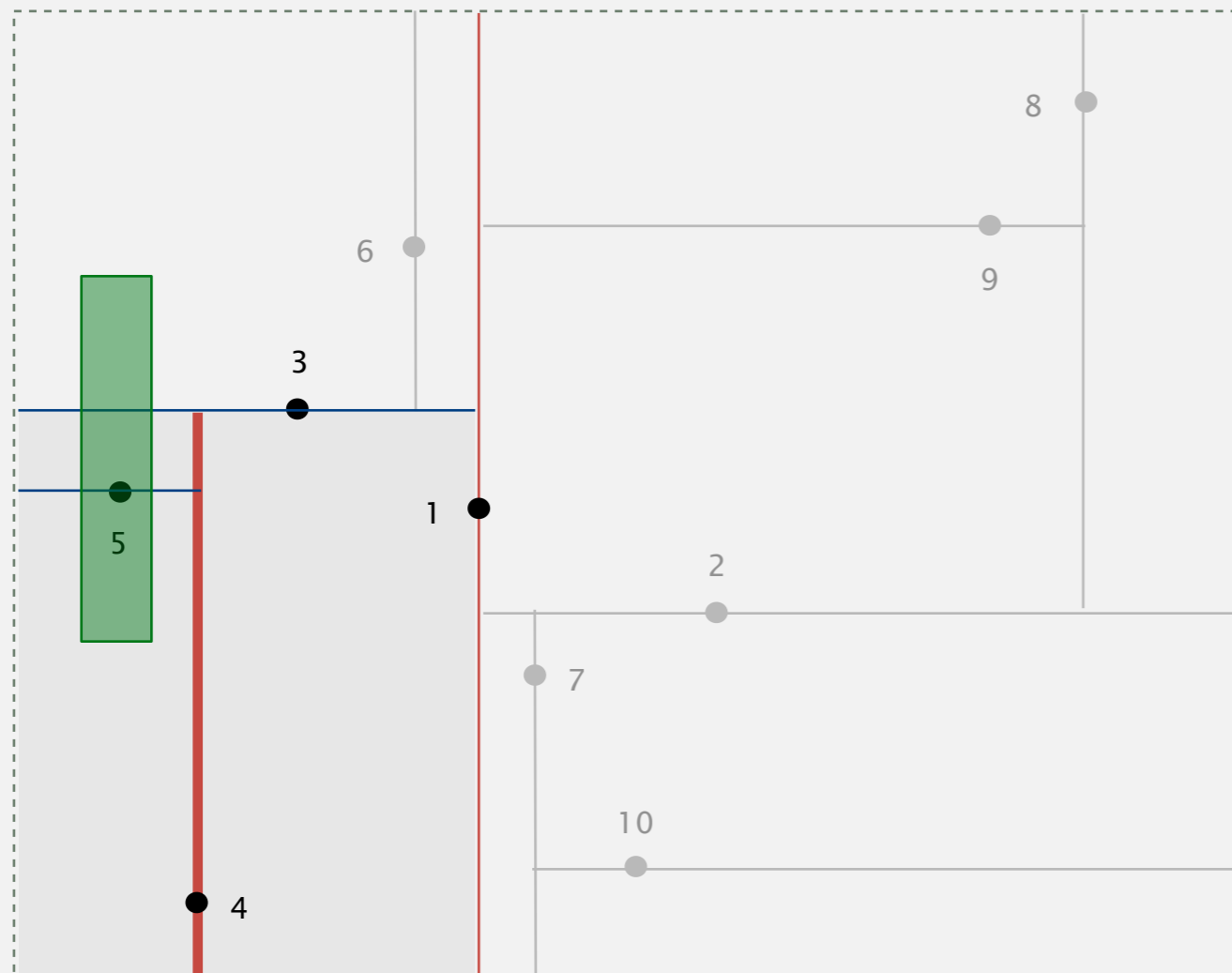
- Check if point in node lies in given rectangle.
- Recursively search left/bottom subdivision (if any could fall in rectangle).
- Recursively search right/top subdivision (if any could fall in rectangle).



return from function call

## Range search in a 2d tree

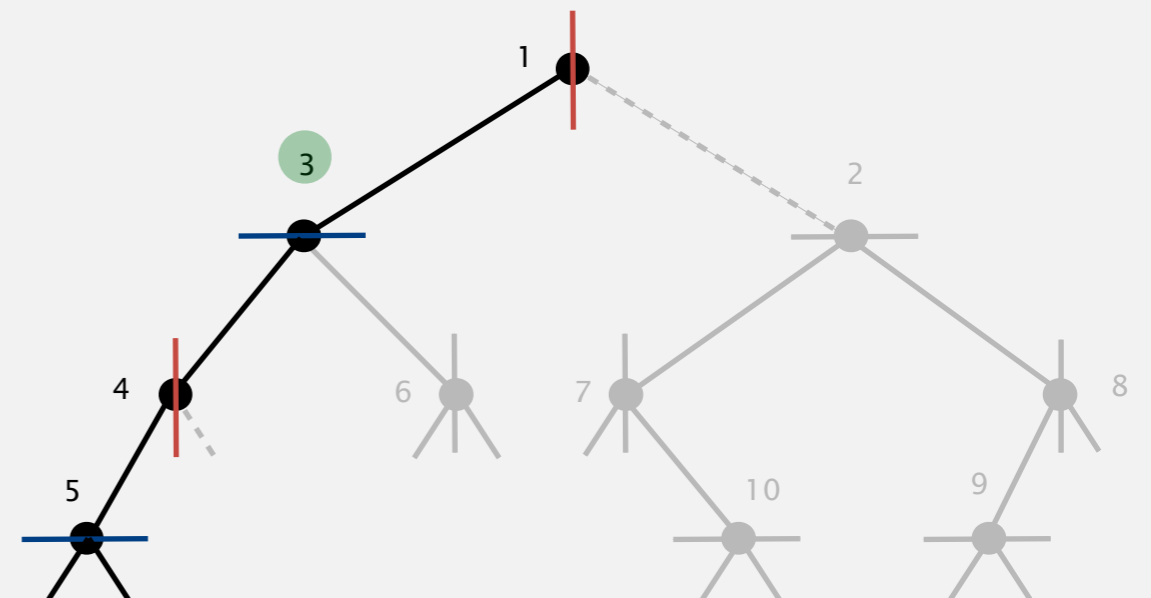
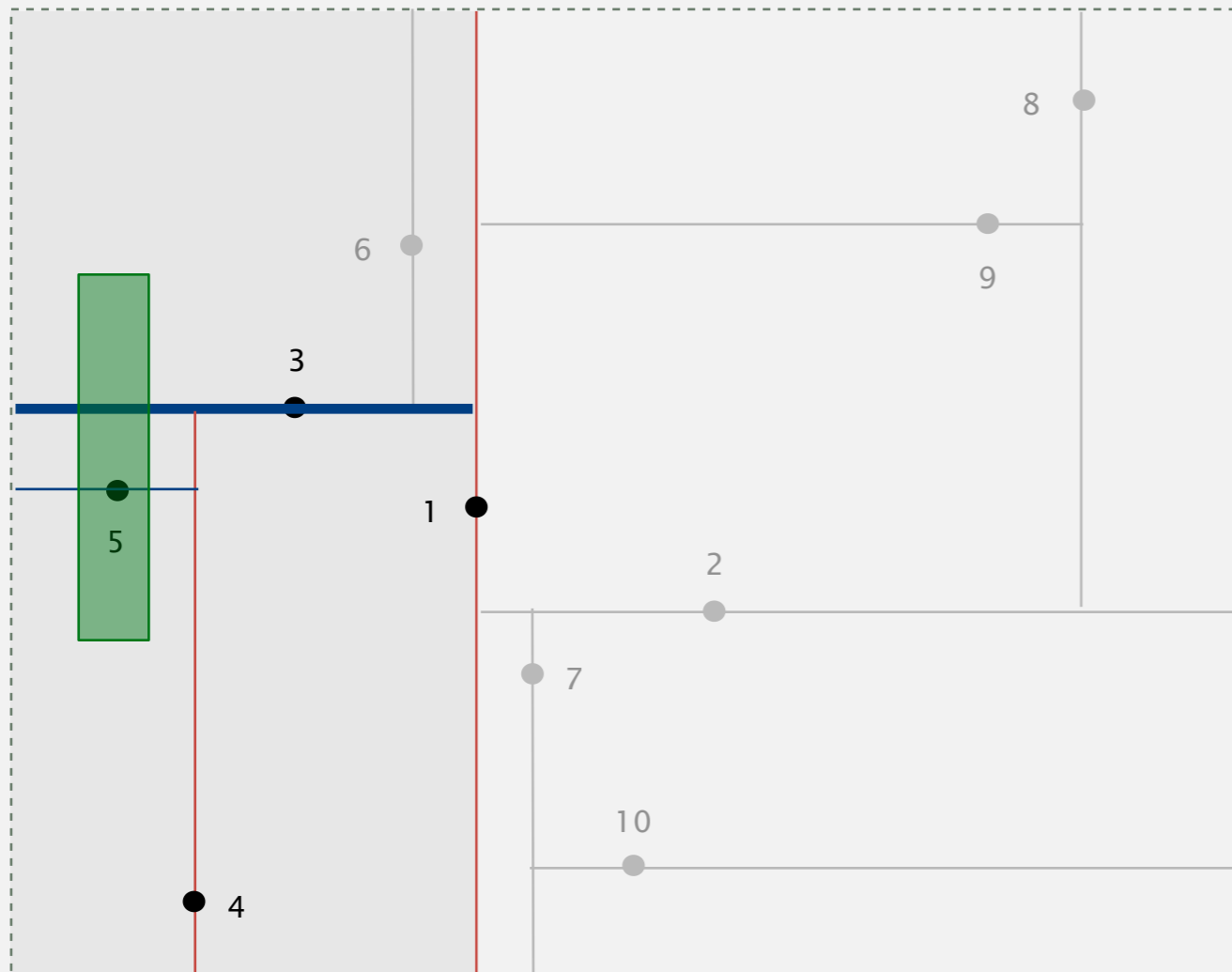
- Check if point in node lies in given rectangle.
- Recursively search left/bottom subdivision (if any could fall in rectangle).
- Recursively search right/top subdivision (if any could fall in rectangle).



return from function call

## Range search in a 2d tree

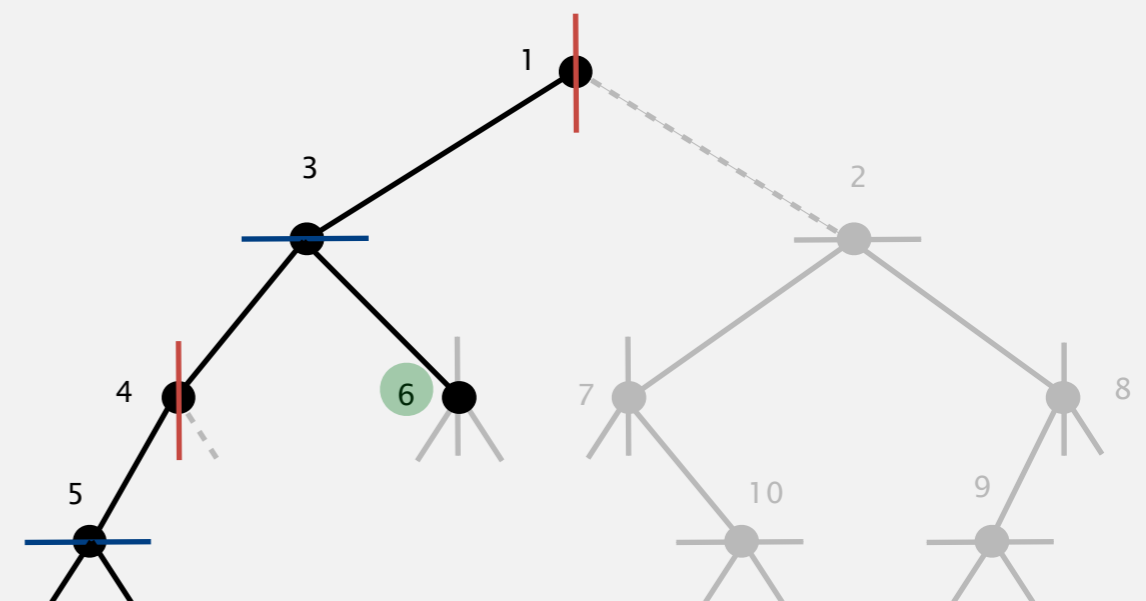
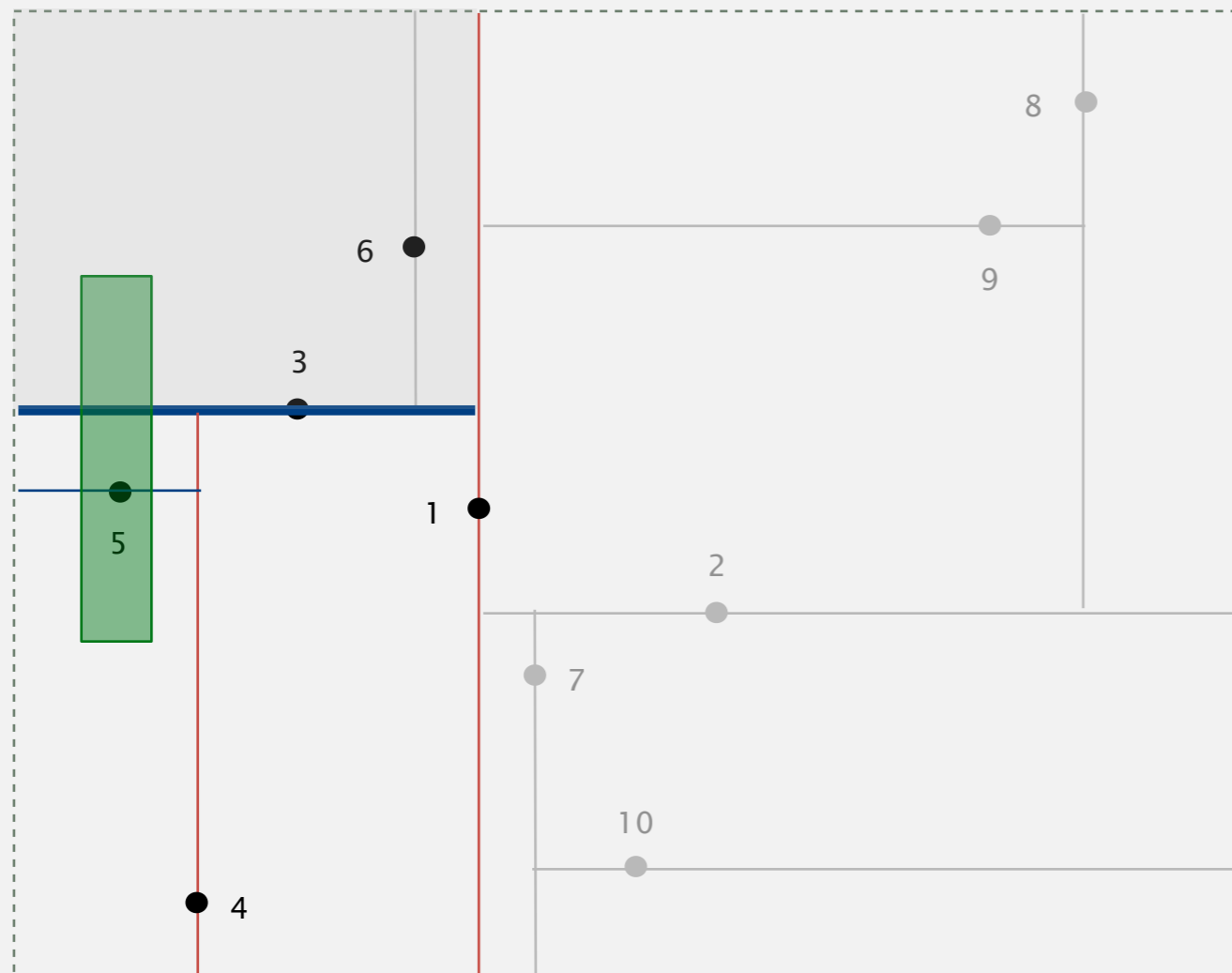
- Check if point in node lies in given rectangle.
- Recursively search left/bottom subdivision (if any could fall in rectangle).
- Recursively search right/top subdivision (if any could fall in rectangle).



return from function call

## Range search in a 2d tree

- Check if point in node lies in given rectangle.
- Recursively search left/bottom subdivision (if any could fall in rectangle).
- Recursively search right/top subdivision (if any could fall in rectangle).

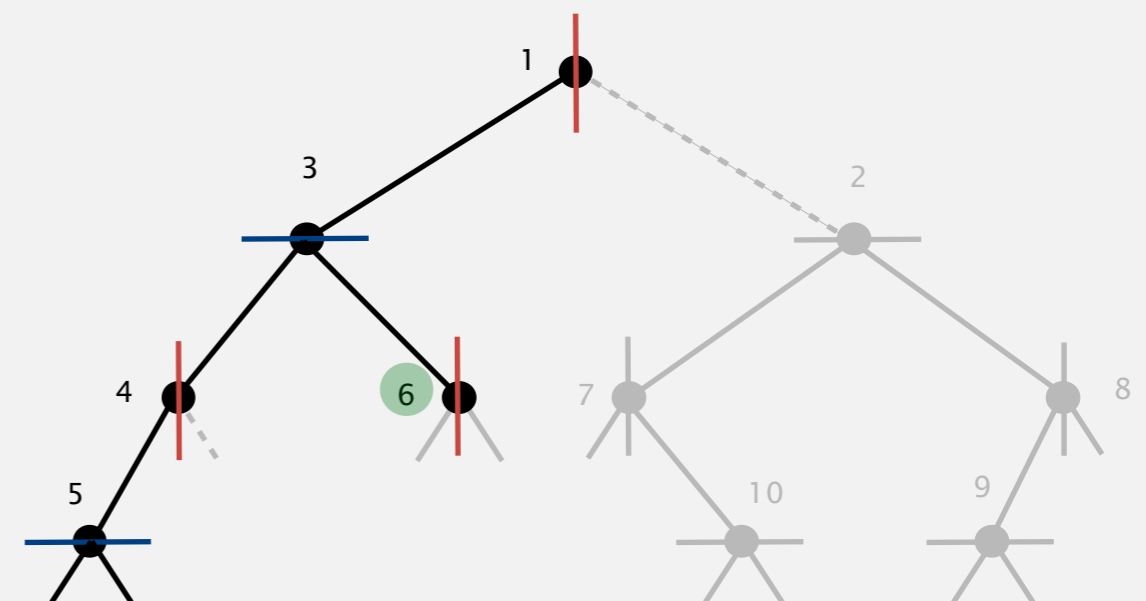
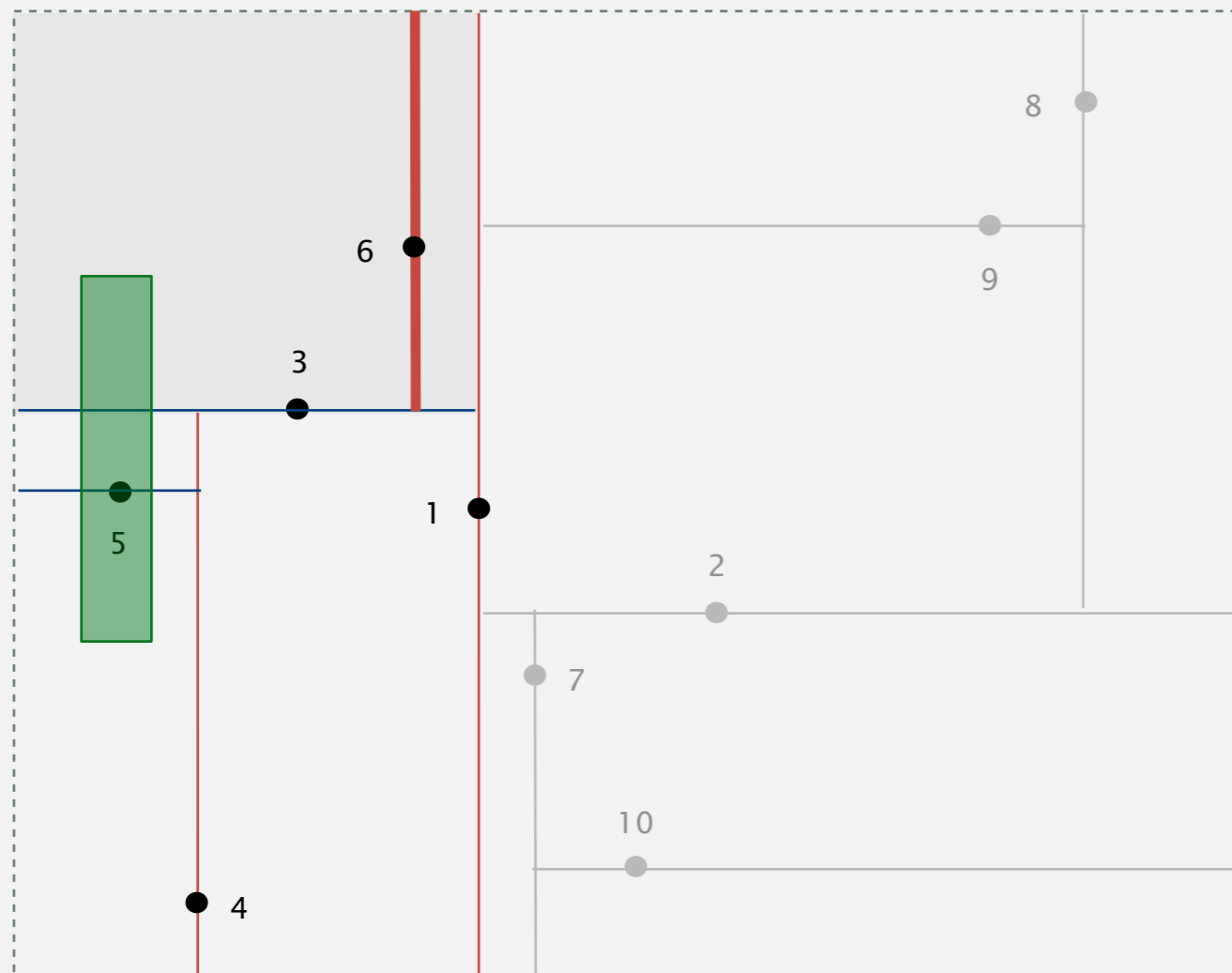


**search top subtree**  
**check if query rectangle contains point 6**



## Range search in a 2d tree

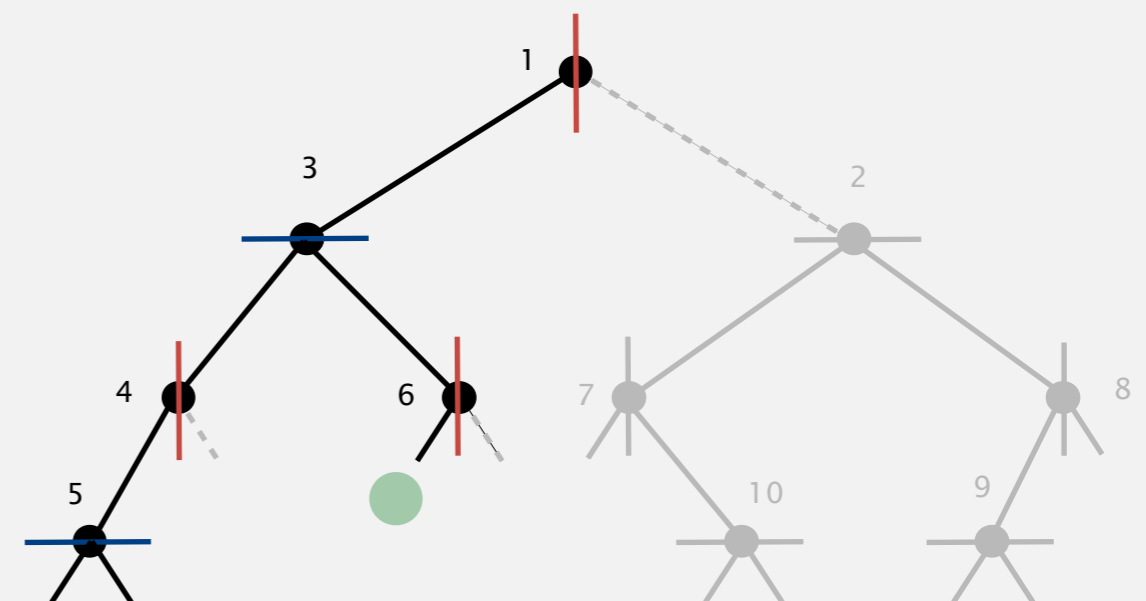
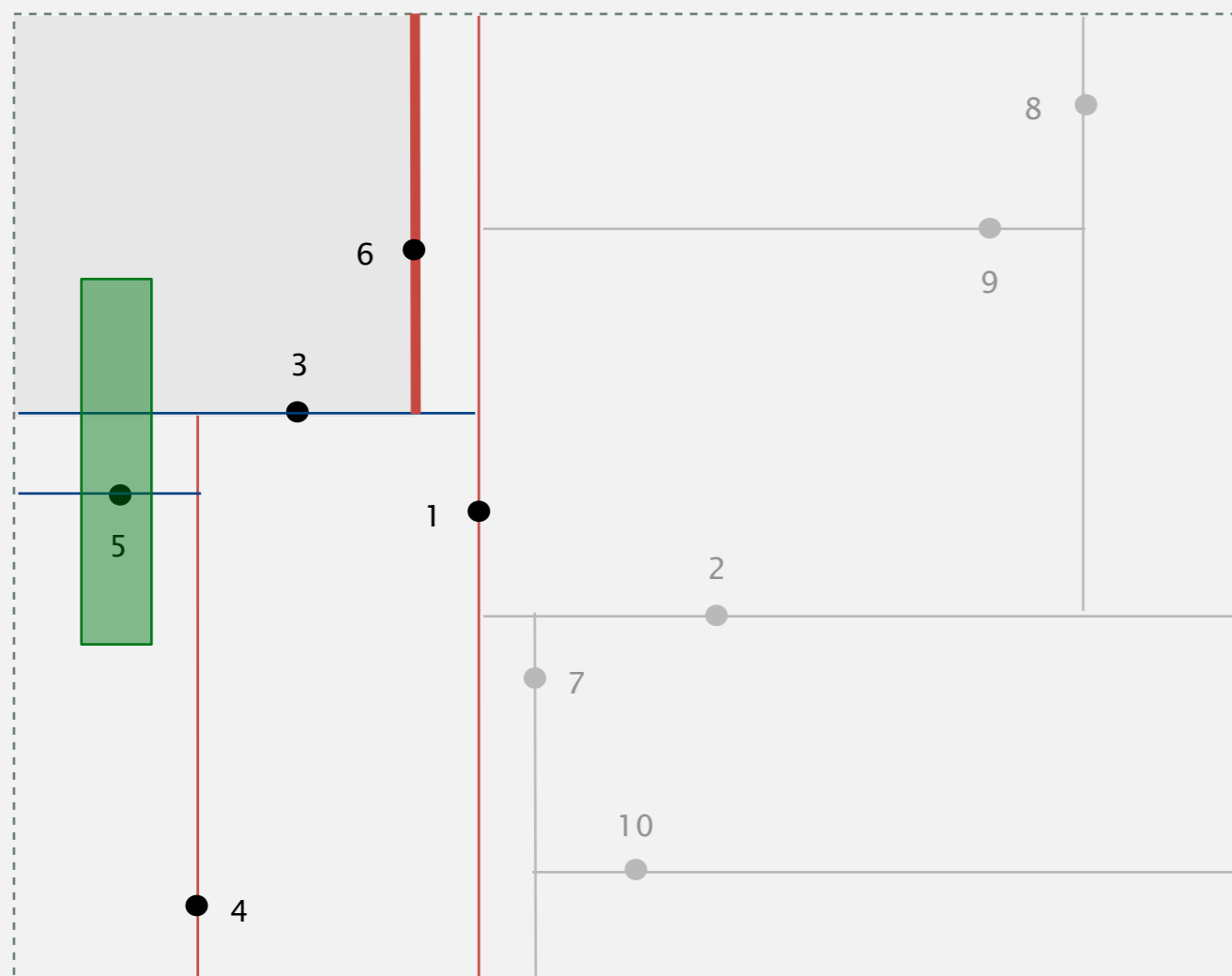
- Check if point in node lies in given rectangle.
- Recursively search left/bottom subdivision (if any could fall in rectangle).
- Recursively search right/top subdivision (if any could fall in rectangle).



query rectangle to left of splitting line  
search only in left subtree

## Range search in a 2d tree

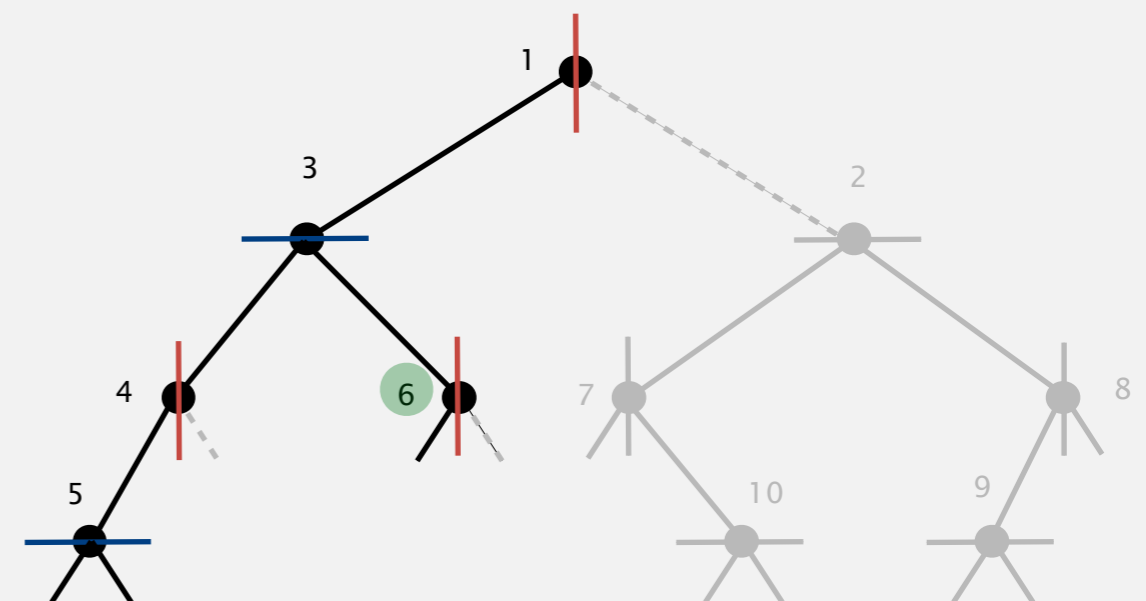
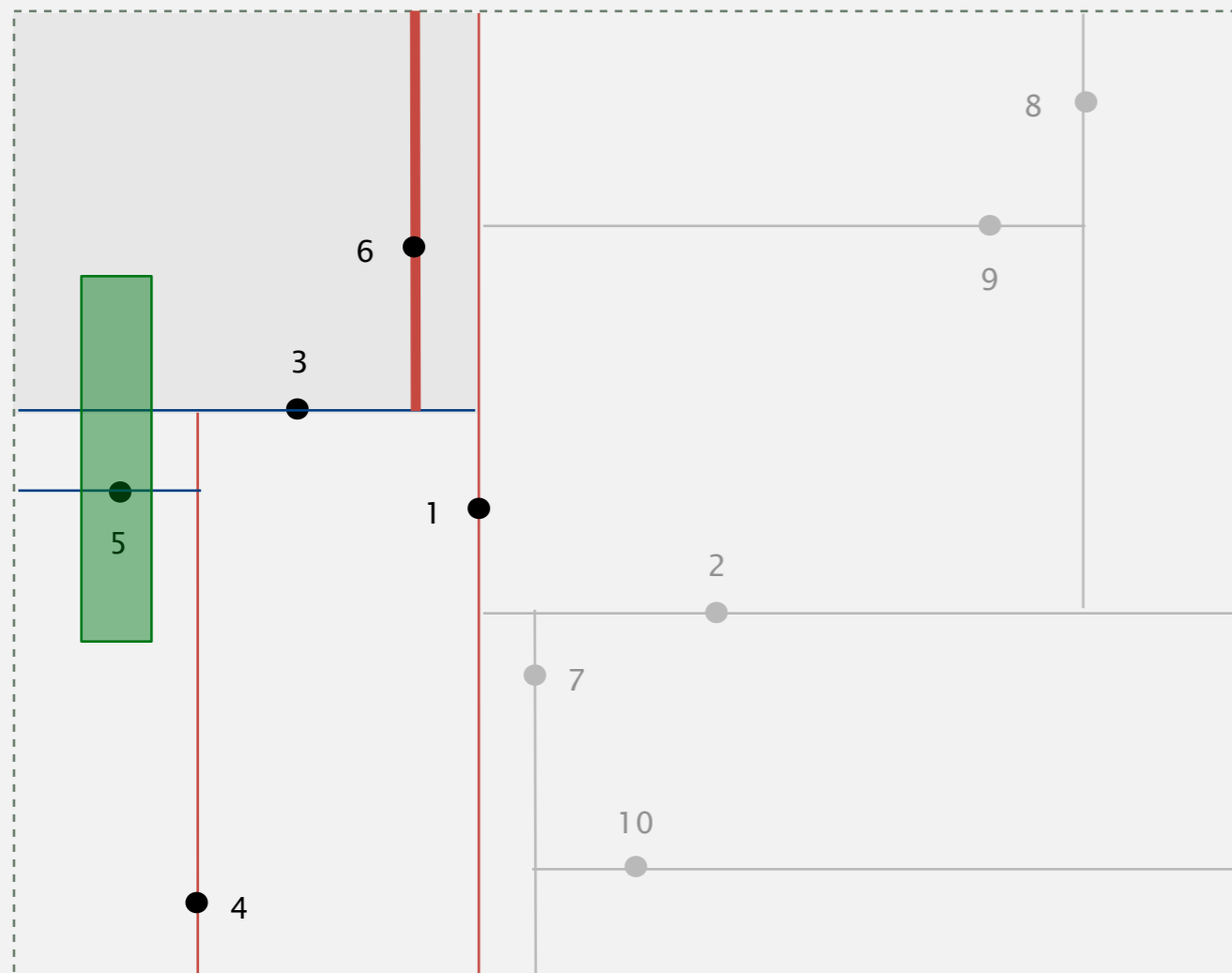
- Check if point in node lies in given rectangle.
- Recursively search left/bottom subdivision (if any could fall in rectangle).
- Recursively search right/top subdivision (if any could fall in rectangle).



**search left subtree  
stop since empty**

## Range search in a 2d tree

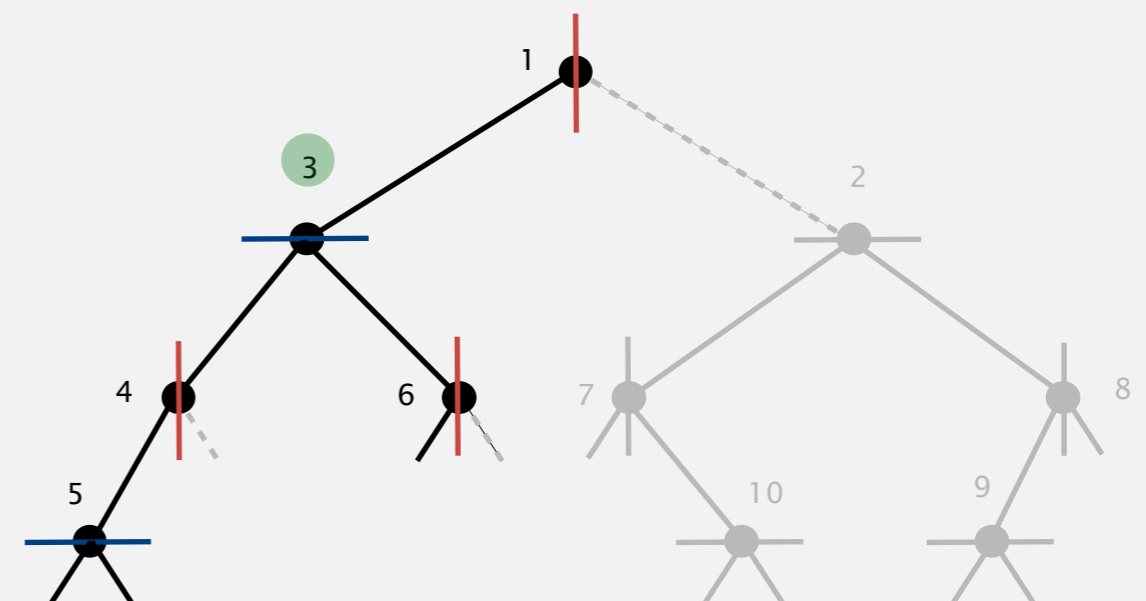
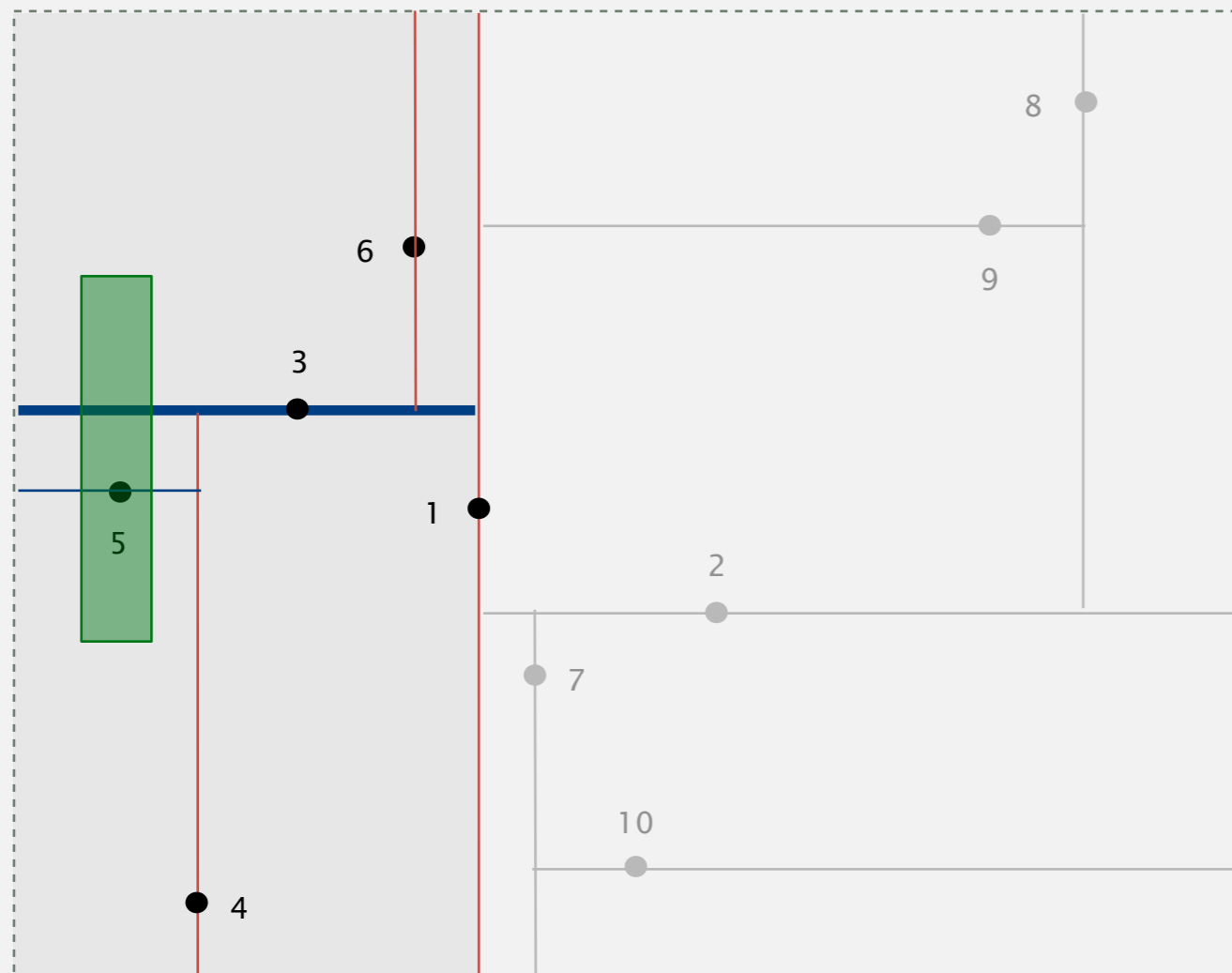
- Check if point in node lies in given rectangle.
- Recursively search left/bottom subdivision (if any could fall in rectangle).
- Recursively search right/top subdivision (if any could fall in rectangle).



return from function call

## Range search in a 2d tree

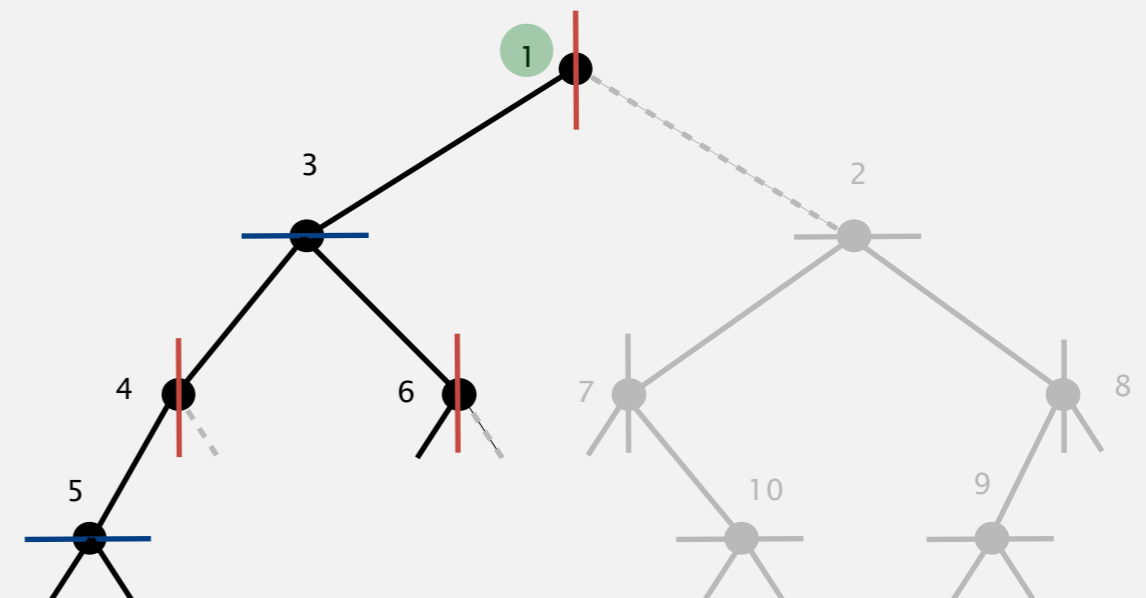
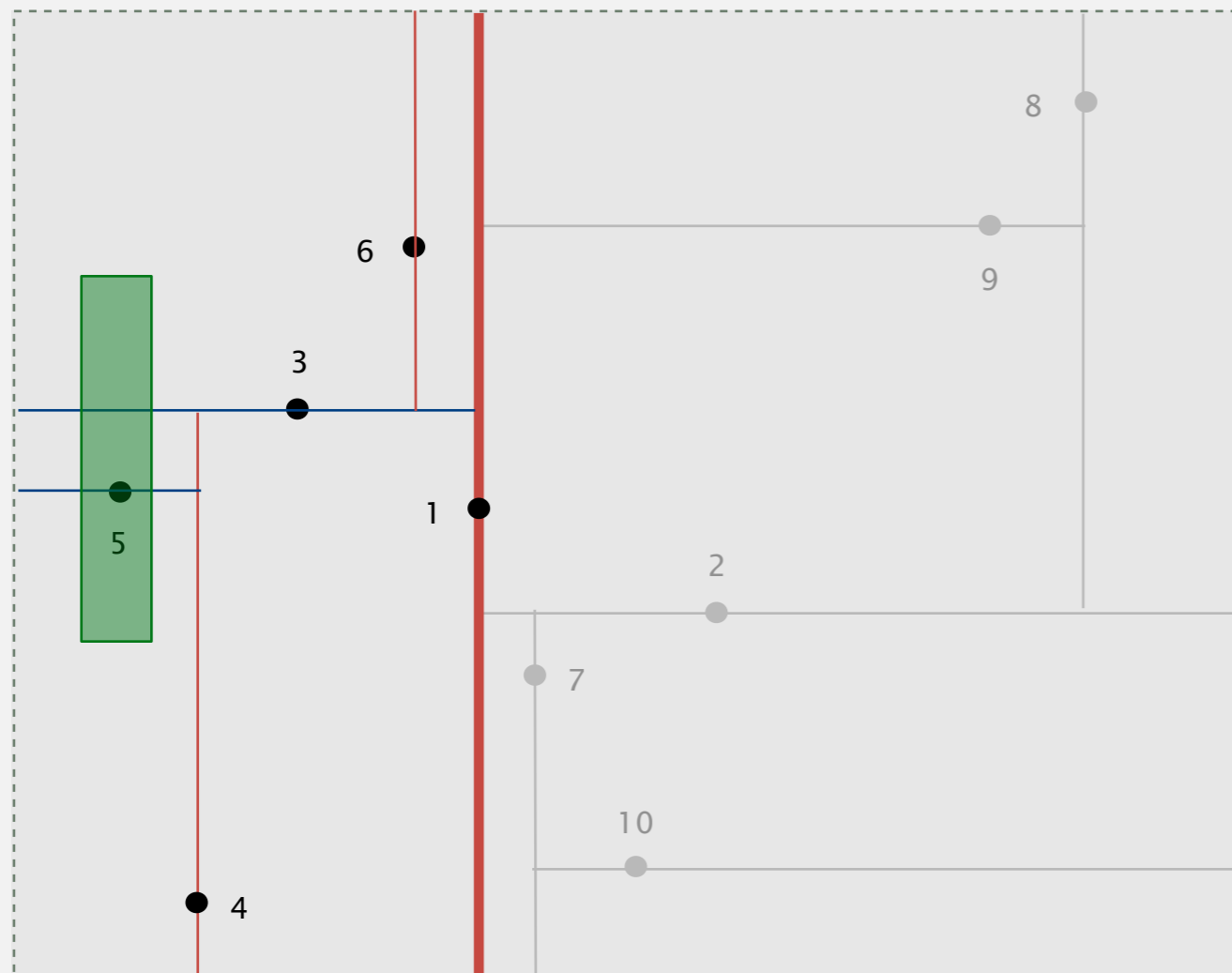
- Check if point in node lies in given rectangle.
- Recursively search left/bottom subdivision (if any could fall in rectangle).
- Recursively search right/top subdivision (if any could fall in rectangle).



return from function call

## Range search in a 2d tree

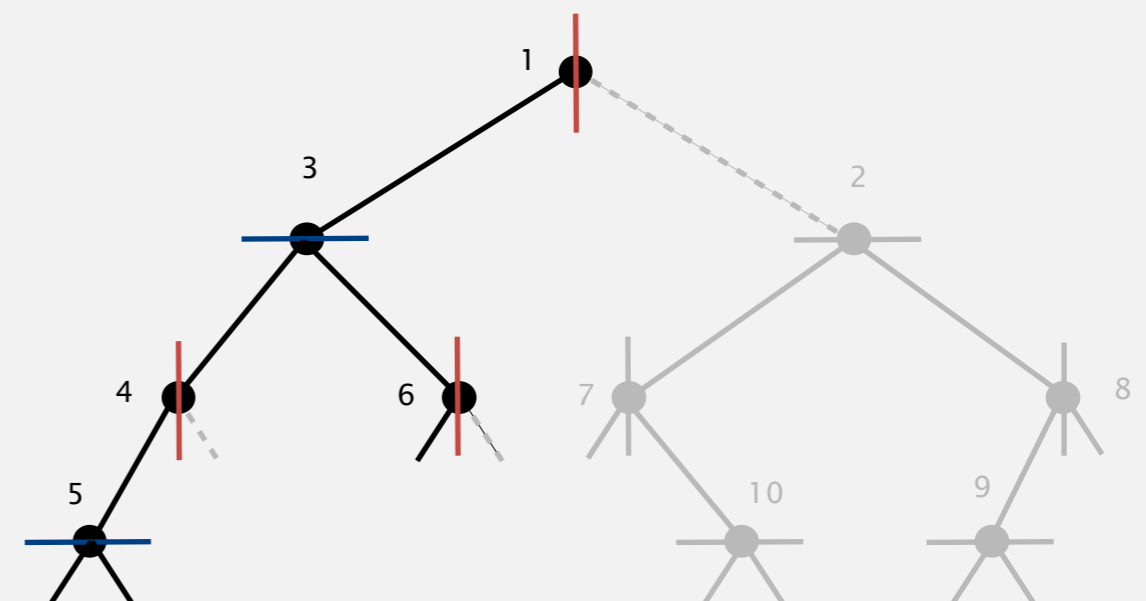
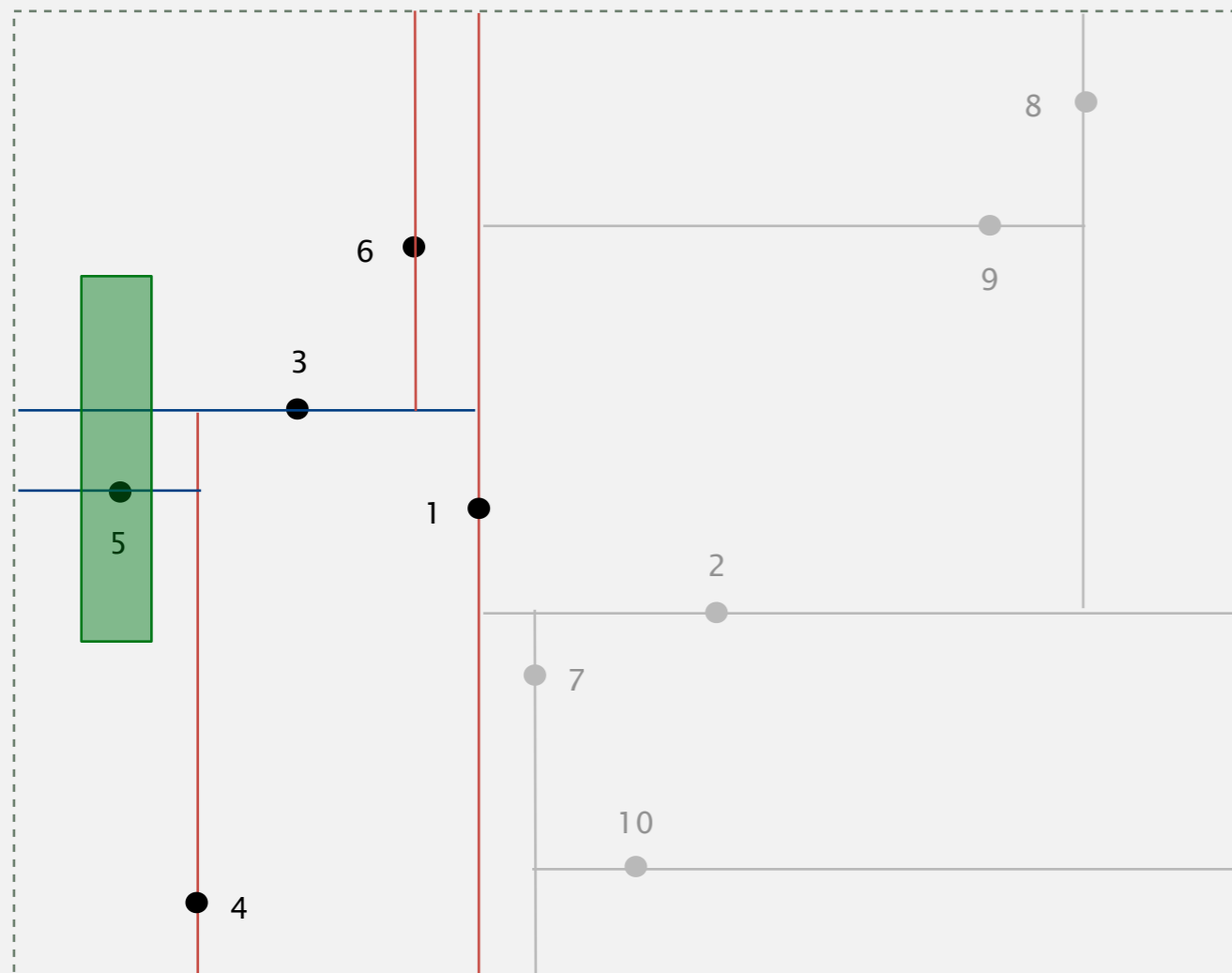
- Check if point in node lies in given rectangle.
- Recursively search left/bottom subdivision (if any could fall in rectangle).
- Recursively search right/top subdivision (if any could fall in rectangle).



return from function call

## Range search in a 2d tree

- Check if point in node lies in given rectangle.
- Recursively search left/bottom subdivision (if any could fall in rectangle).
- Recursively search right/top subdivision (if any could fall in rectangle).

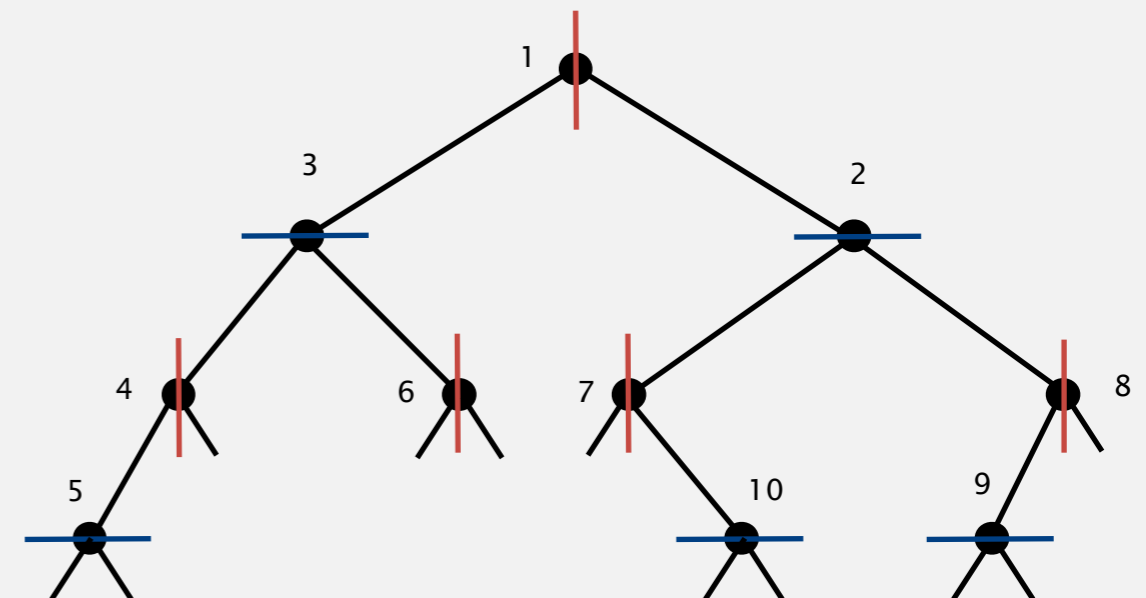
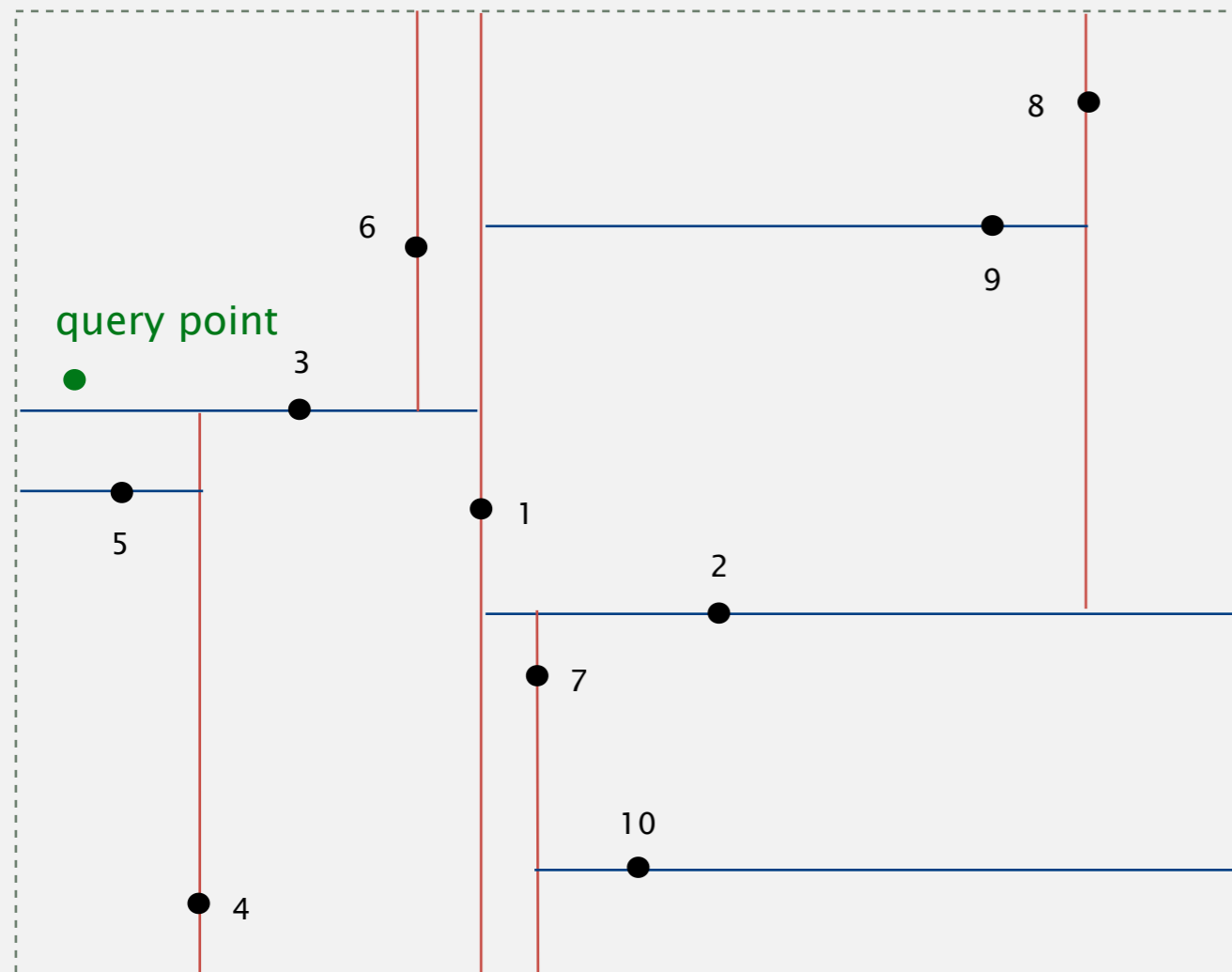


done

- ▶ insertion
- ▶ range search
- ▶ **nearest neighbor search**

## Nearest neighbor search in a 2d tree

- Check distance from point in node to query point.
- Recursively search left/bottom subdivision (if it could contain a closer point).
- Recursively search right/top subdivision (if it could contain a closer point).
- Organize recursive method so that it begins by searching for query point.

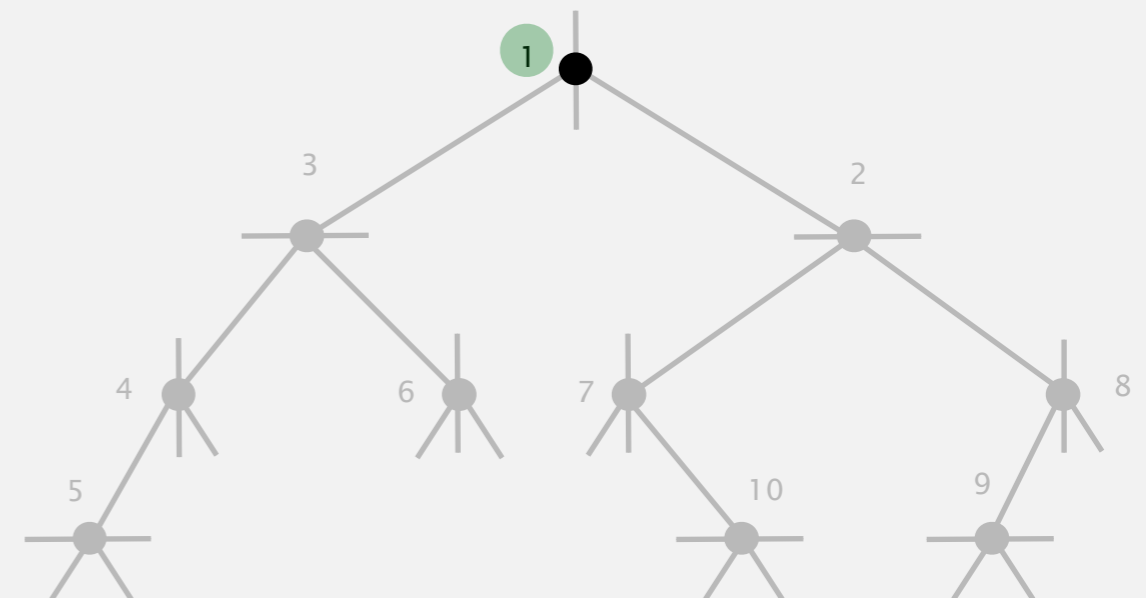
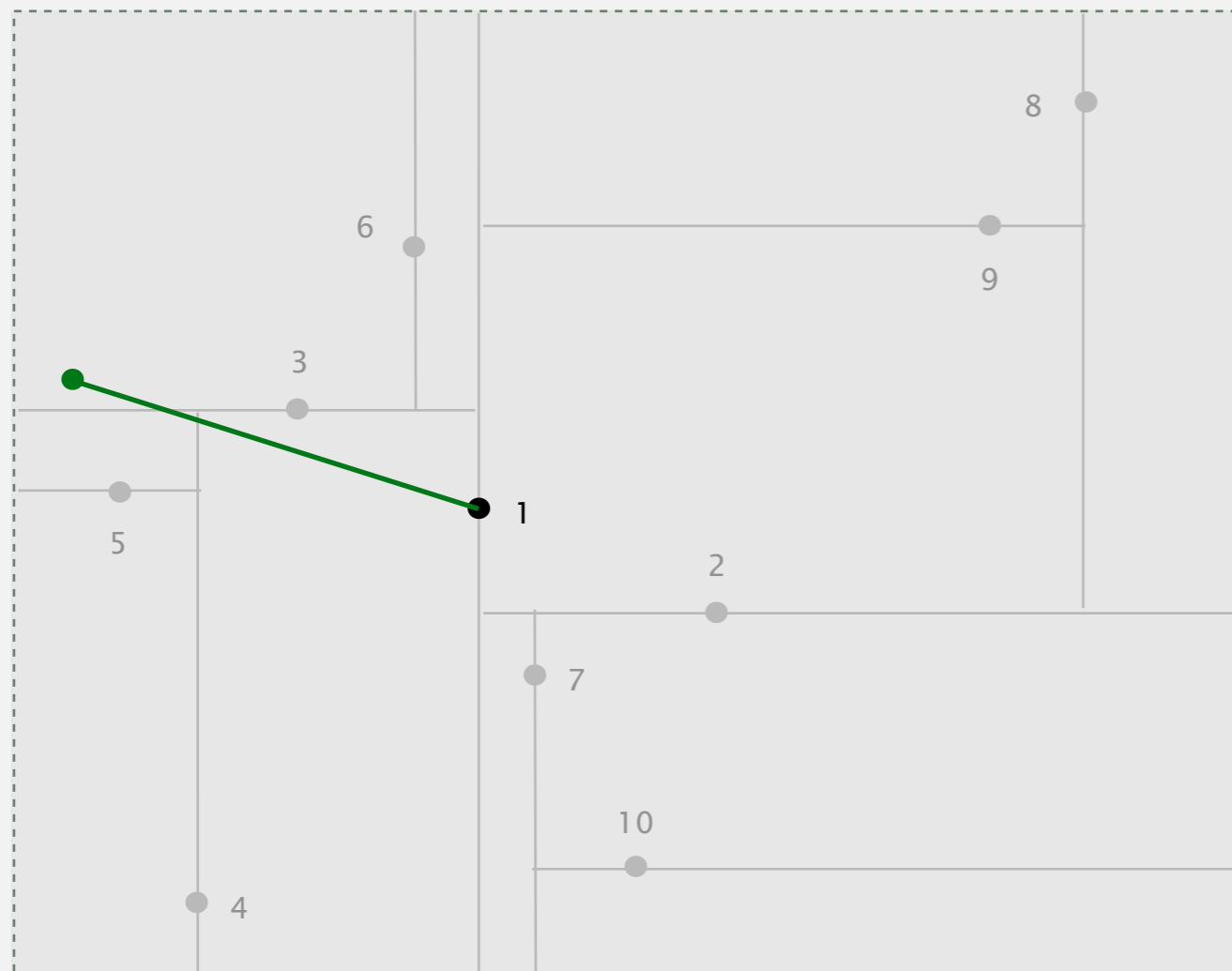


find closest points in 2d tree  
to green query point



## Nearest neighbor search in a 2d tree

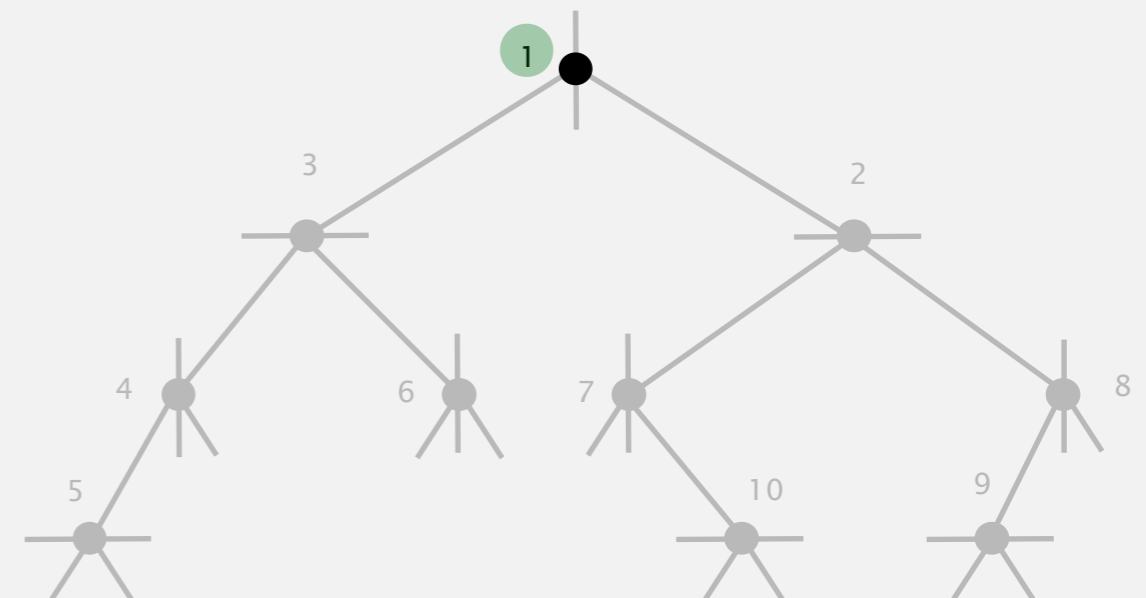
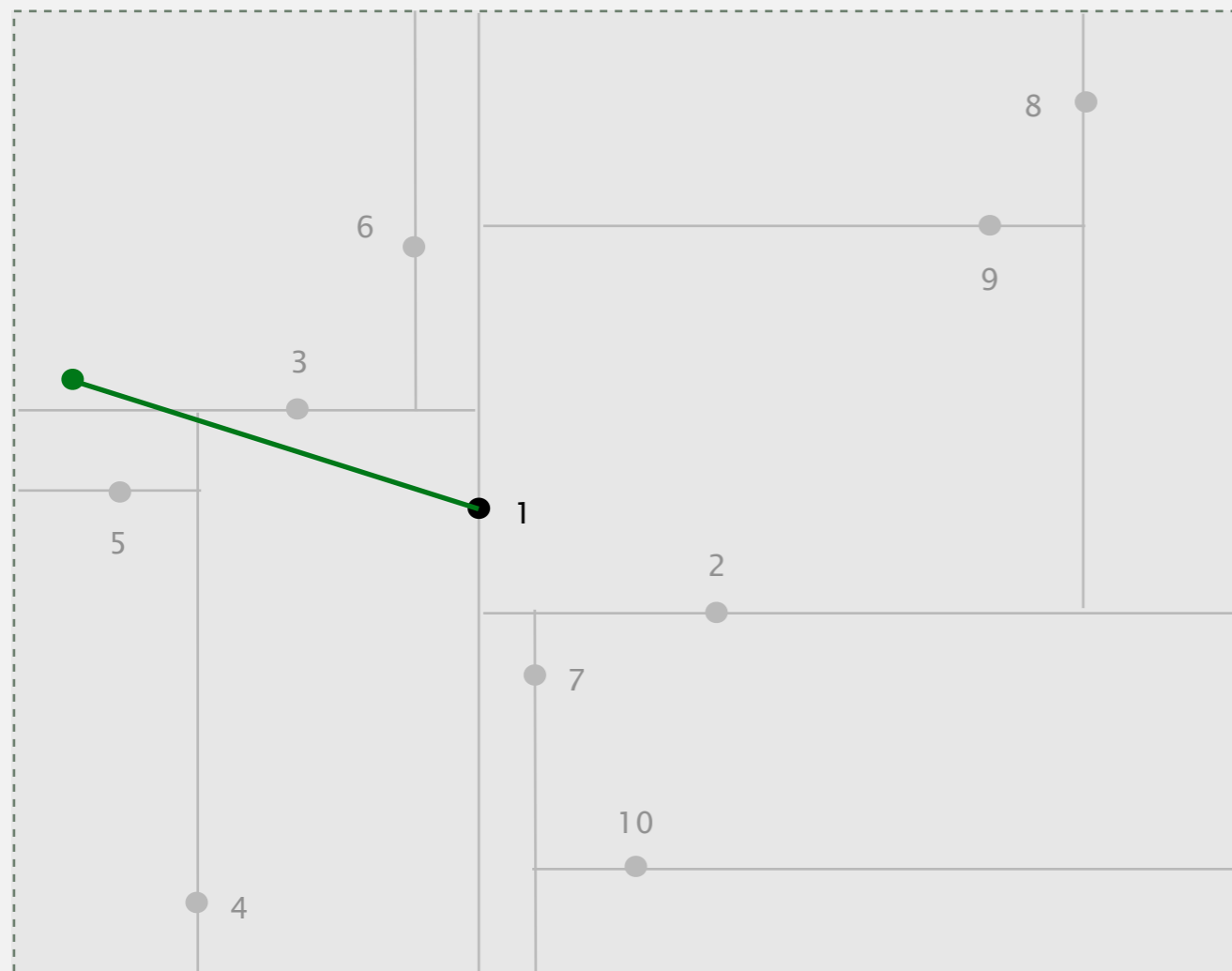
- Check distance from point in node to query point.
- Recursively search left/bottom subdivision (if it could contain a closer point).
- Recursively search right/top subdivision (if it could contain a closer point).
- Organize recursive method so that it begins by searching for query point.



**search root node**  
**compute distance from query point to 1**  
**(update champion nearest neighbor)**

## Nearest neighbor search in a 2d tree

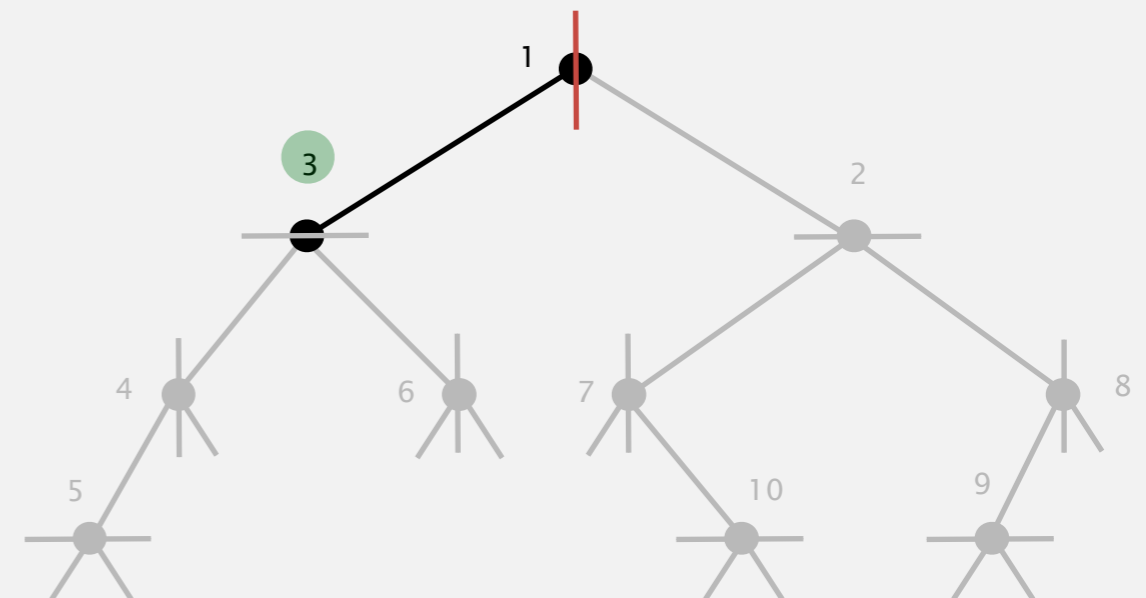
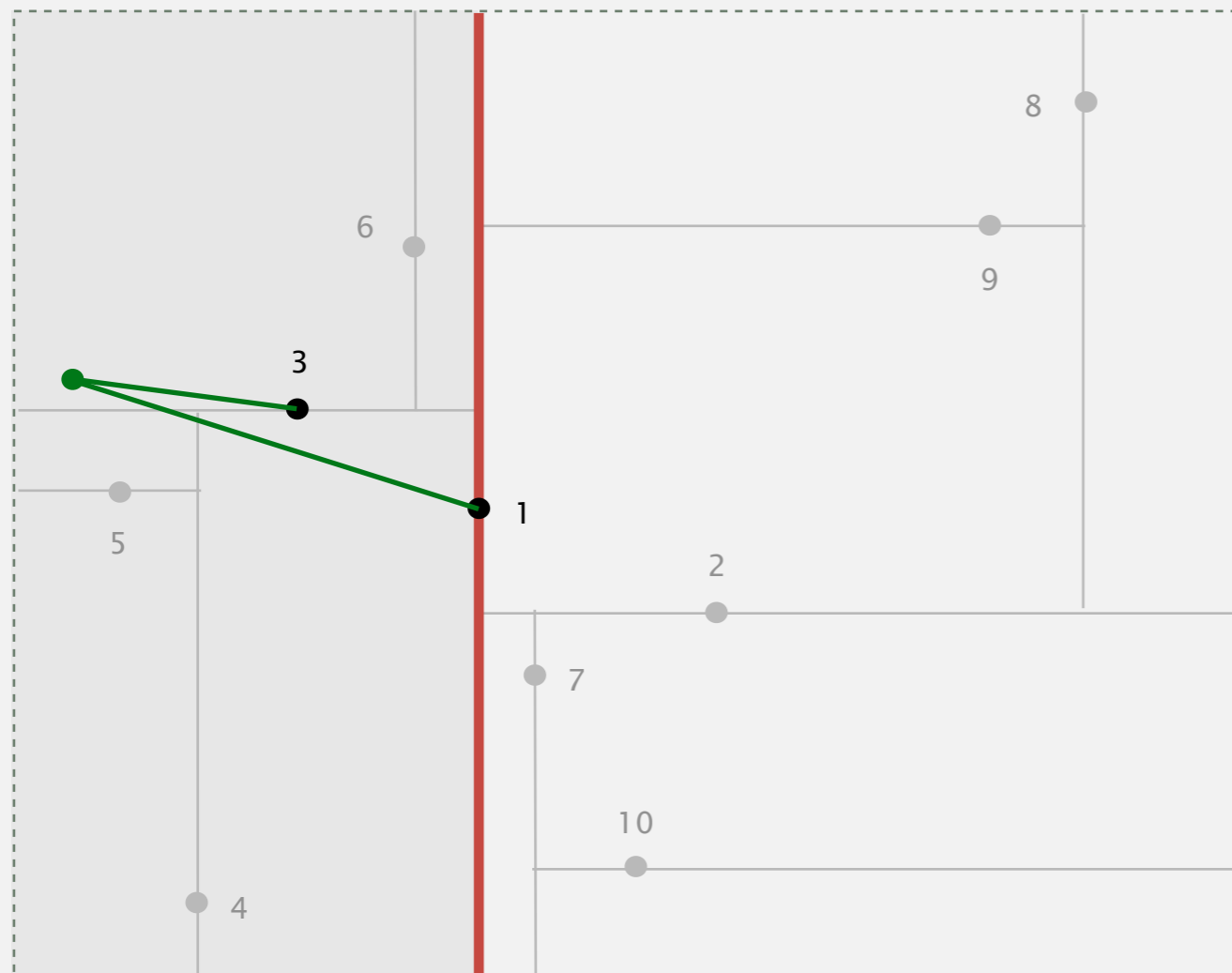
- Check distance from point in node to query point.
- Recursively search left/bottom subdivision (if it could contain a closer point).
- Recursively search right/top subdivision (if it could contain a closer point).
- Organize recursive method so that it begins by searching for query point.



**query point is to the left of splitting line  
search left subtree first**

## Nearest neighbor search in a 2d tree

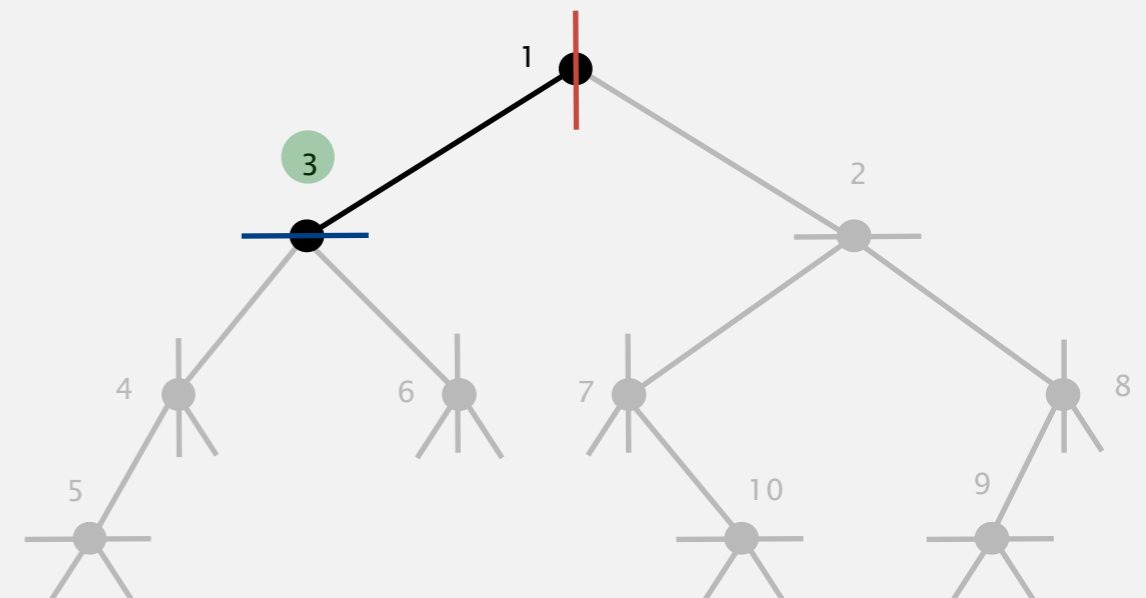
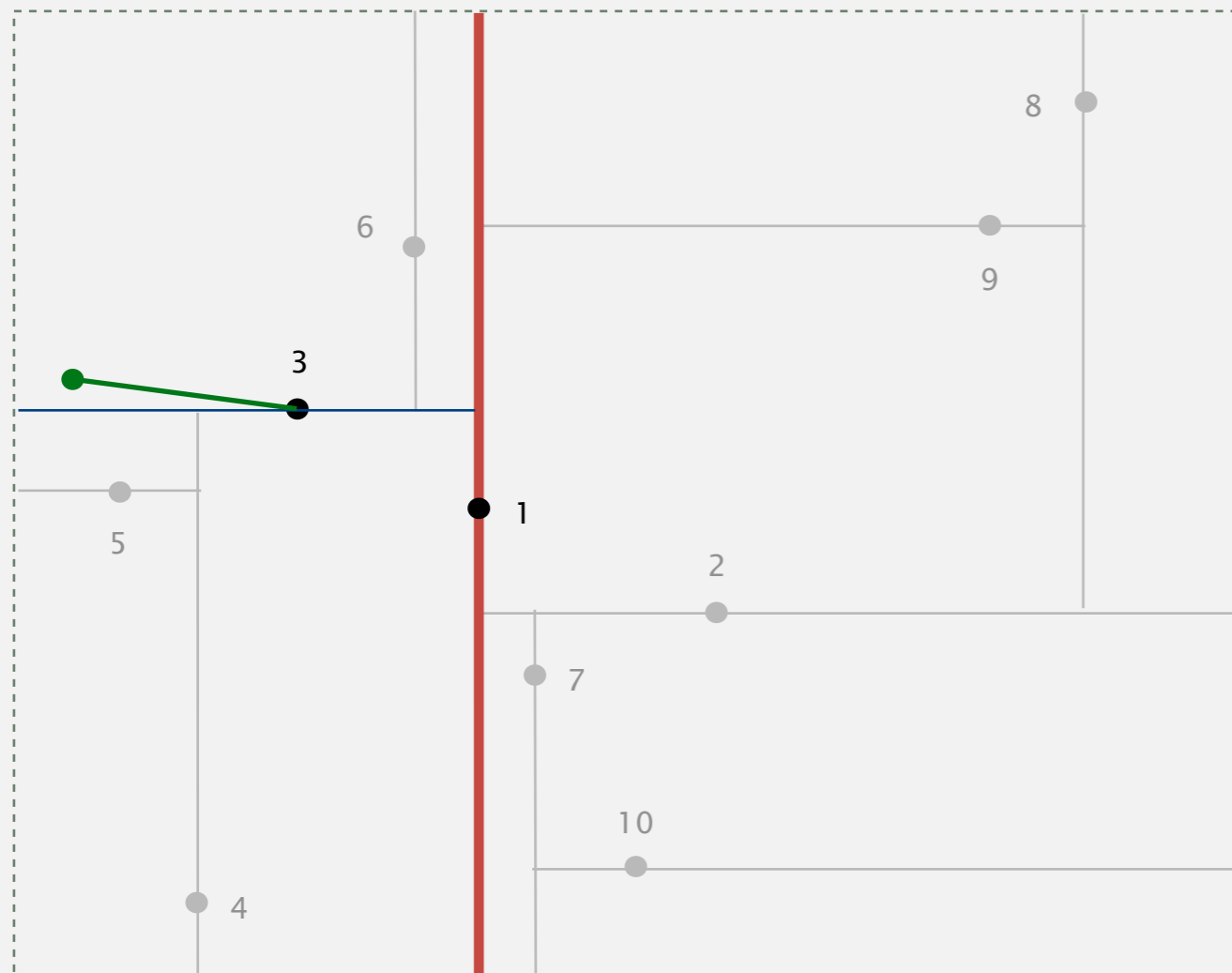
- Check distance from point in node to query point.
- Recursively search left/bottom subdivision (if it could contain a closer point).
- Recursively search right/top subdivision (if it could contain a closer point).
- Organize recursive method so that it begins by searching for query point.



**search left subtree**  
**compute distance from query point to 3**  
**(update champion)**

## Nearest neighbor search in a 2d tree

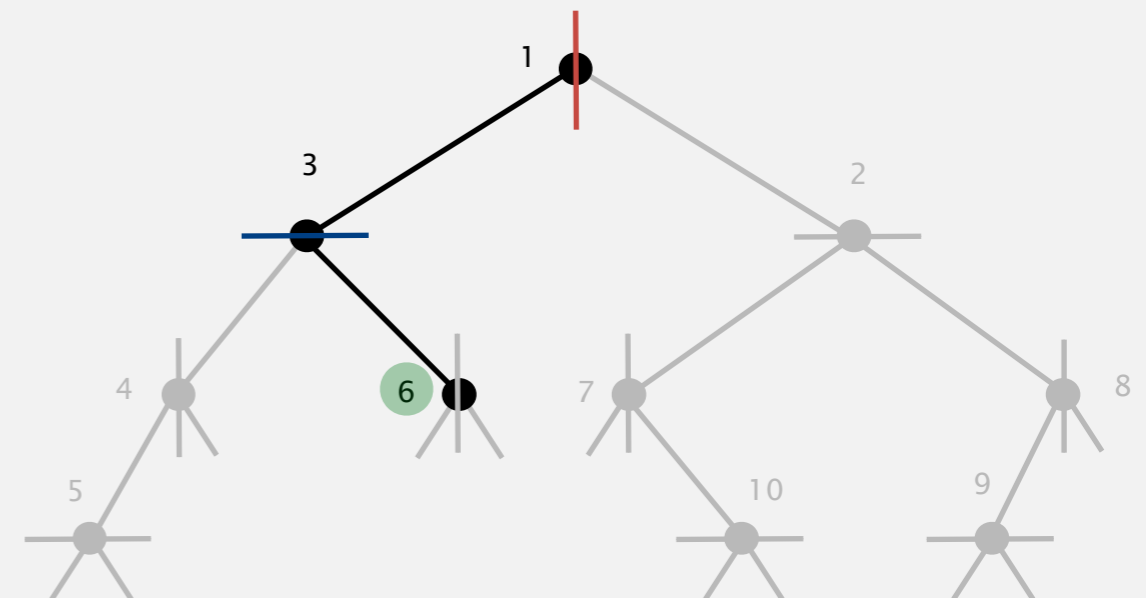
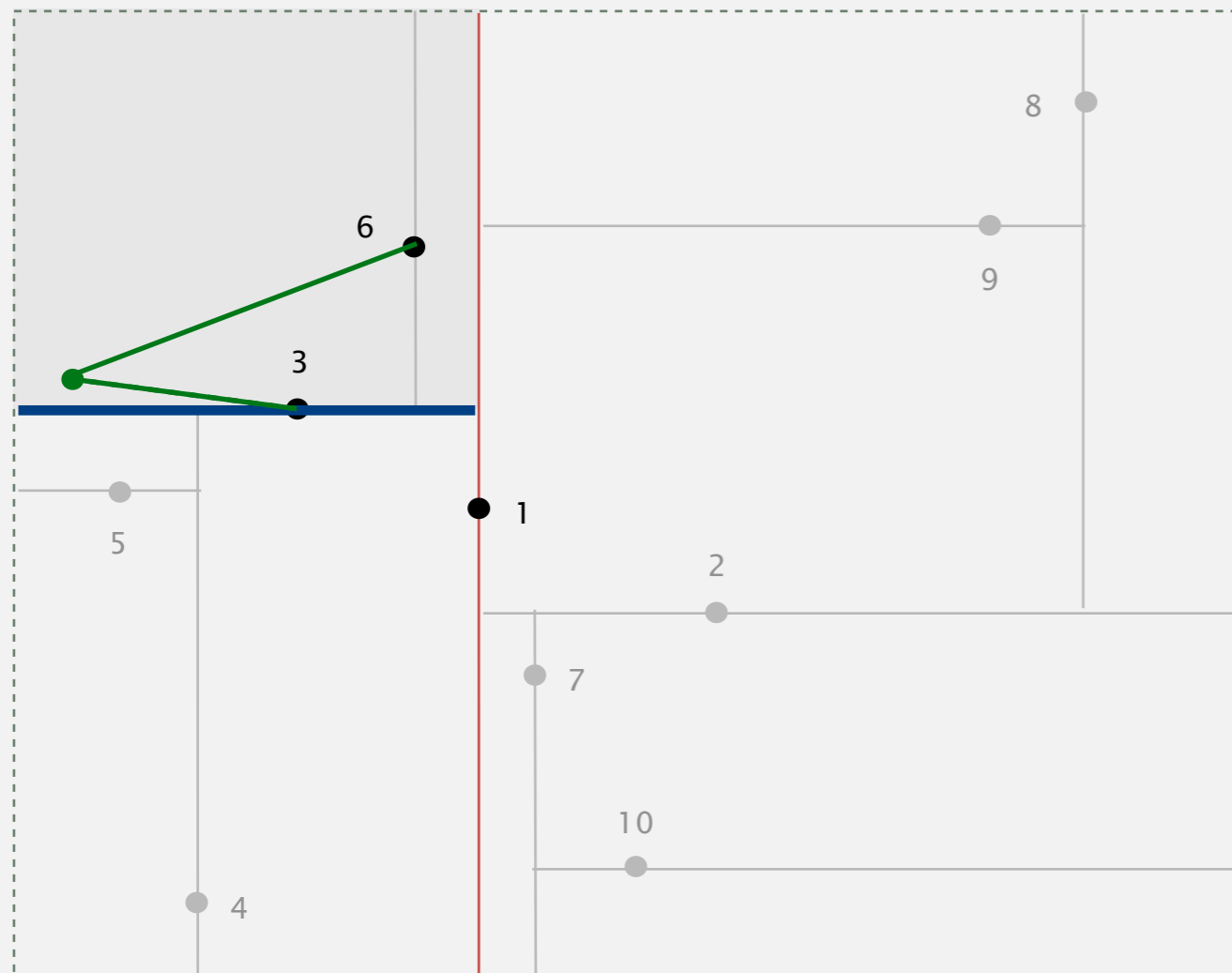
- Check distance from point in node to query point.
- Recursively search left/bottom subdivision (if it could contain a closer point).
- Recursively search right/top subdivision (if it could contain a closer point).
- Organize recursive method so that it begins by searching for query point.



**query point is above splitting line  
search top subtree first**

## Nearest neighbor search in a 2d tree

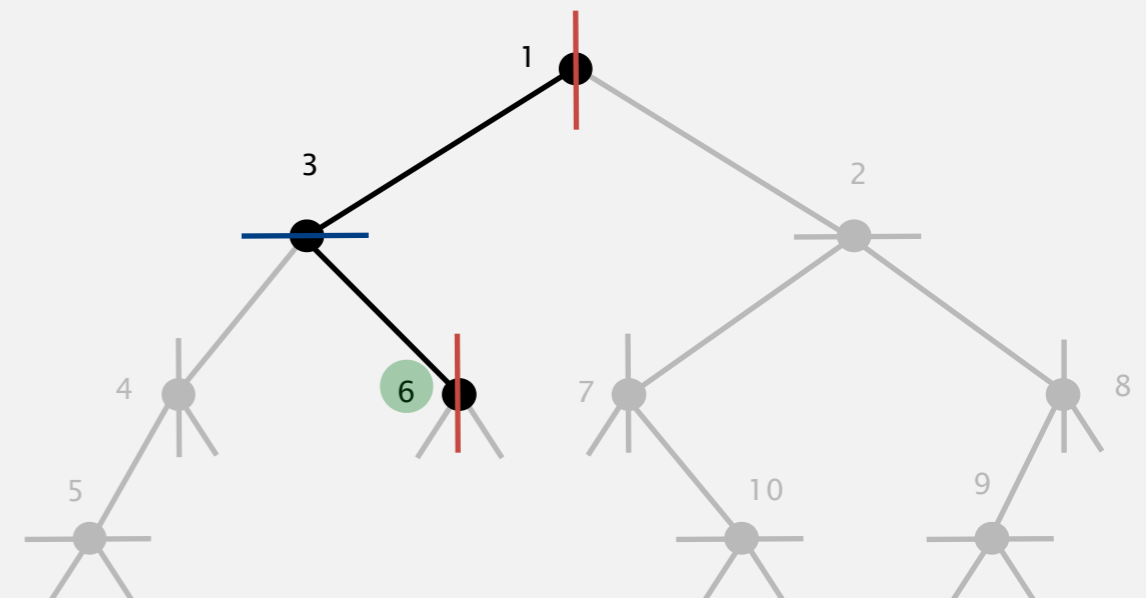
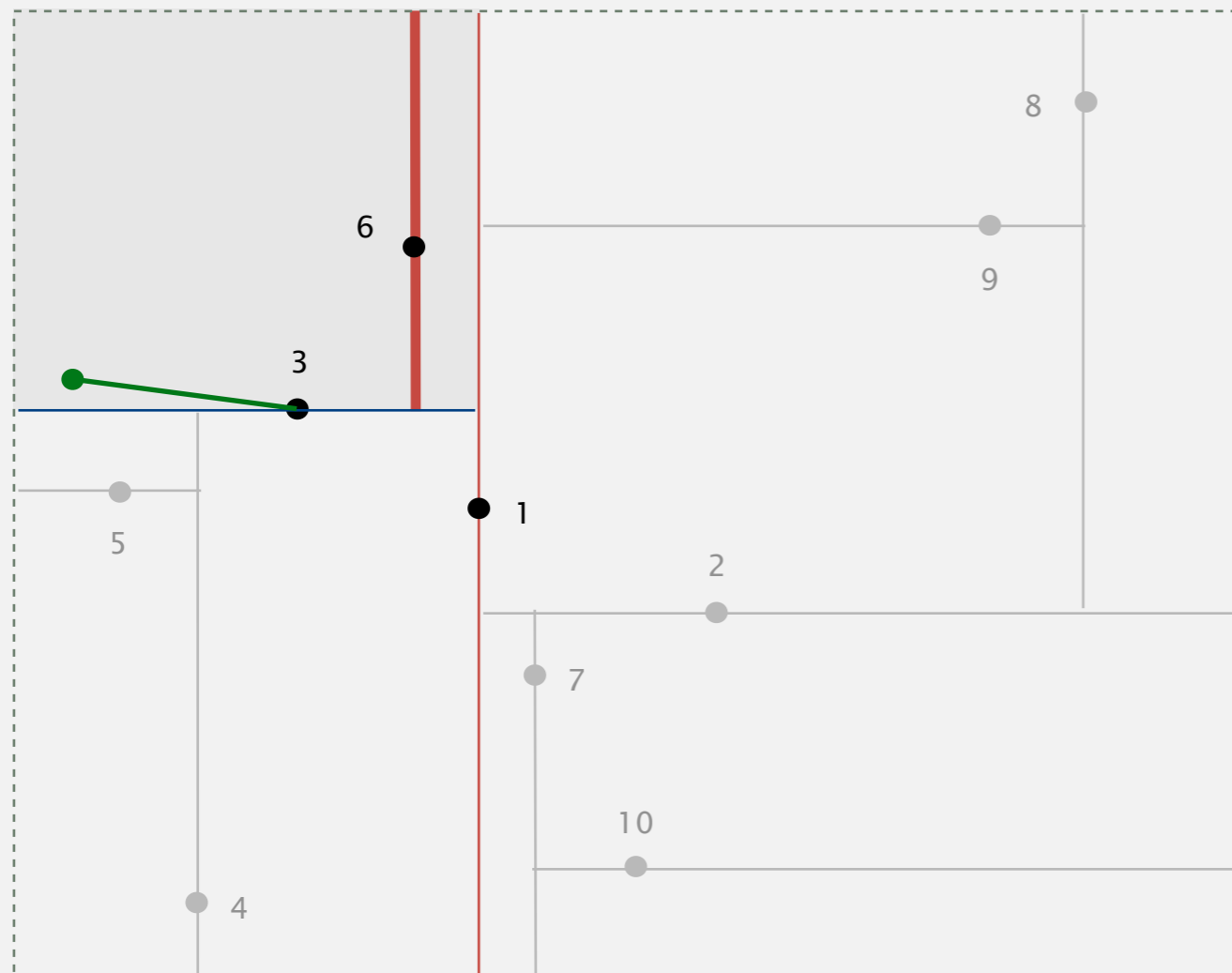
- Check distance from point in node to query point.
- Recursively search left/bottom subdivision (if it could contain a closer point).
- Recursively search right/top subdivision (if it could contain a closer point).
- Organize recursive method so that it begins by searching for query point.



**search top subtree**  
**compute distance from query point to 6**

## Nearest neighbor search in a 2d tree

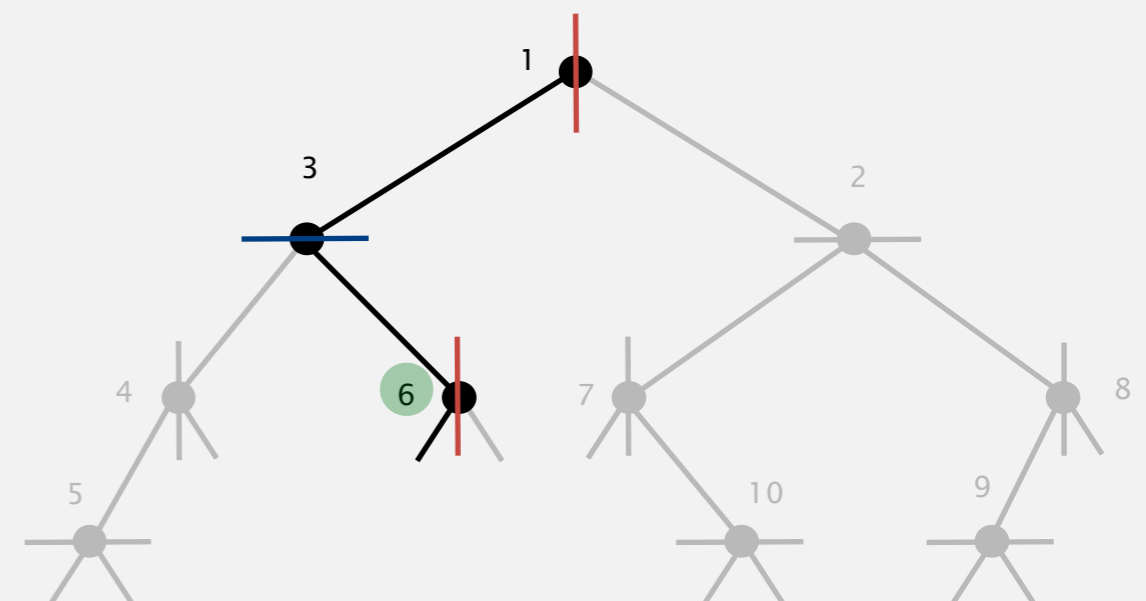
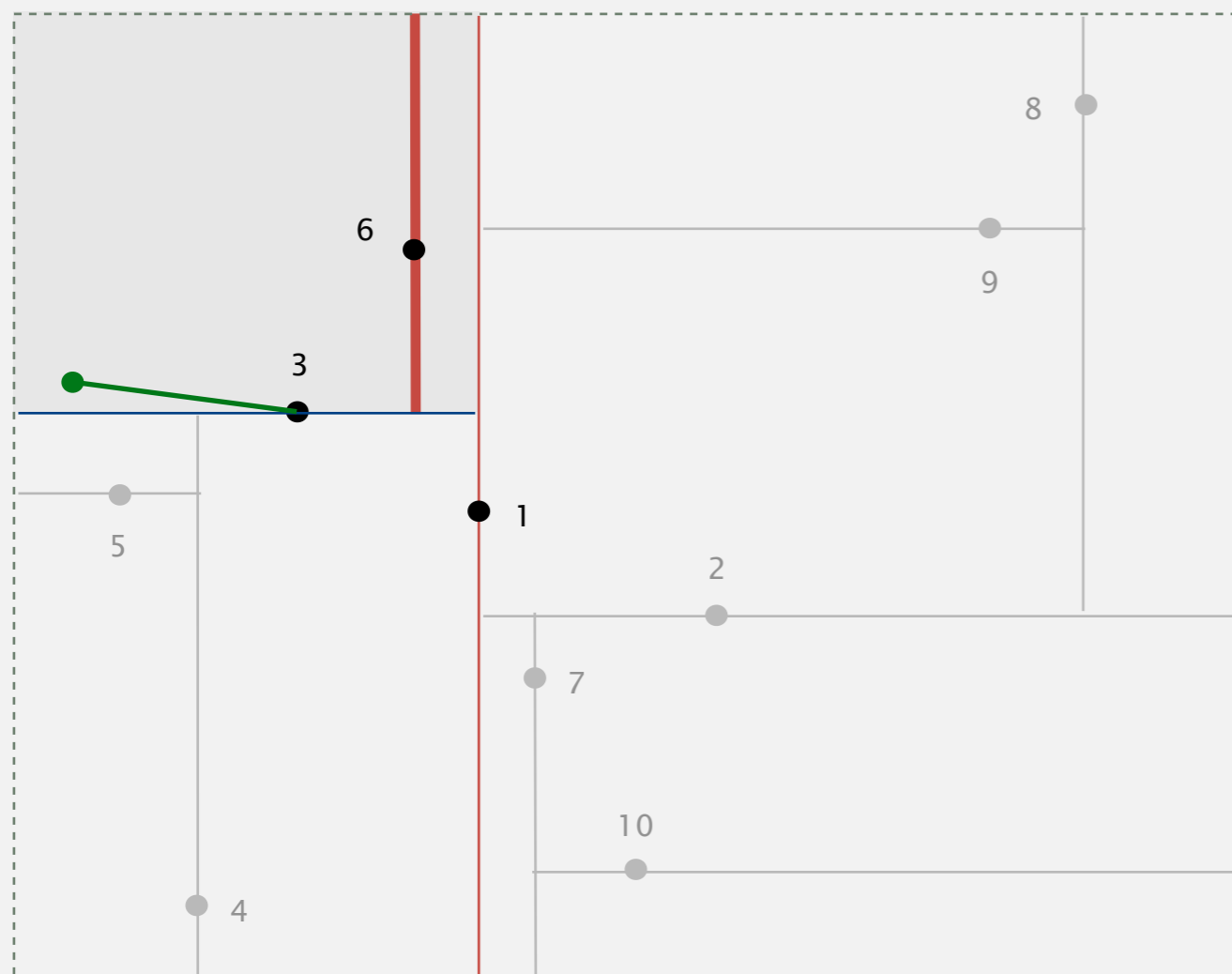
- Check distance from point in node to query point.
- Recursively search left/bottom subdivision (if it could contain a closer point).
- Recursively search right/top subdivision (if it could contain a closer point).
- Organize recursive method so that it begins by searching for query point.



**query point is to left of splitting line  
search left subtree first**

## Nearest neighbor search in a 2d tree

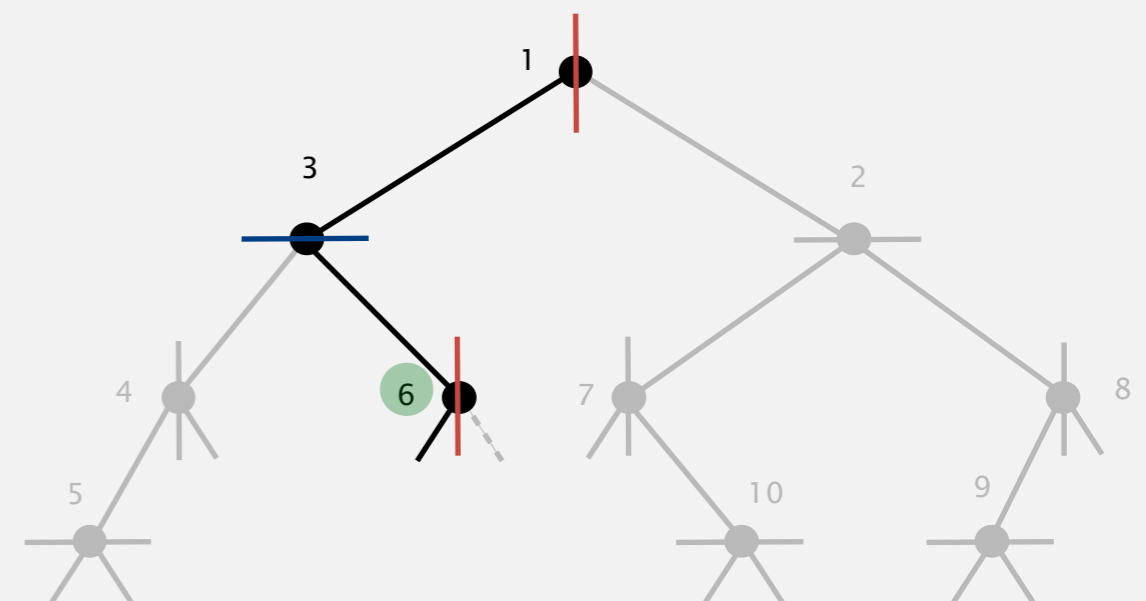
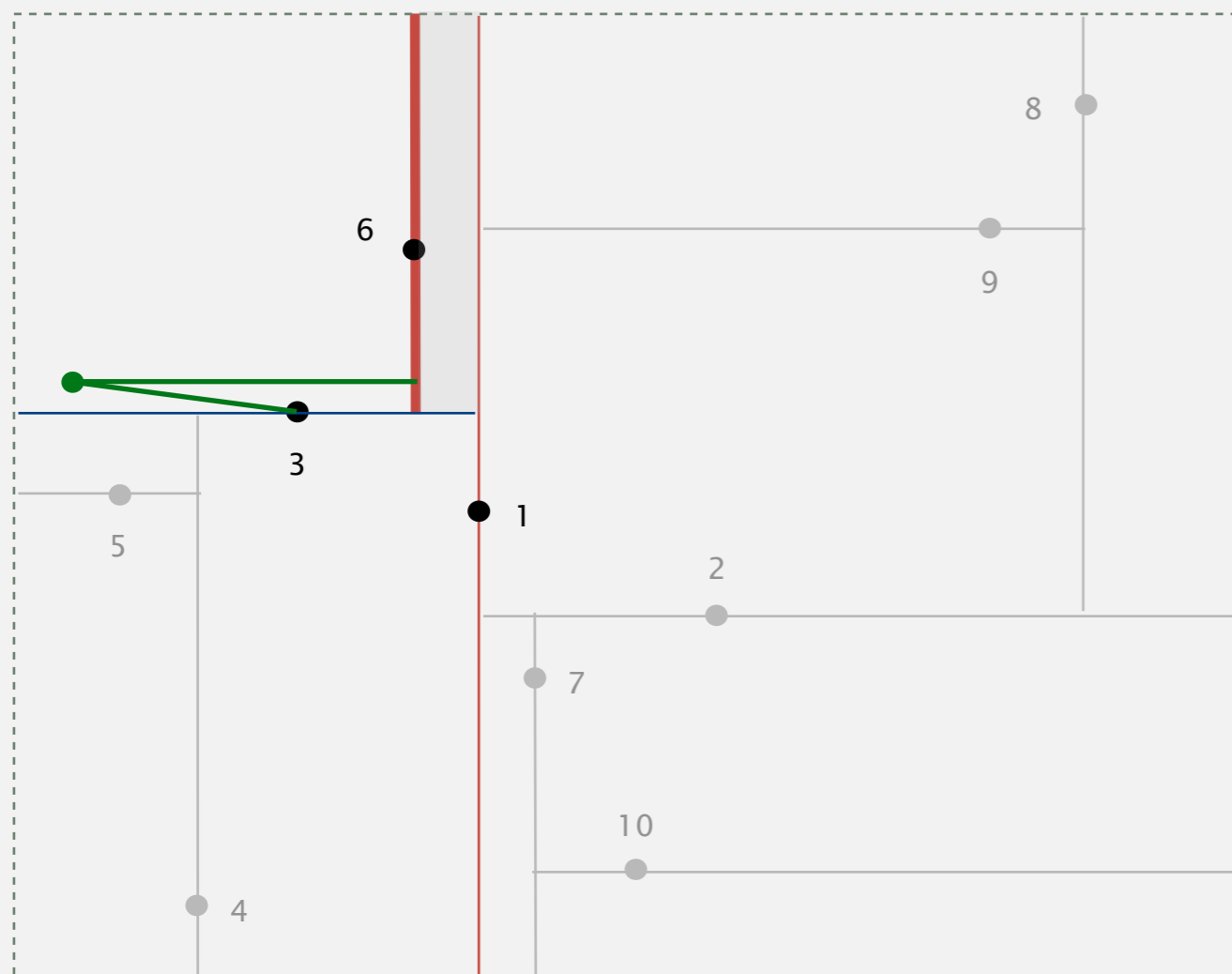
- Check distance from point in node to query point.
- Recursively search left/bottom subdivision (if it could contain a closer point).
- Recursively search right/top subdivision (if it could contain a closer point).
- Organize recursive method so that it begins by searching for query point.



**search left subtree  
return since empty**

## Nearest neighbor search in a 2d tree

- Check distance from point in node to query point.
- Recursively search left/bottom subdivision (if it could contain a closer point).
- Recursively search right/top subdivision (if it could contain a closer point).
- Organize recursive method so that it begins by searching for query point.

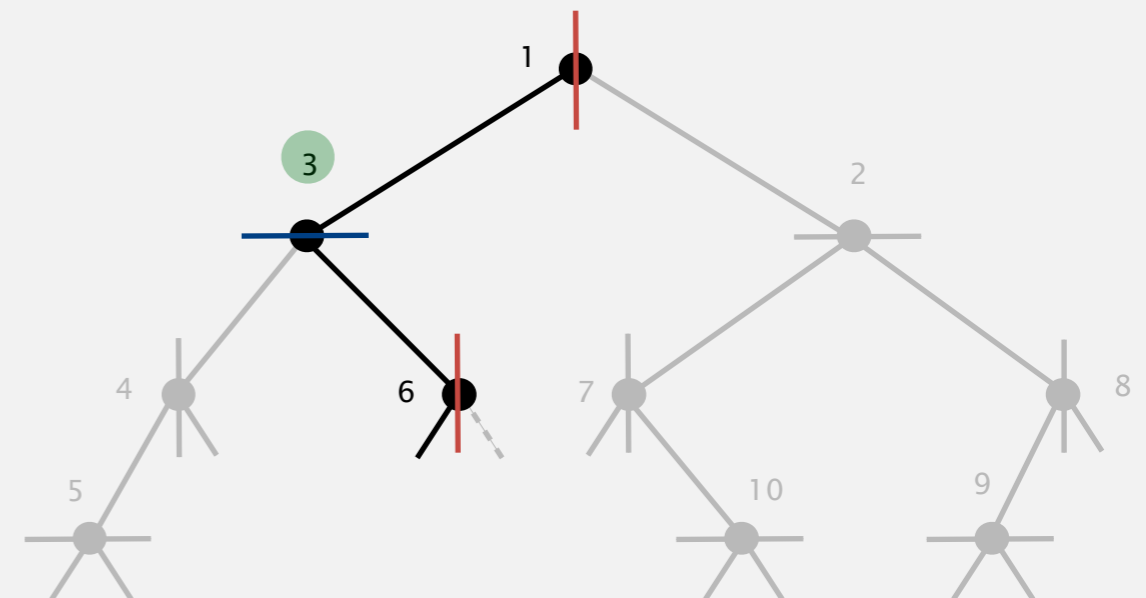
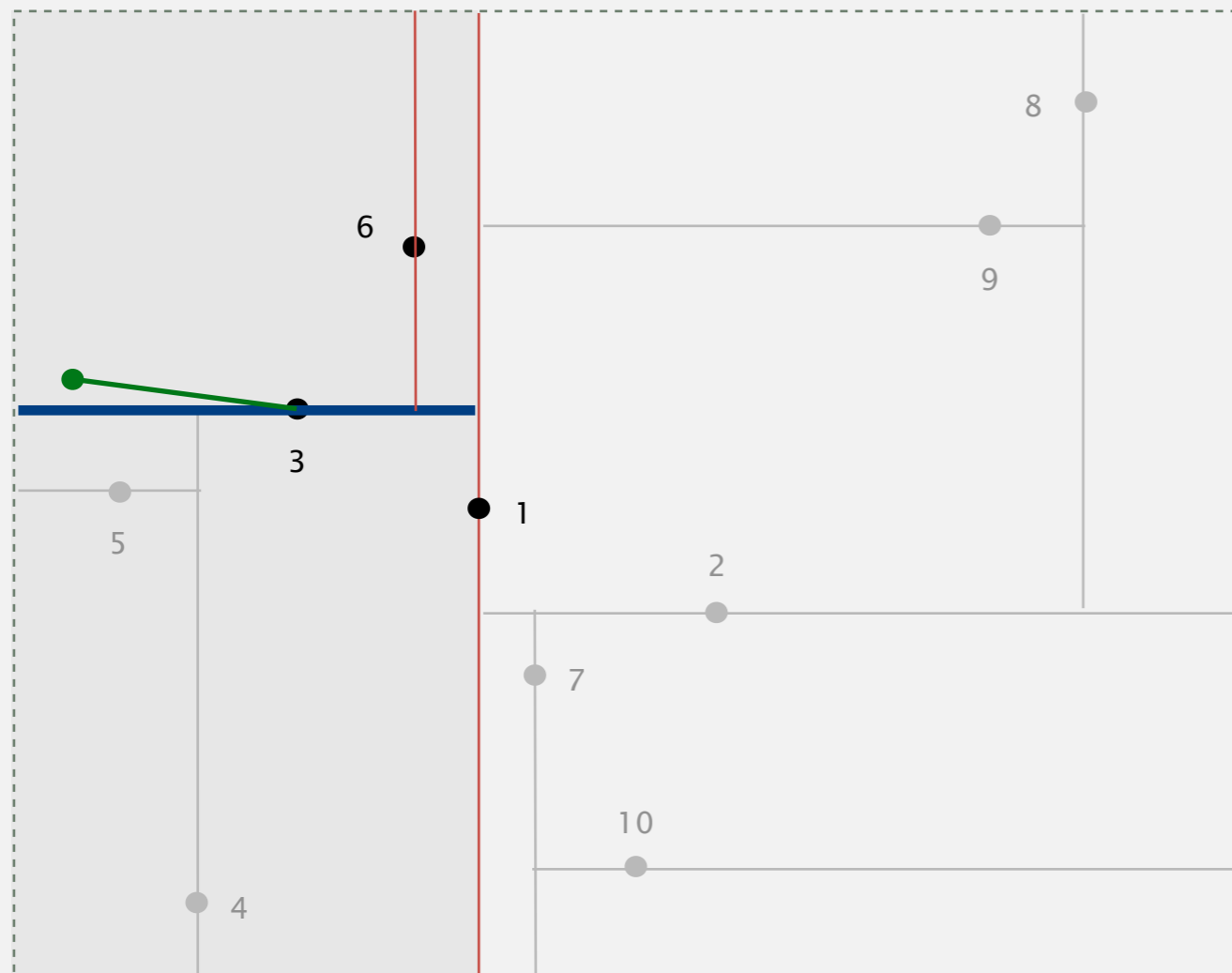


**search right subtree  
prune since nearest neighbor  
can't be in subdivision**



## Nearest neighbor search in a 2d tree

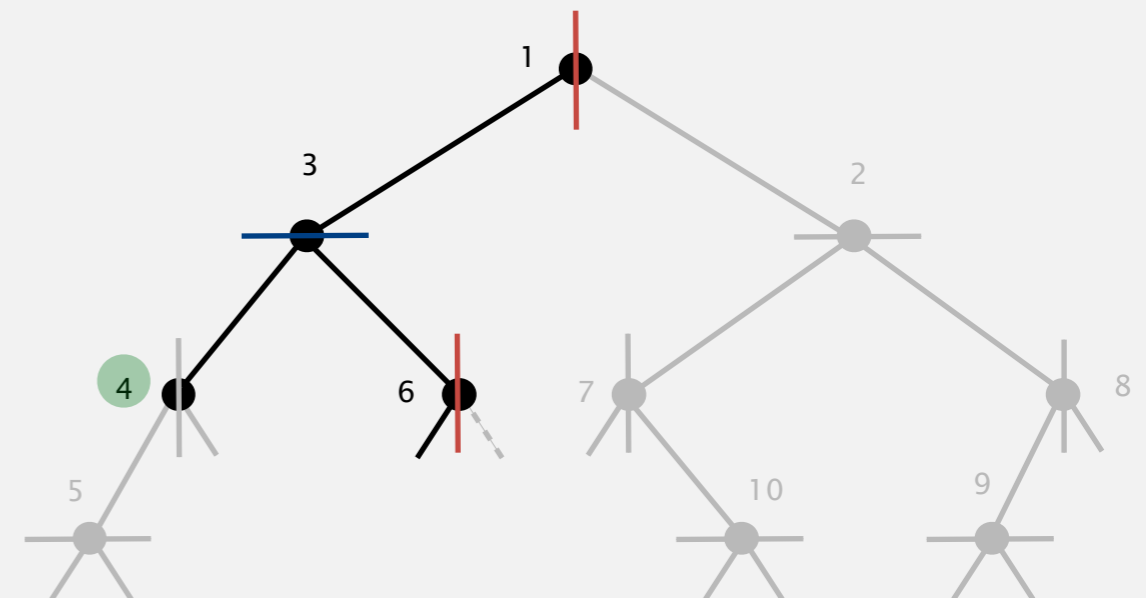
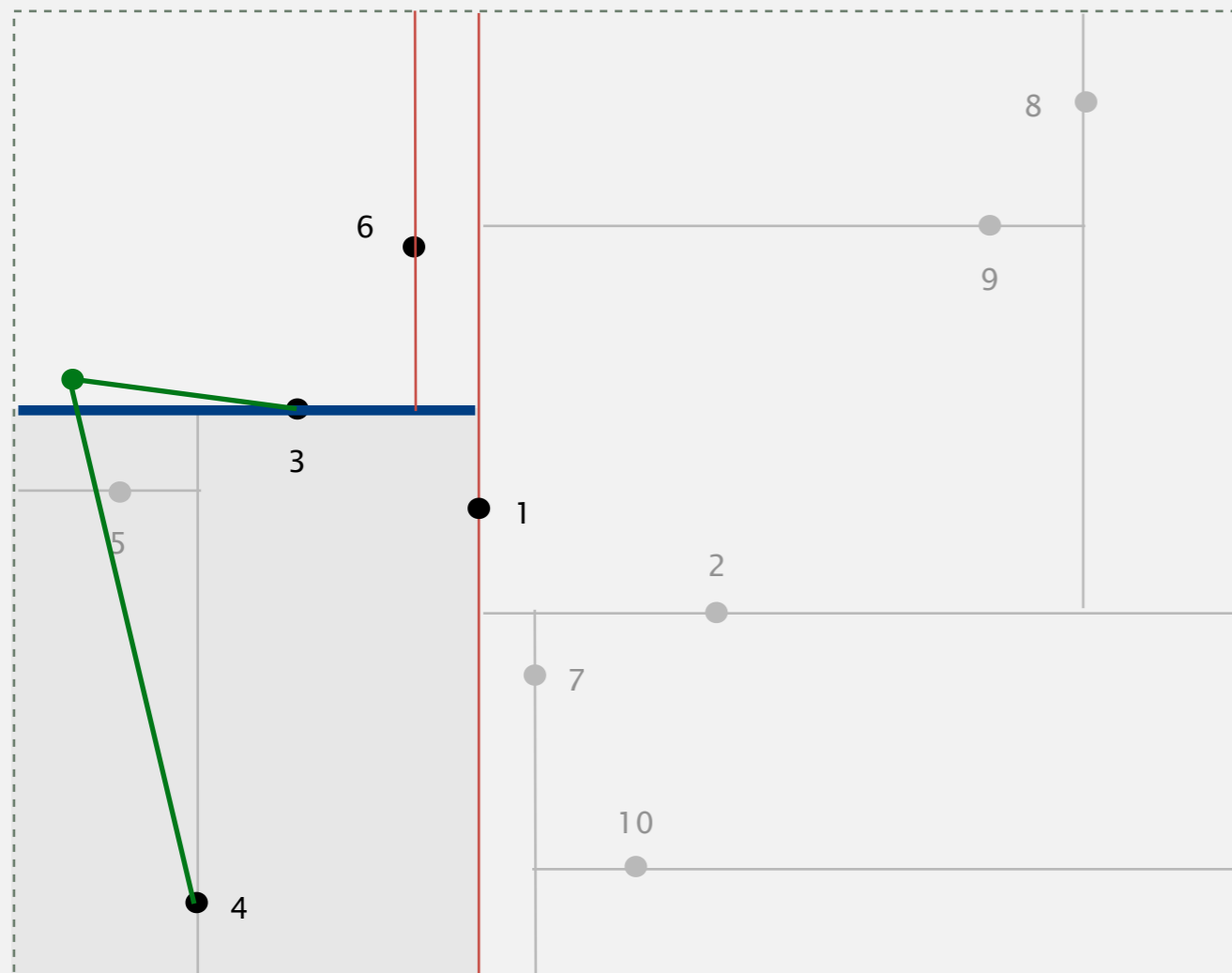
- Check distance from point in node to query point.
- Recursively search left/bottom subdivision (if it could contain a closer point).
- Recursively search right/top subdivision (if it could contain a closer point).
- Organize recursive method so that it begins by searching for query point.



return from function call  
search bottom subtree next

## Nearest neighbor search in a 2d tree

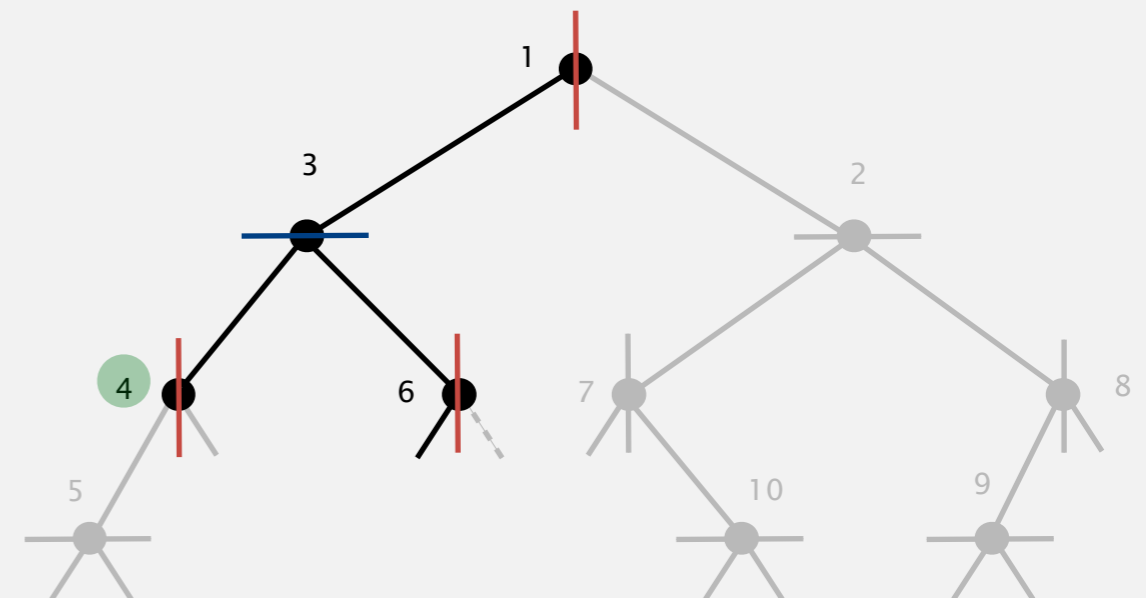
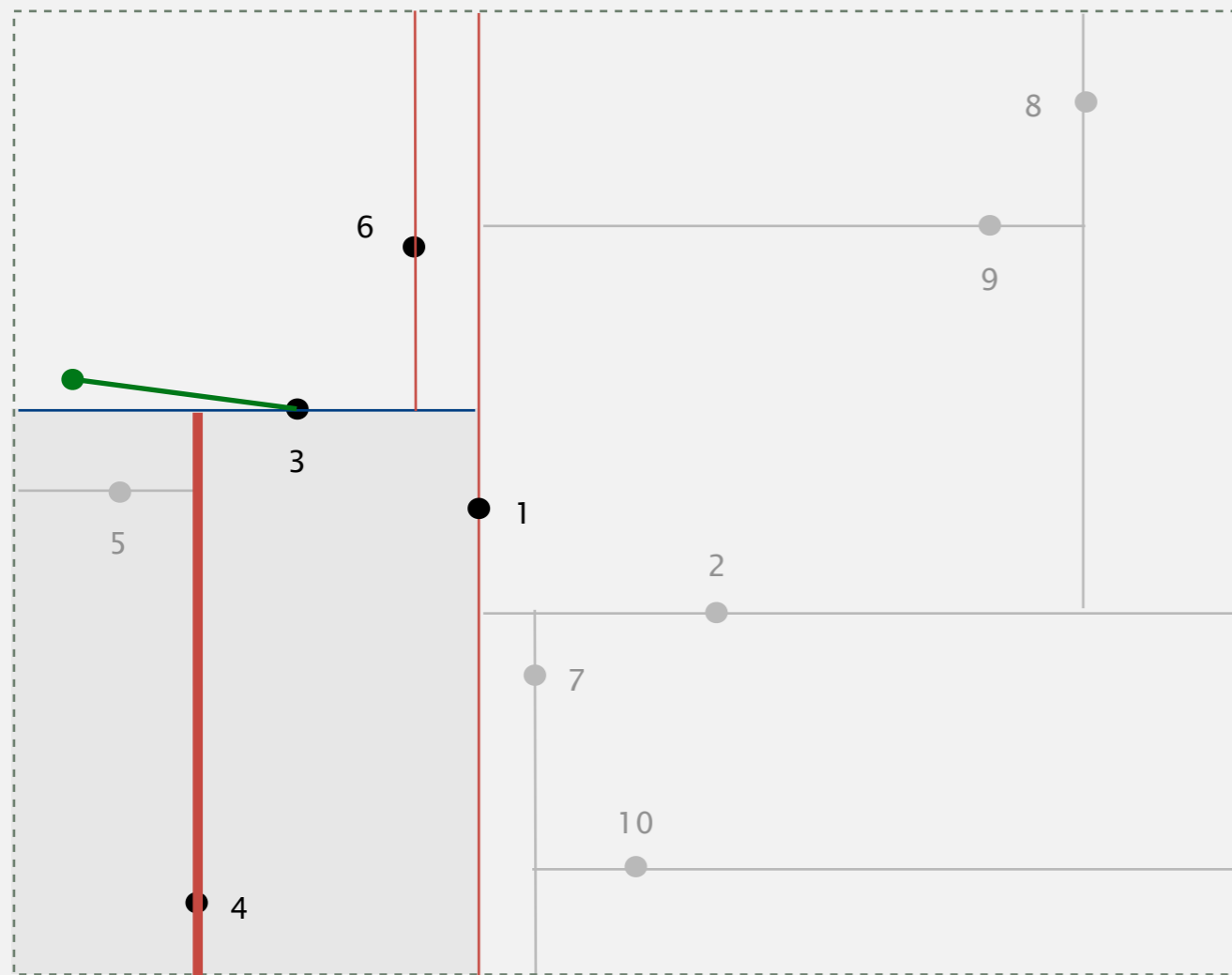
- Check distance from point in node to query point.
- Recursively search left/bottom subdivision (if it could contain a closer point).
- Recursively search right/top subdivision (if it could contain a closer point).
- Organize recursive method so that it begins by searching for query point.



**search bottom subtree**  
**compute distance from query point to 4**

## Nearest neighbor search in a 2d tree

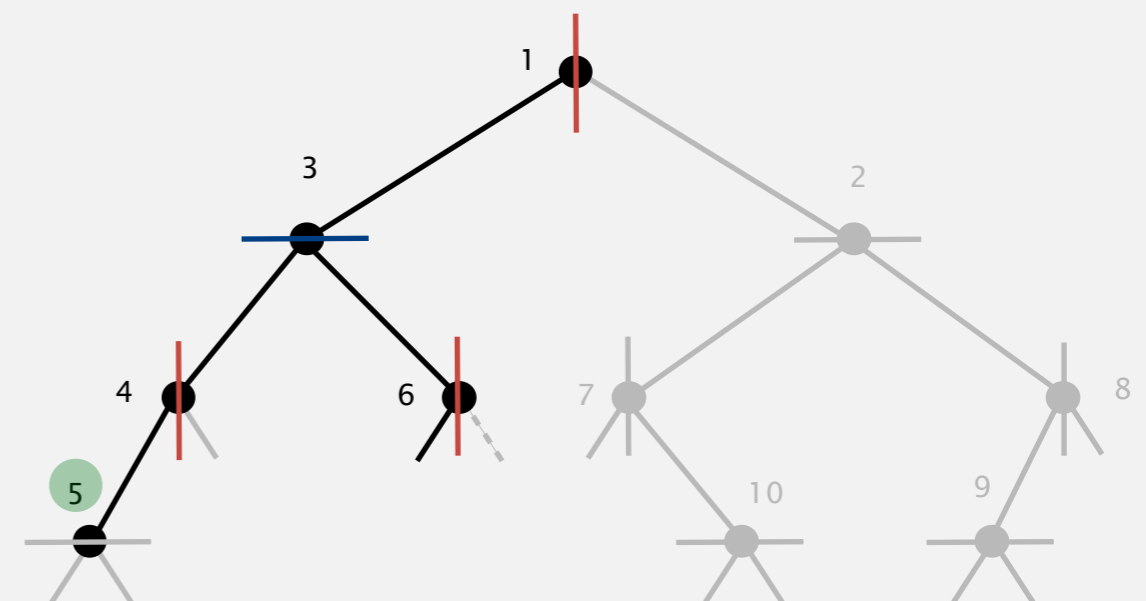
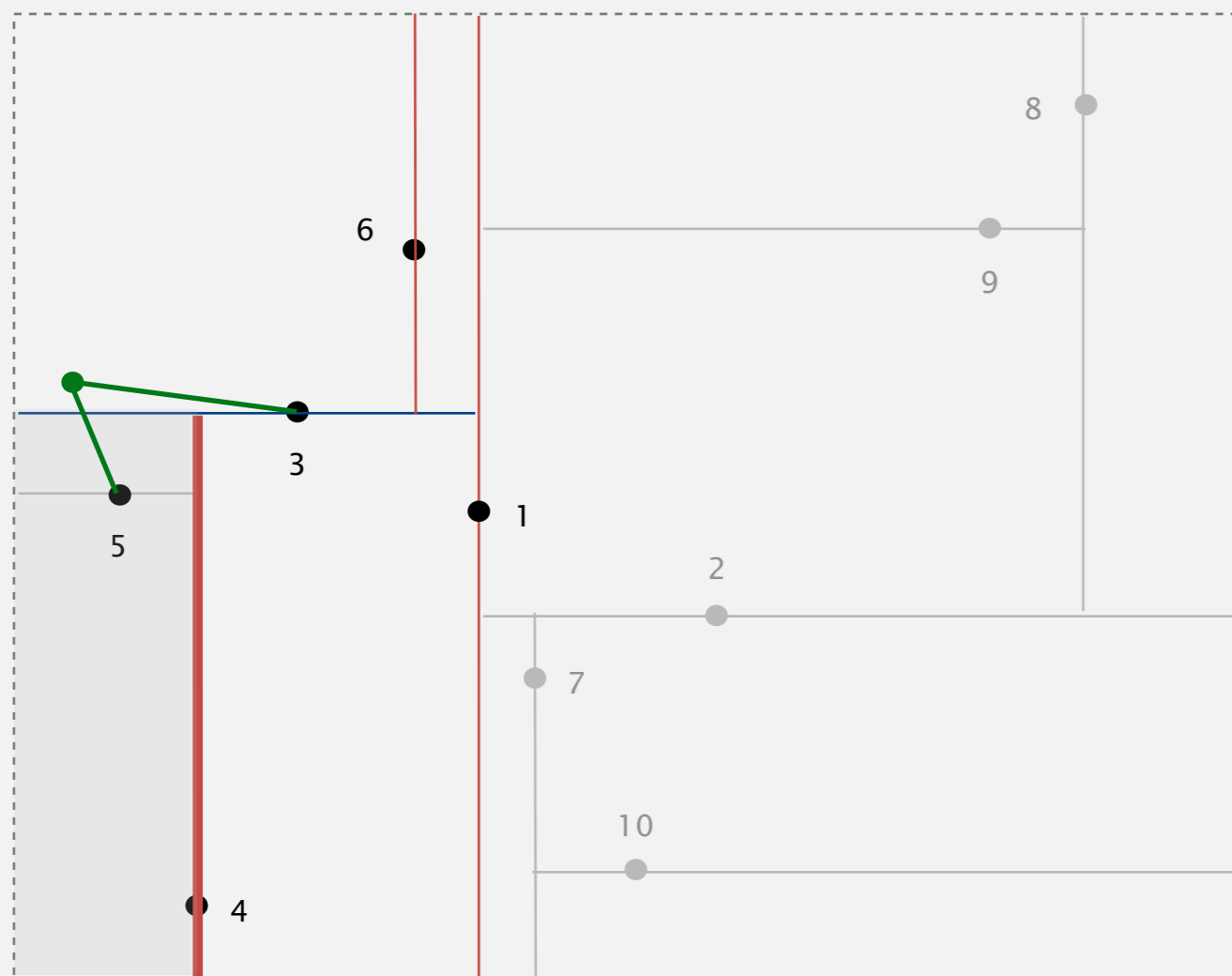
- Check distance from point in node to query point.
- Recursively search left/bottom subdivision (if it could contain a closer point).
- Recursively search right/top subdivision (if it could contain a closer point).
- Organize recursive method so that it begins by searching for query point.



**query point is to left of splitting line  
search left subtree first**

## Nearest neighbor search in a 2d tree

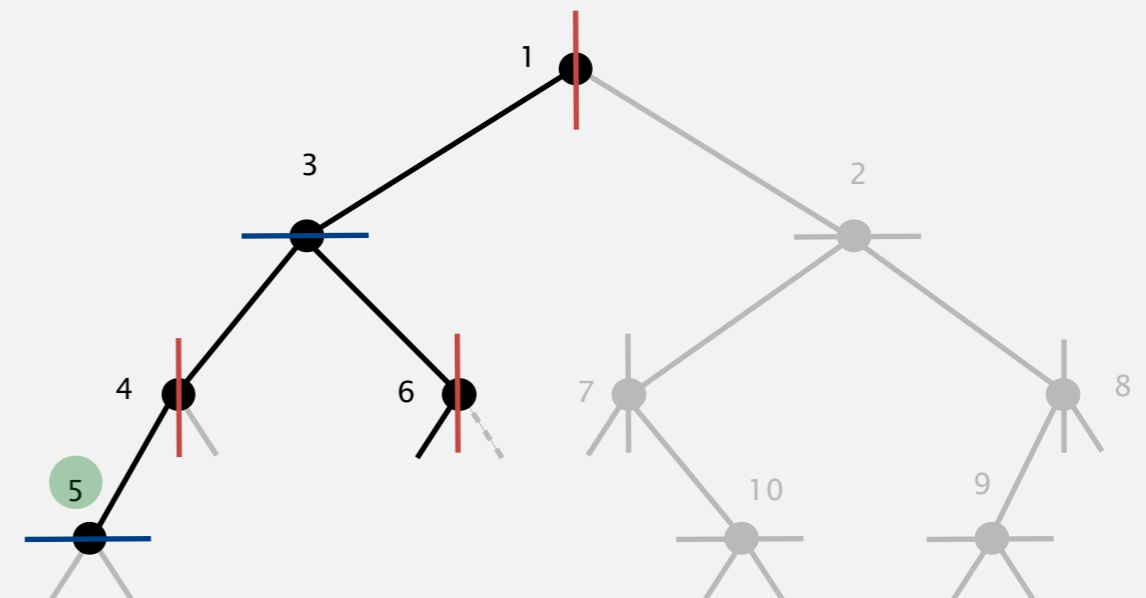
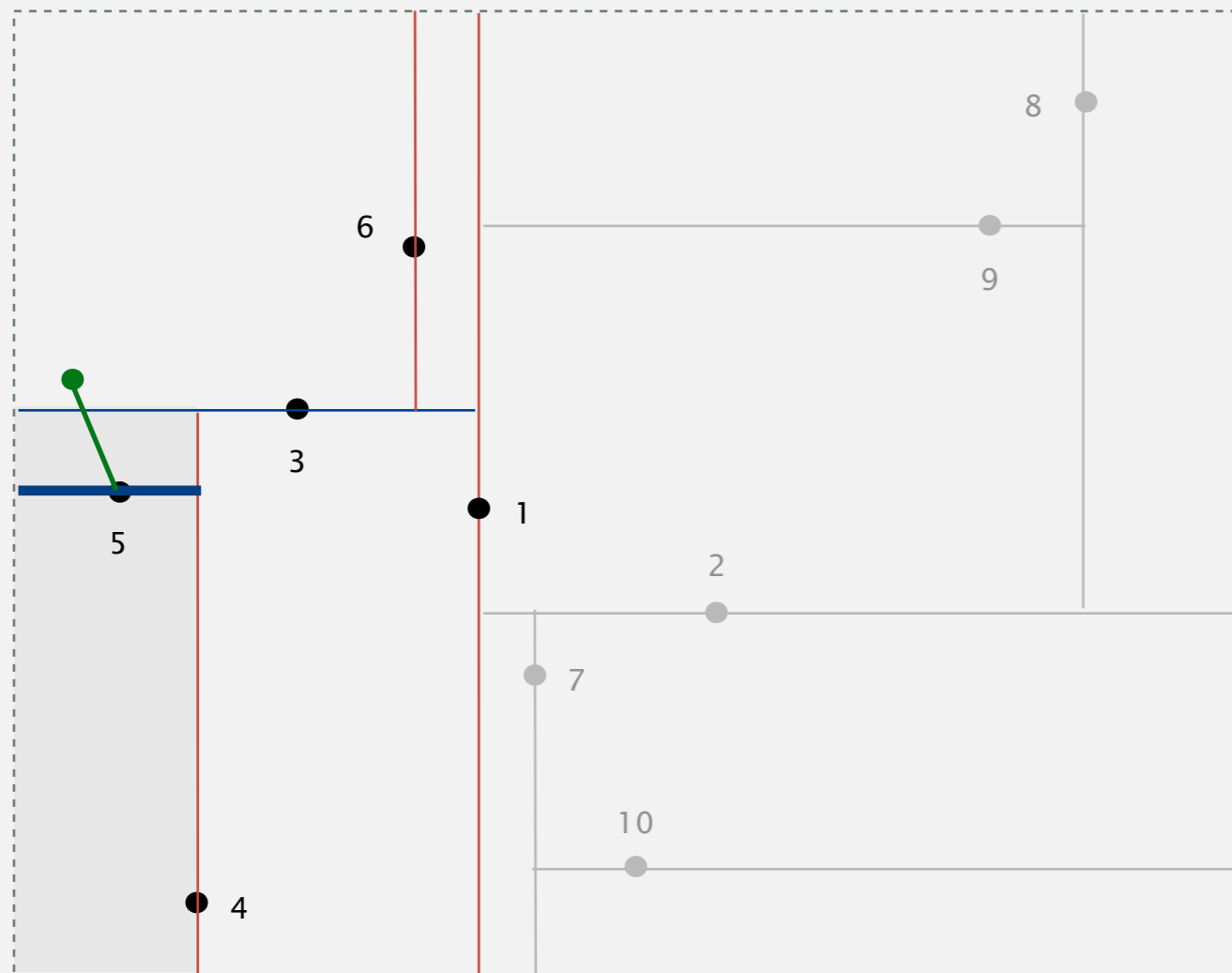
- Check distance from point in node to query point.
- Recursively search left/bottom subdivision (if it could contain a closer point).
- Recursively search right/top subdivision (if it could contain a closer point).
- Organize recursive method so that it begins by searching for query point.



**search left subtree**  
**compute distance from query point to 5**  
**(update champion)**

## Nearest neighbor search in a 2d tree

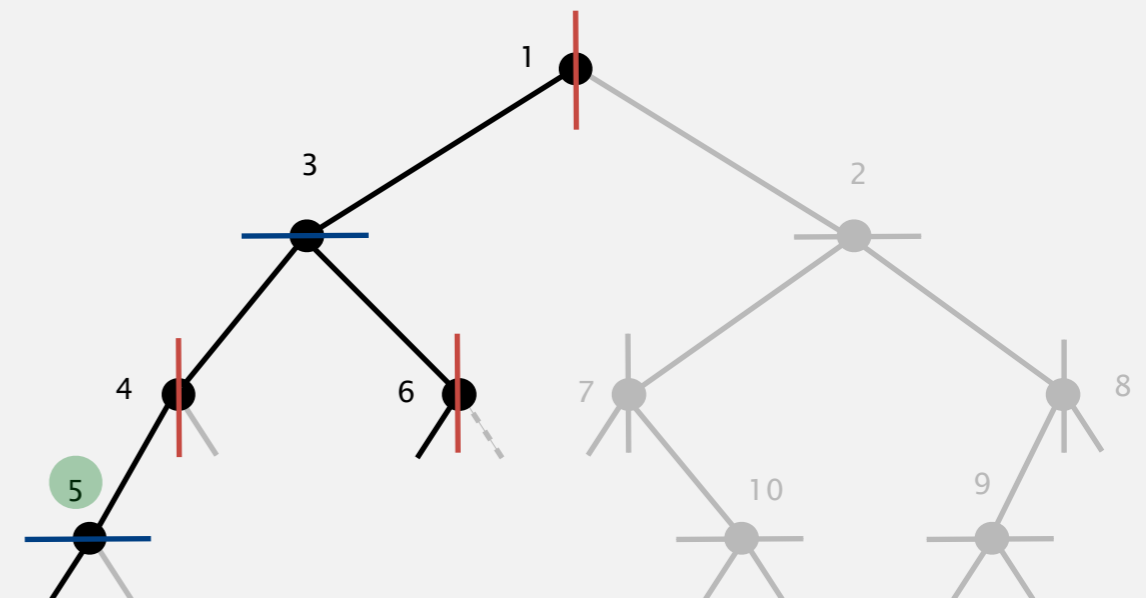
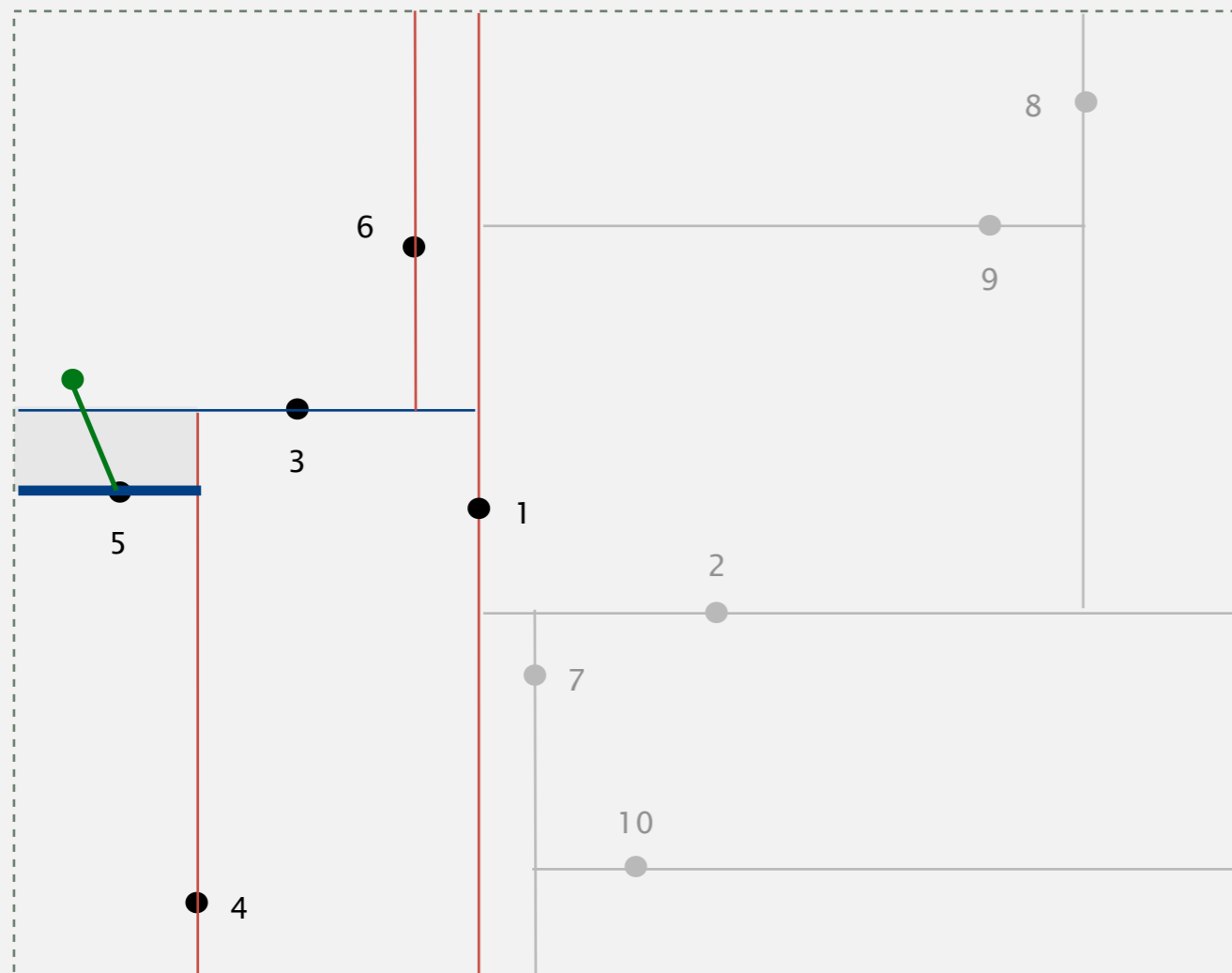
- Check distance from point in node to query point.
- Recursively search left/bottom subdivision (if it could contain a closer point).
- Recursively search right/top subdivision (if it could contain a closer point).
- Organize recursive method so that it begins by searching for query point.



**query point is above splitting line  
search top subtree first**

## Nearest neighbor search in a 2d tree

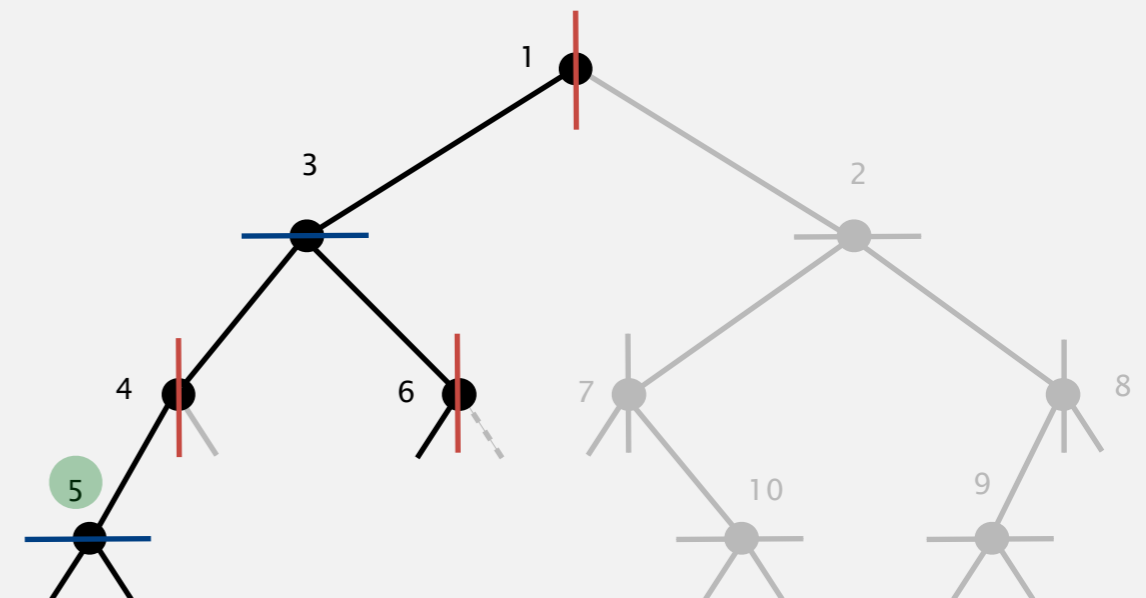
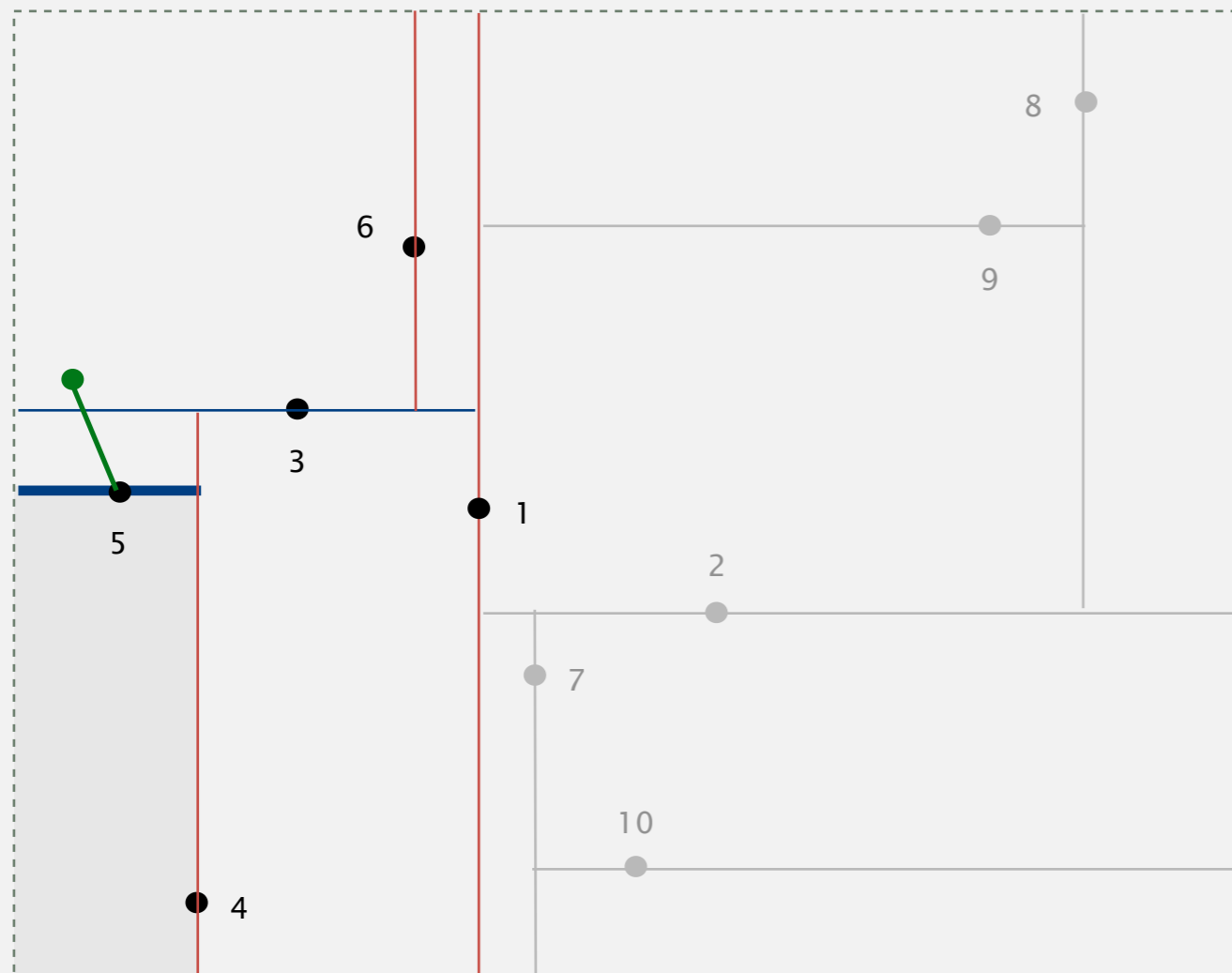
- Check distance from point in node to query point.
- Recursively search left/bottom subdivision (if it could contain a closer point).
- Recursively search right/top subdivision (if it could contain a closer point).
- Organize recursive method so that it begins by searching for query point.



search top subtree  
return since empty

## Nearest neighbor search in a 2d tree

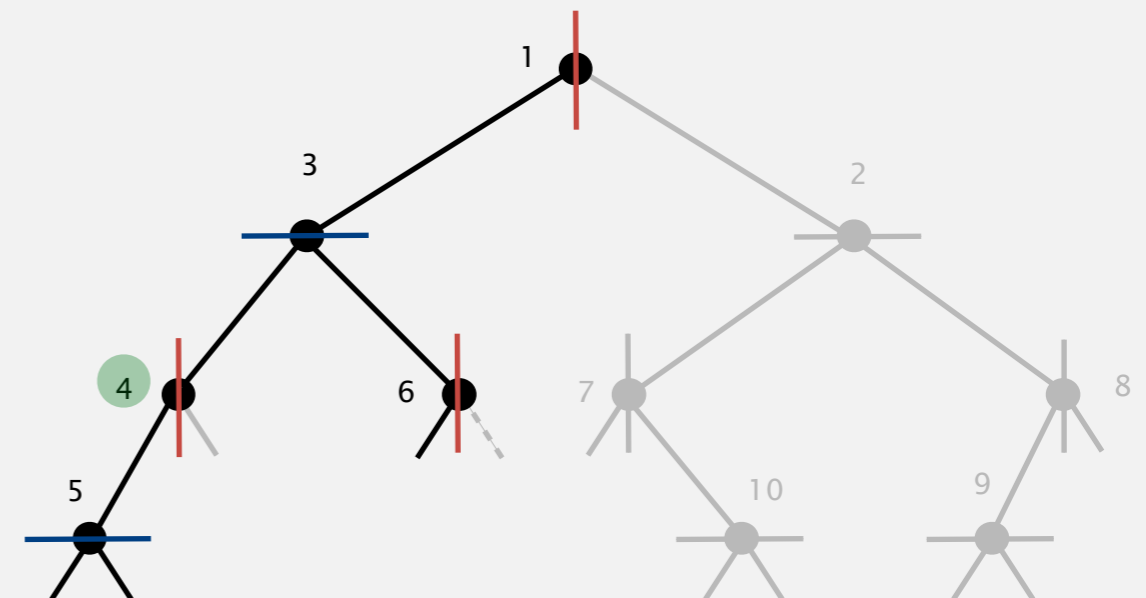
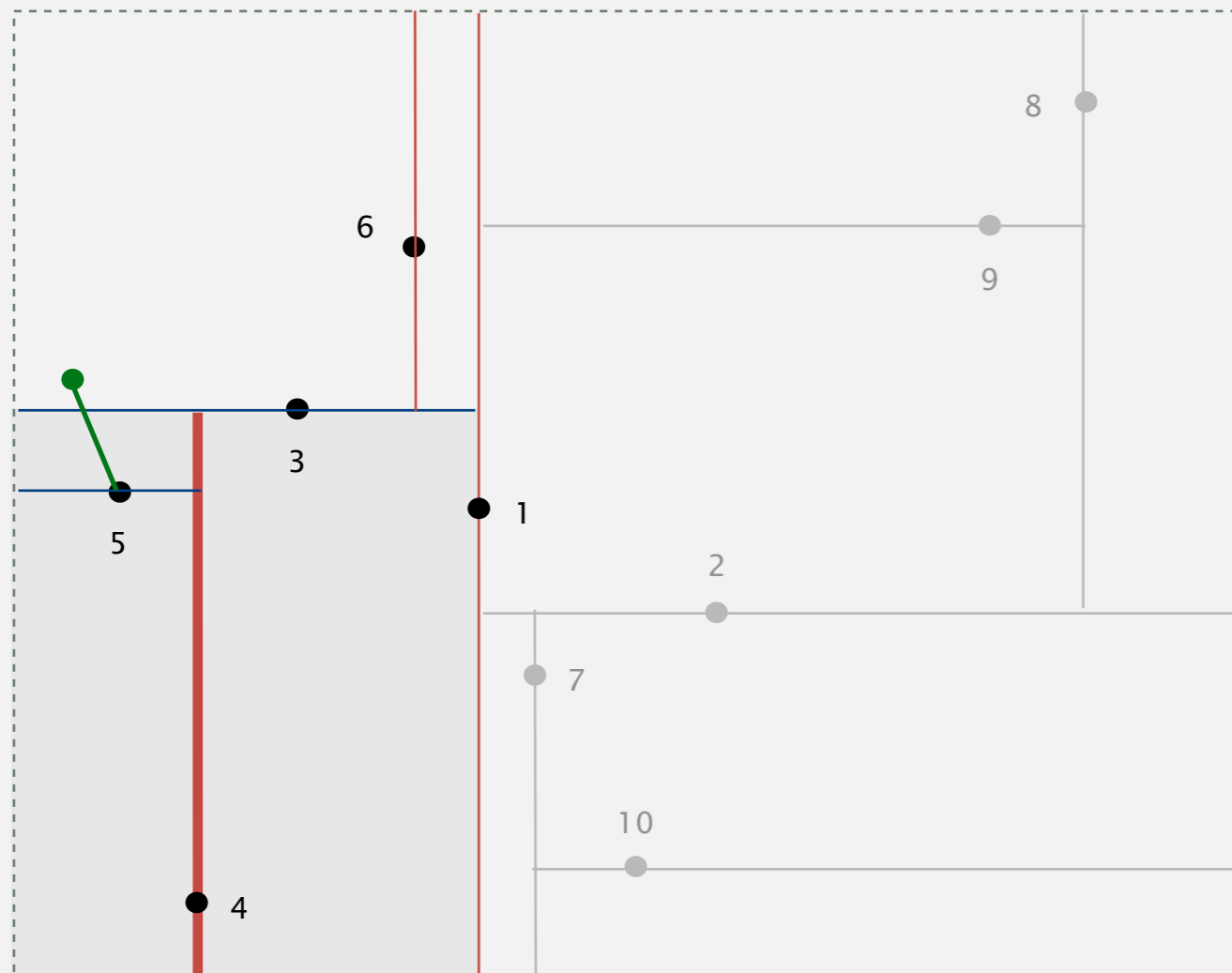
- Check distance from point in node to query point.
- Recursively search left/bottom subdivision (if it could contain a closer point).
- Recursively search right/top subdivision (if it could contain a closer point).
- Organize recursive method so that it begins by searching for query point.



**search bottom subtree  
return since empty**

## Nearest neighbor search in a 2d tree

- Check distance from point in node to query point.
- Recursively search left/bottom subdivision (if it could contain a closer point).
- Recursively search right/top subdivision (if it could contain a closer point).
- Organize recursive method so that it begins by searching for query point.

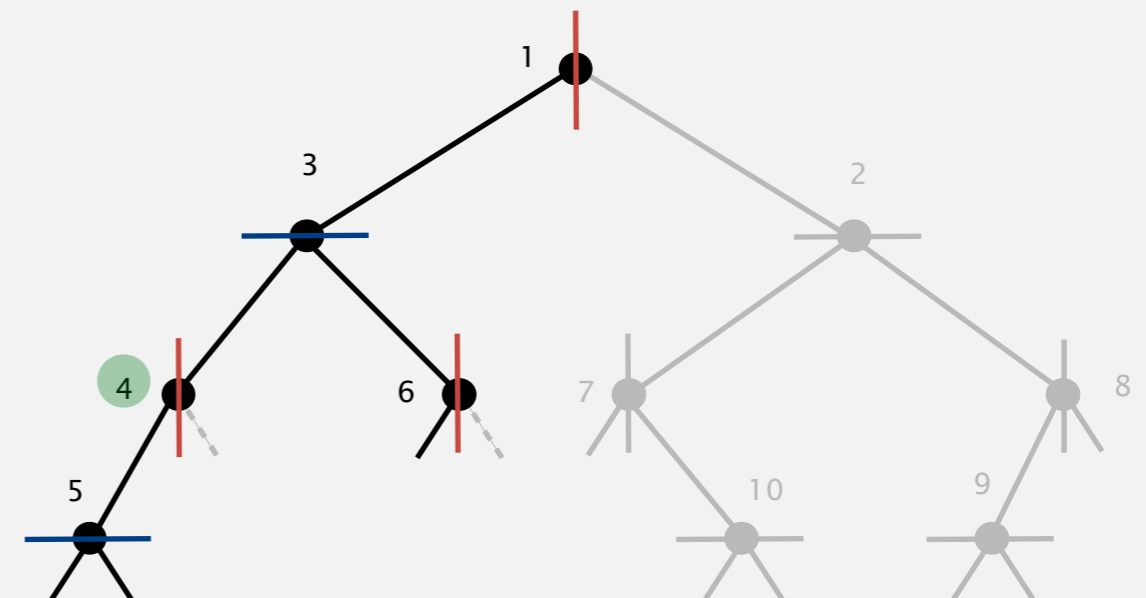
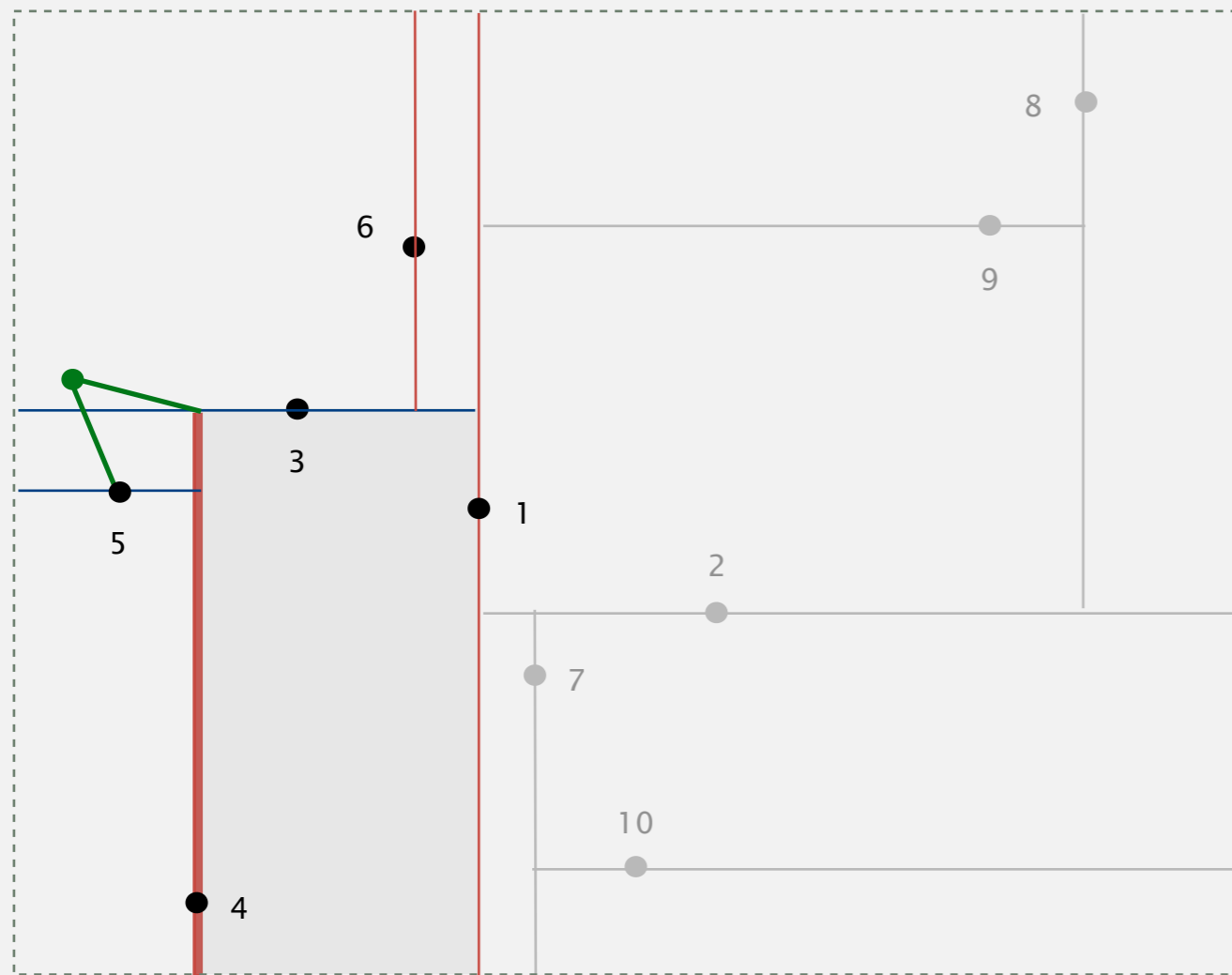


return from function call  
search right subtree next



## Nearest neighbor search in a 2d tree

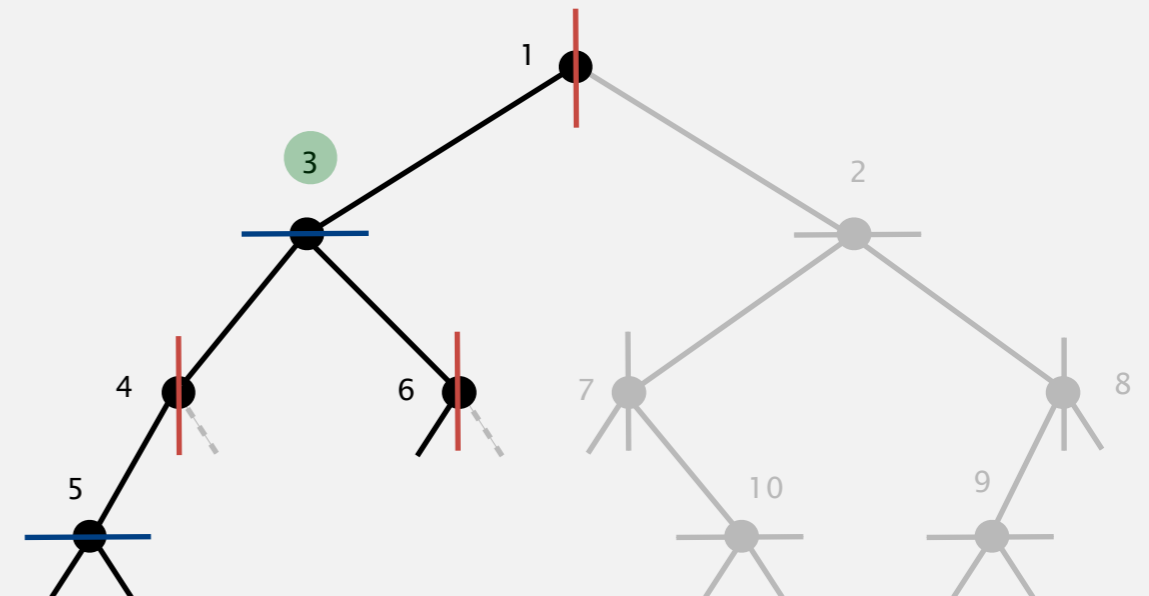
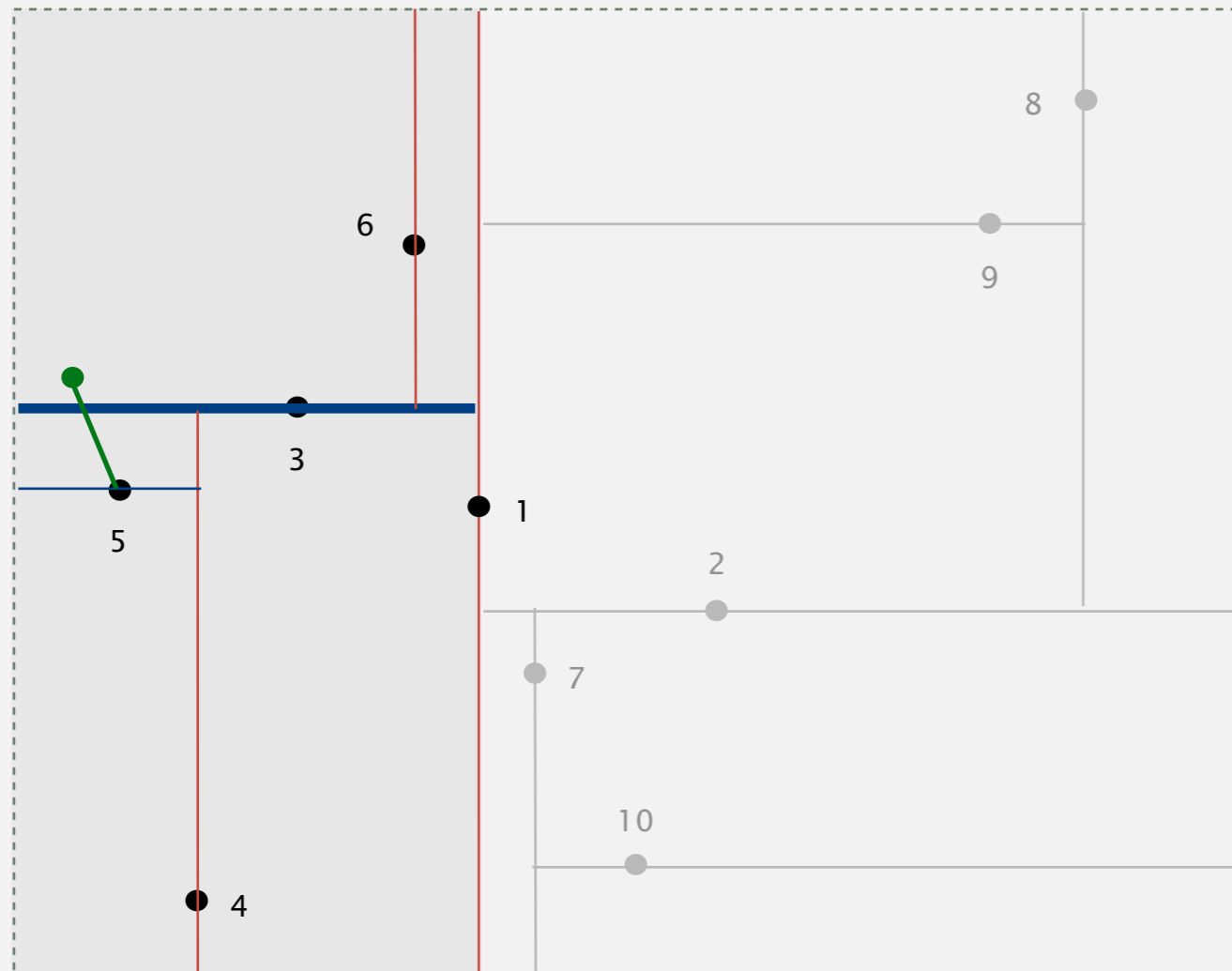
- Check distance from point in node to query point.
- Recursively search left/bottom subdivision (if it could contain a closer point).
- Recursively search right/top subdivision (if it could contain a closer point).
- Organize recursive method so that it begins by searching for query point.



**search right subtree  
prune since nearest neighbor  
can't be in subdivision**

## Nearest neighbor search in a 2d tree

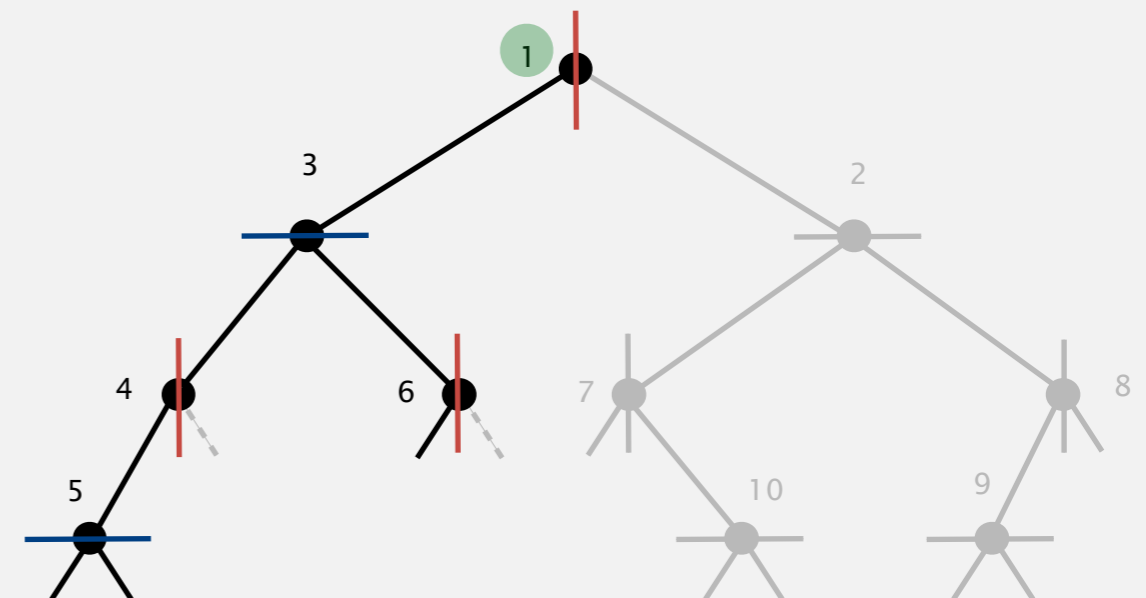
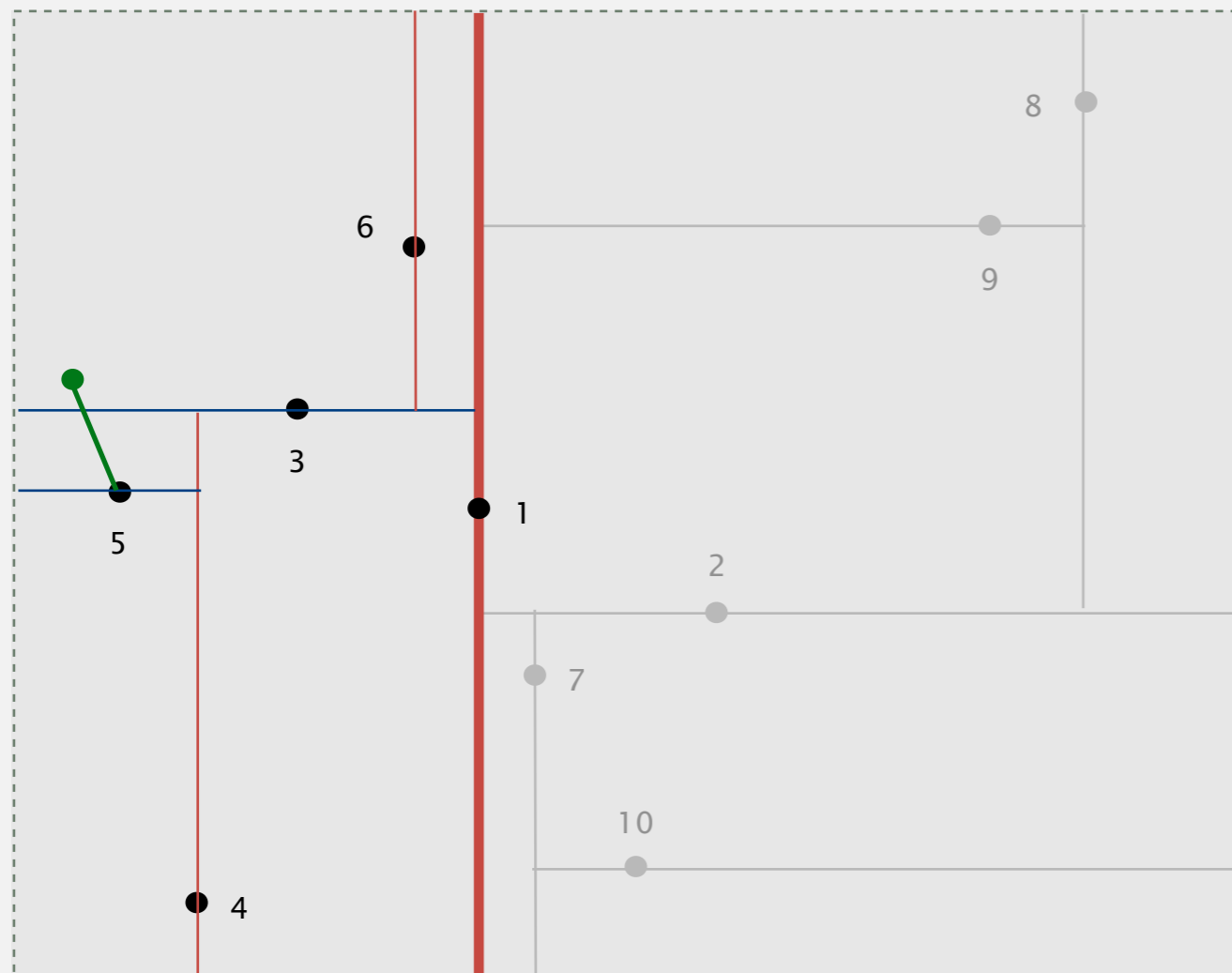
- Check distance from point in node to query point.
- Recursively search left/bottom subdivision (if it could contain a closer point).
- Recursively search right/top subdivision (if it could contain a closer point).
- Organize recursive method so that it begins by searching for query point.



return from function call

## Nearest neighbor search in a 2d tree

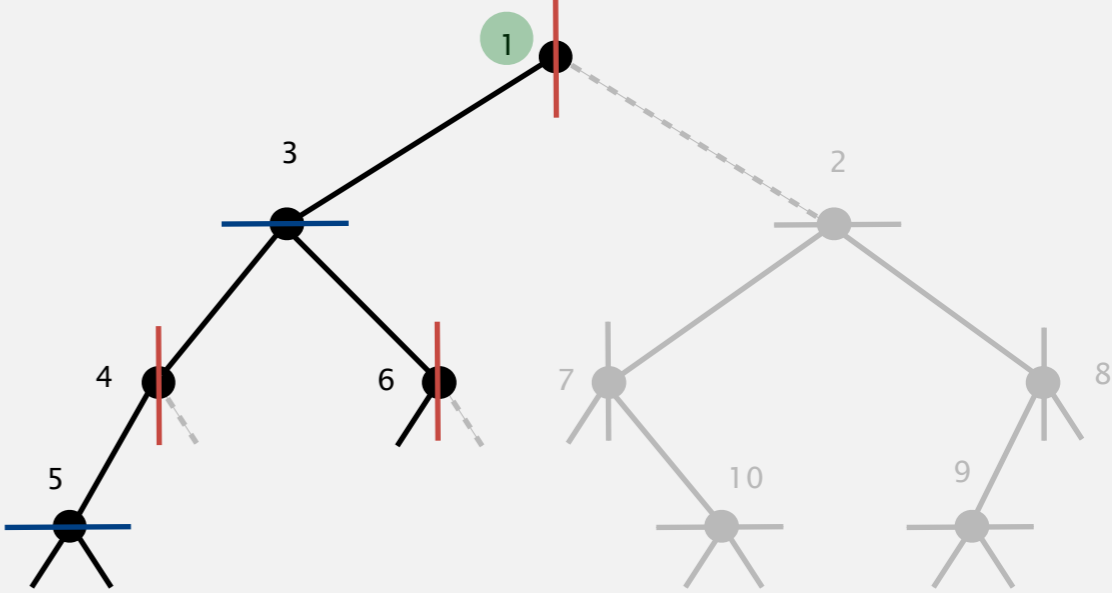
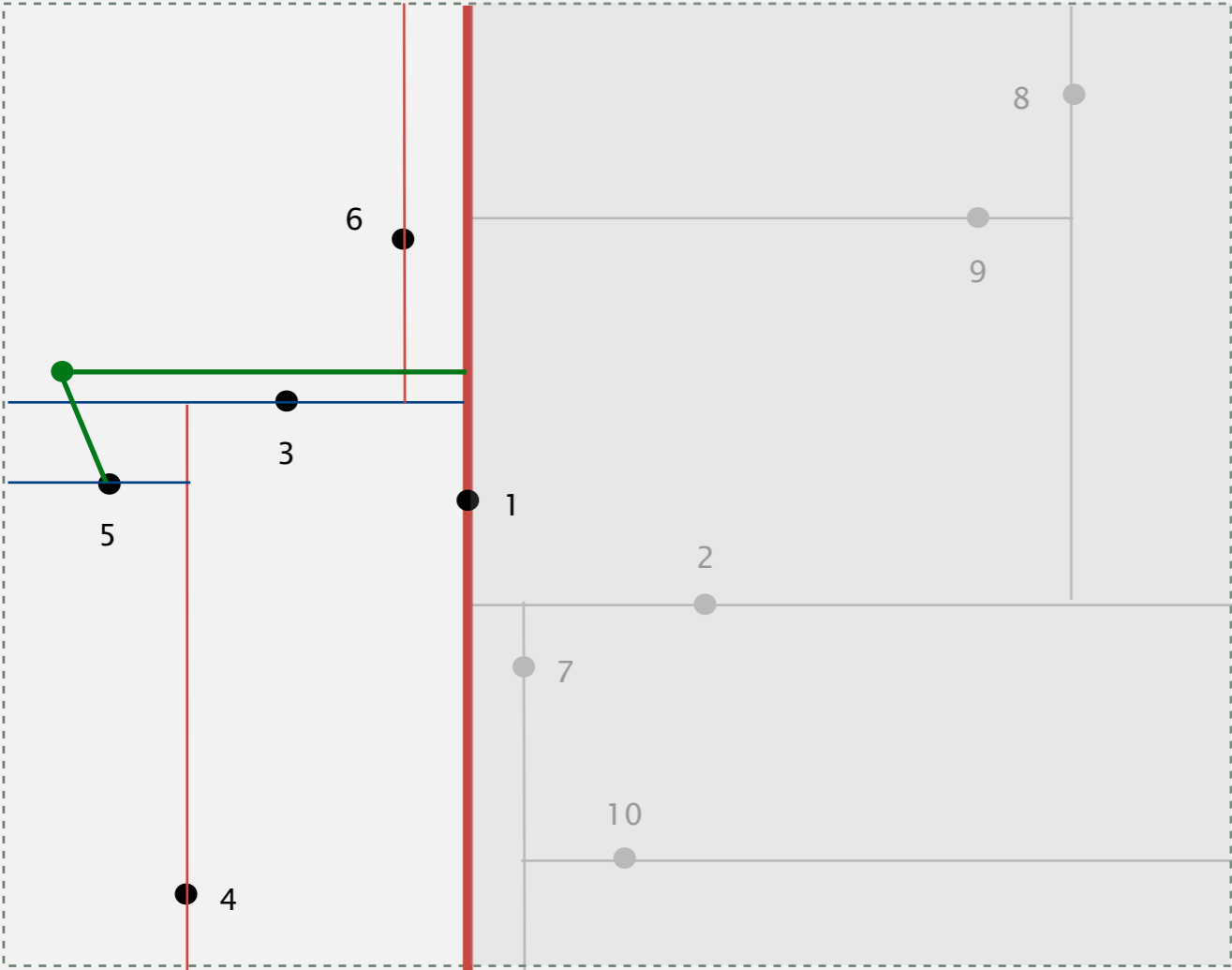
- Check distance from point in node to query point.
- Recursively search left/bottom subdivision (if it could contain a closer point).
- Recursively search right/top subdivision (if it could contain a closer point).
- Organize recursive method so that it begins by searching for query point.



return from function call  
search right subtree next

# Nearest neighbor search in a 2d tree

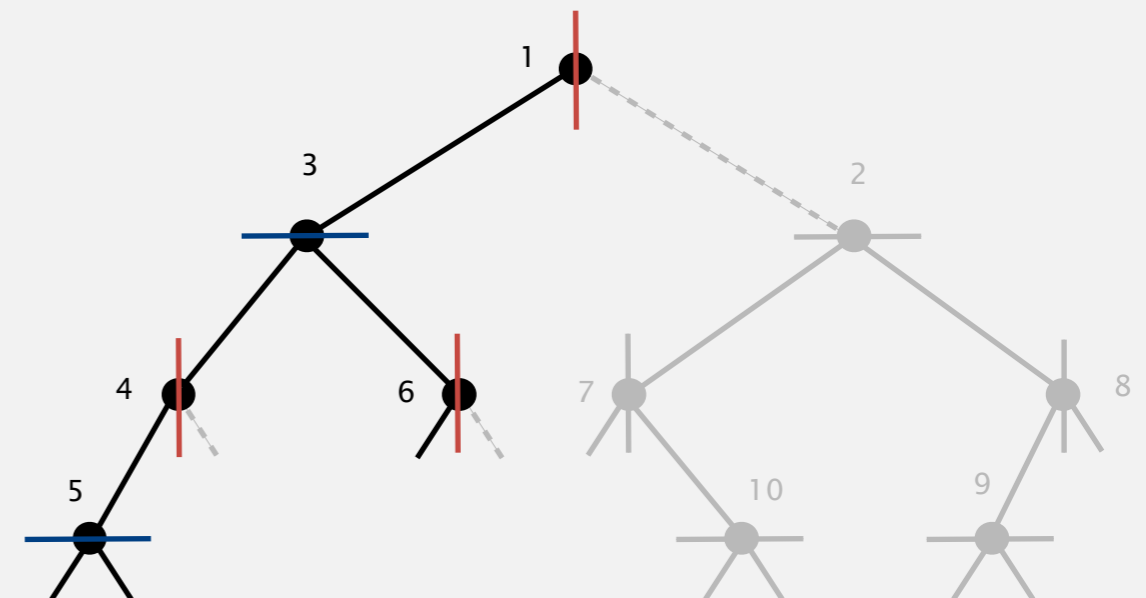
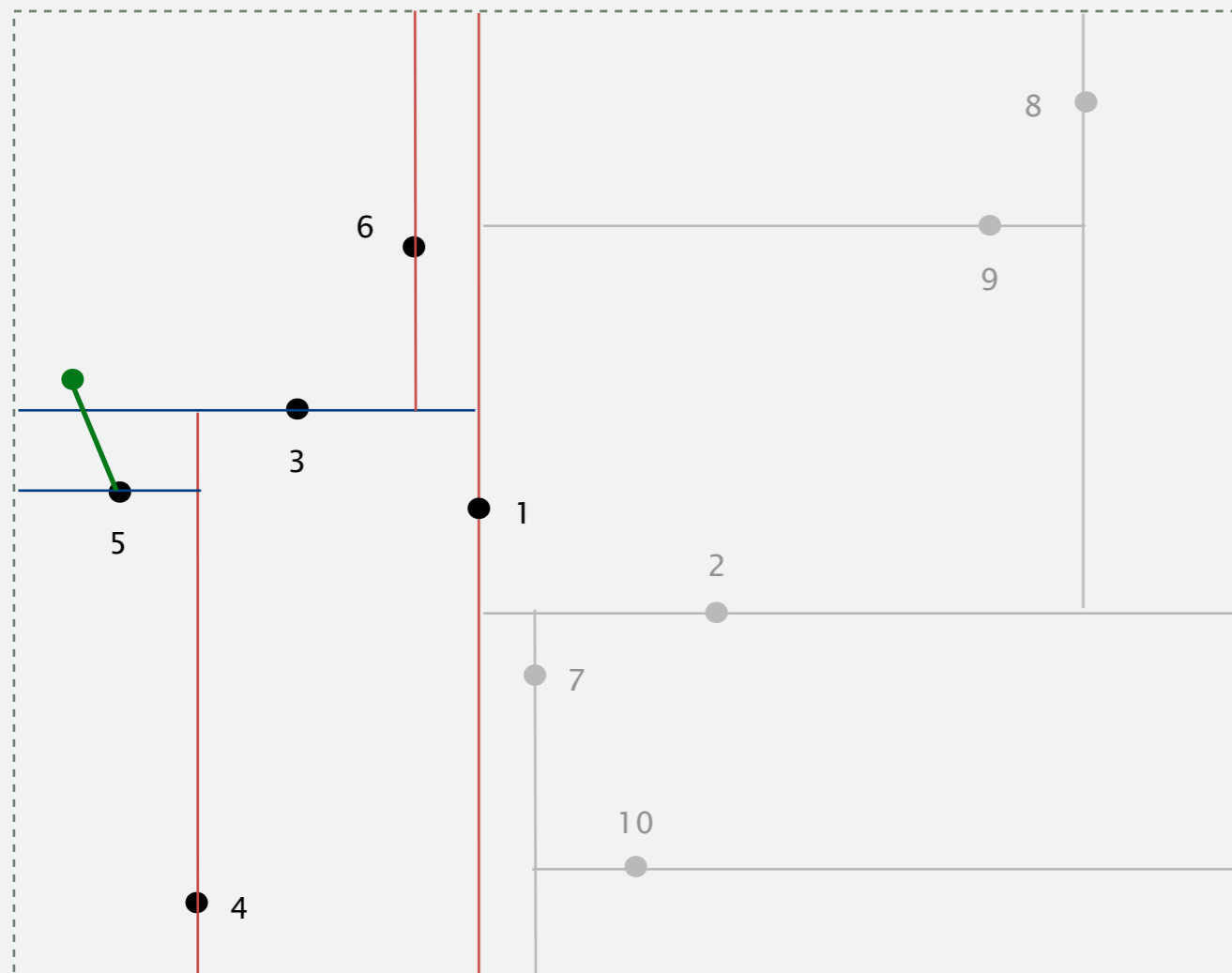
- Check distance from point in node to query point.
- Recursively search left/bottom subdivision (if it could contain a closer point).
- Recursively search right/top subdivision (if it could contain a closer point).
- Organize recursive method so that it begins by searching for query point.



search right subtree  
prune since nearest neighbor  
can't be in subdivision

## Nearest neighbor search in a 2d tree

- Check distance from point in node to query point.
- Recursively search left/bottom subdivision (if it could contain a closer point).
- Recursively search right/top subdivision (if it could contain a closer point).
- Organize recursive method so that it begins by searching for query point.



nearest neighbor = 5